

Full Spectrum Boost in Nanoparticle Solar Cells

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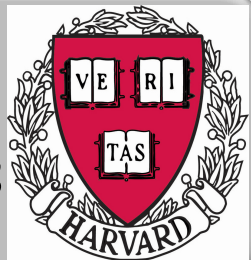
Chicago:
G.Galli



Nancy:
D.Rocca



Harvard:
T.Kaxiras



Max Planck:
S.Wippermann

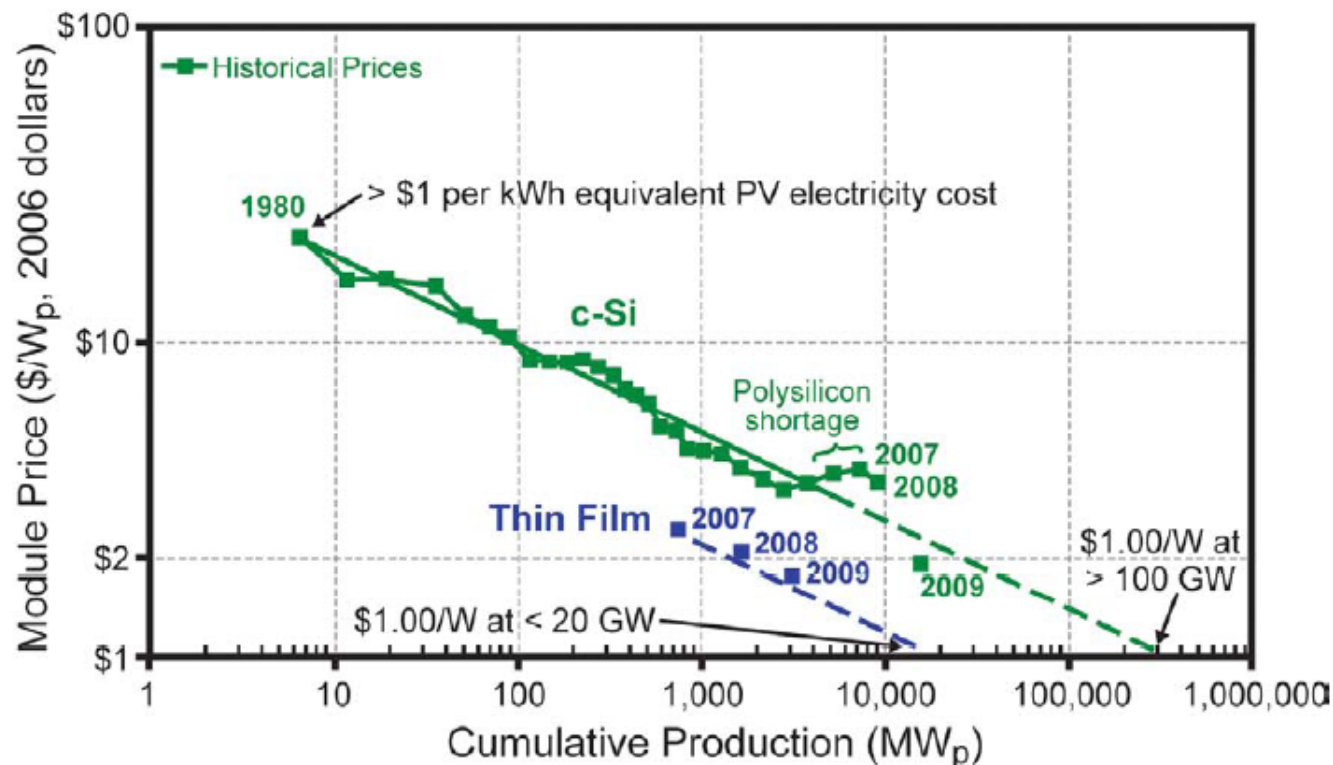


I do as I preach



Our "Solar Snow Koan" camp at Burning Man

DOE Goal - Reach grid parity at 1\$/W



The Solar Moore's Law:

Price drops by 20% for every doubling of production

No doubling per 18 months: area is not scaled down as in chips

DOE Sunshot initiative: Reach grid parity at 1\$/W!

Present Day

Present status: 0.53-0.72 \$/W: Economy of scales, strong production in China: DOE's SunShot goal achieved early!

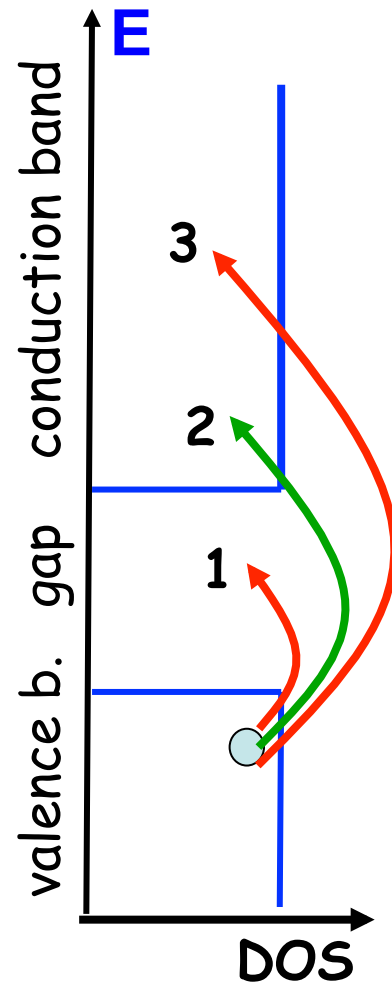
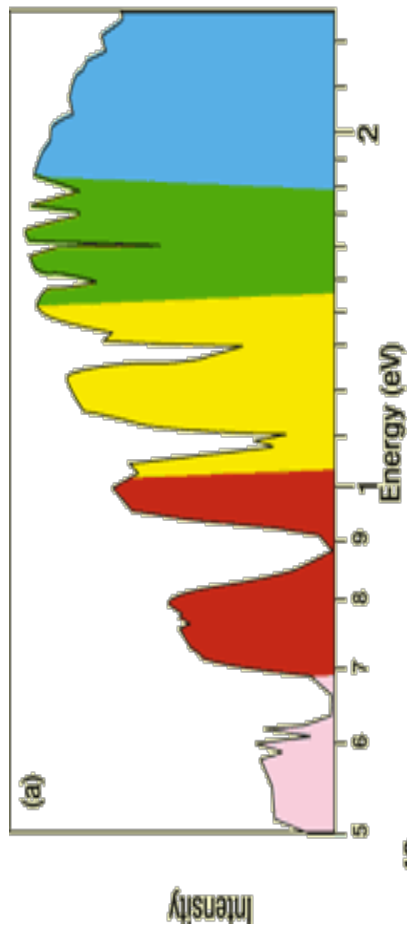
Present records:

GaAs	29%	Alta Devices
HIT c-Si cell	26%	Panasonic, SunPower
Thin film CdTe	20%	First Solar
Organic solar cells	12%	Sumitomo

BUT: (1) Fracking moved grid parity to ~0.3\$/W
(2) Energy problem needs pursuing all promising ideas

Bold & Innovative PV designs are needed

Solar Energy Conversion: Basics



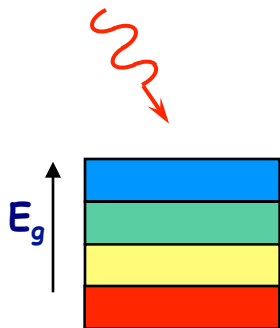
1. No absorption below gap:
photon wasted
2. Absorption to bottom of
conduction band: optimal
3. Absorption high into band:
excess energy to phonons heats cell

Optimization of gap:
max efficiency: 31%

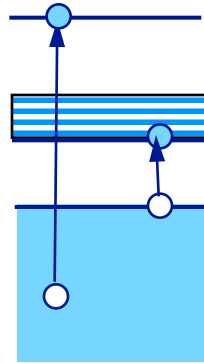
(Shockley Queisser 1961)

In real PV cells ~80% of incident
solar energy is lost!

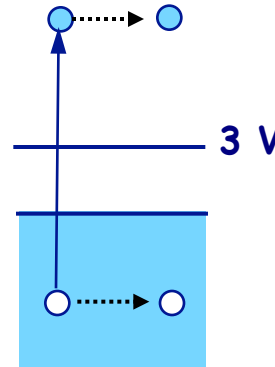
Examples of Innovative PV Designs



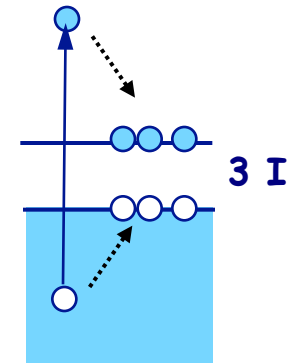
Multiple
junctions



Intermediate
Band absorbs
IR photons:
Boosts absorption
at low energies.
Max eff: 49%



Hot carriers



Multiple excitons
generated by high
energy photon:
Boosts absorption
at high energies.
Max eff: 44%

Measured efficiency increases
not close to theoretical maxima

Selection of Innovative PV Designs

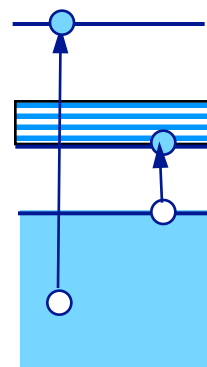
Efficiency of colloidal nanoparticle solar cells rapidly grew to 9.2% by 2014 from 4% a few years ago.

Organic PV(McGehee): 9%-2011, 12%-2014

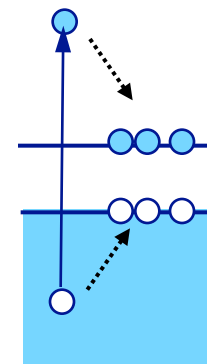
In the 17 years since its invention, IB was only tried in epitaxial solar cell structures, with limited success.

IB was never tried in colloidal NPs

CM can be enhanced by
(a) optimizing NP design, and
(b) implementing IB at the same time
to pursue CM-IB synergies



IB boosts
absorption at
low energies



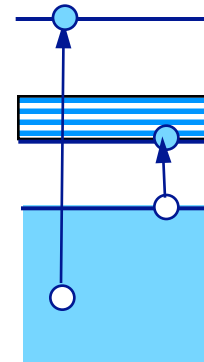
CM boosts
absorption at
high energies

The Full Spectrum Boost Project

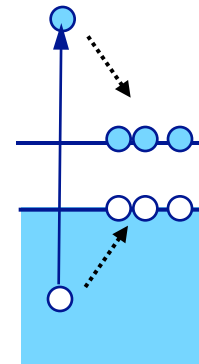
Focus on colloidal nanoparticle solar cells

Implement the Intermediate Band mechanism in colloidal NP solar cells

(a) Optimize NP design for CM
(b) Implement CM and IB to
boost absorption at low & high E

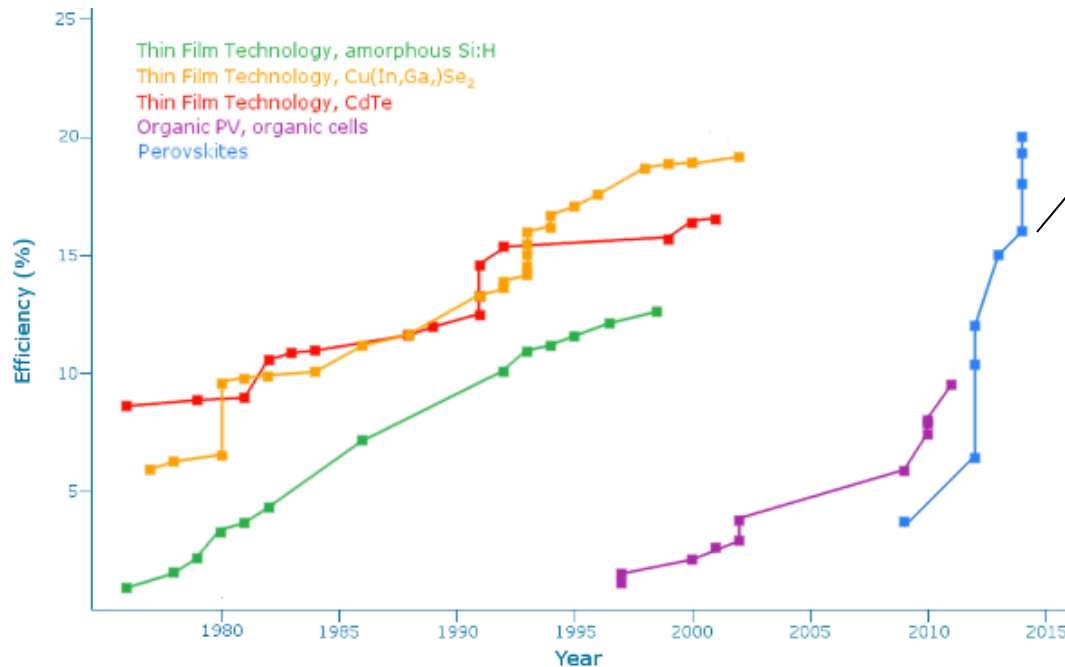
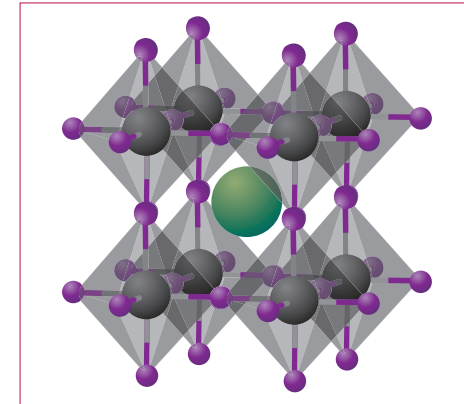
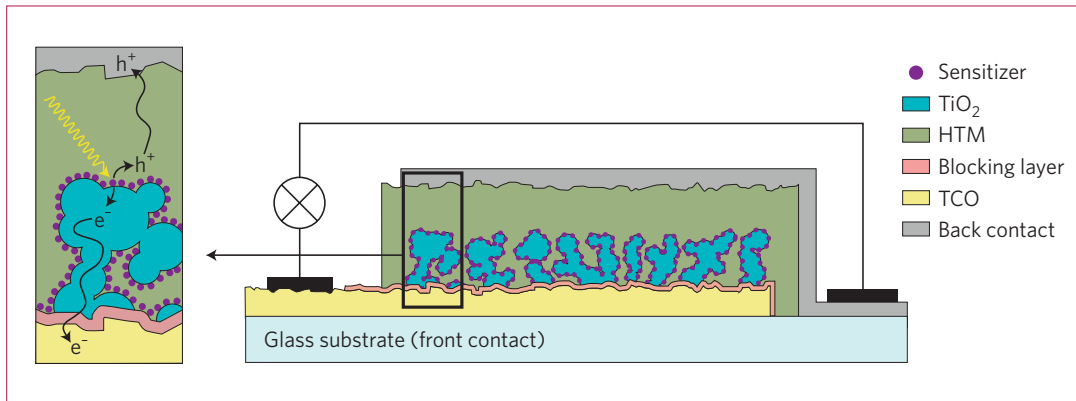


IB boosts absorption at low energies



CM boosts absorption at high energies

The Perovskite Revolution Started in Nanoparticle Solar Cells too



Perovskite: $\text{CH}_3\text{NH}_3\text{PbI}_3$

"High Tc-like" explosion

Simple, low temperature
solution-based fabrication

Lifetime ~ hours

Top cell for Si?

Full Spectrum Boost: Theory Infrastructure

Nanoparticle Structure: ab-initio-driven structural relaxation

One particle energies: DFT, GW, Quantum Espresso , PBE, PBE0

Transport:
Parameter & lifetime calculation

Optical absorption:
TDDFT

Band formation,
Lifetime for
Boltzmann
transport

Ab-initio compute
of E_{1p} , E_c , τ for
Marcus/Miller-A.
hopping transport

Intermediate
Band: VB/IB,
VB/CB rates

Carrier
Multiplication:
X→XX rate

Plan of the Talk

Carrier Multiplication Boost at high energies

Intermediate Band boost at low energies

Transport to extract photo-induced charge carriers

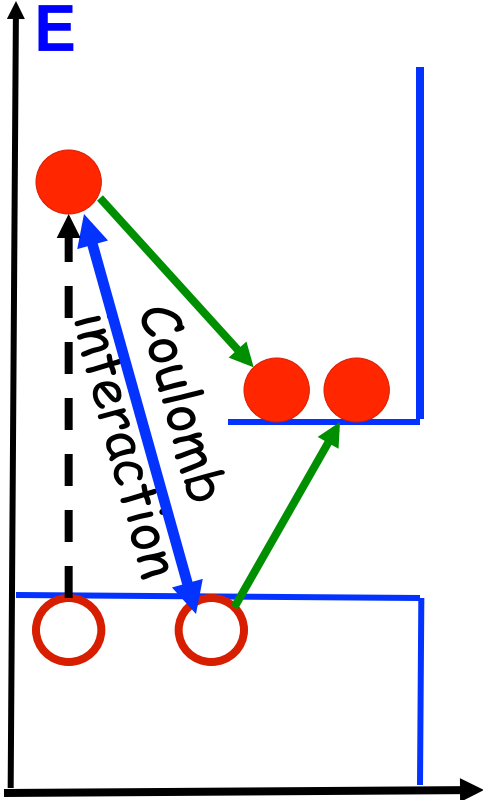
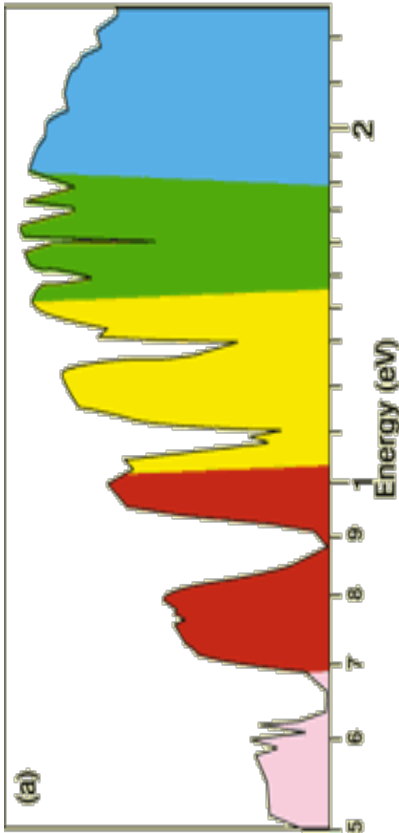
Plan of the Talk

Carrier Multiplication Boost at high energies

Intermediate Band boost at low energies

Transport to extract photo-induced charge carriers

Down-conversion by Carrier Multiplication



Keep energy of high energy photons in electronic sector:

Electron relaxation by Carrier Multiplication:

Photo-excited first exciton
relaxes by **exciting second
exciton** instead of phonons

Max efficiency:

44% 1 Sun (Klimov 2005)

70% 1000 Sun (Nozik 2013)

Carrier Multiplication - 1957

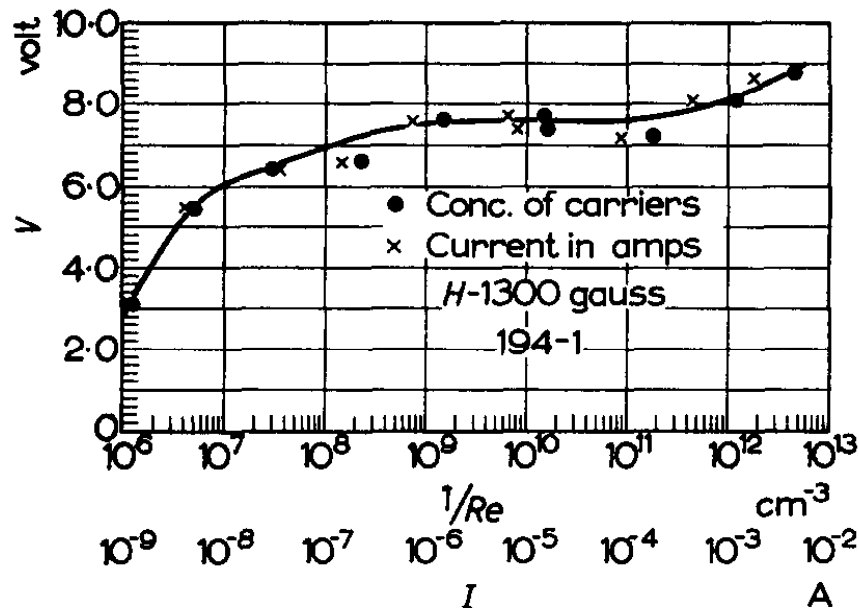
J. Phys. Chem. Solids. Pergamon Press 1957. Vol. 2. pp. 1-23.

IMPACT IONIZATION OF IMPURITIES IN GERMANIUM*

N. SCLAR† AND E. BURSTEIN

United States Naval Research Laboratory, Washington, D.C.

(Received 16 September 1956)



"Impact Ionization" (=CM)
has a 1% efficiency in bulk

Sclar (1957)

Carrier Multiplication

Save the exciton generation from jaws of electron-phonon interaction:

"We gonna need a bigger Coulomb interaction"



Carrier Multiplication

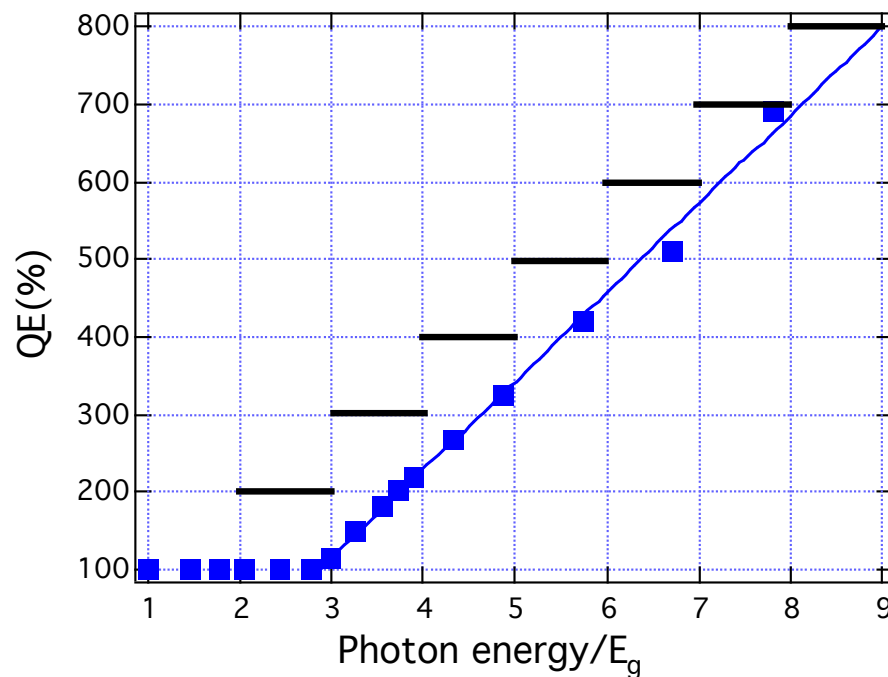
Save the exciton generation from jaws of electron-phonon interaction:

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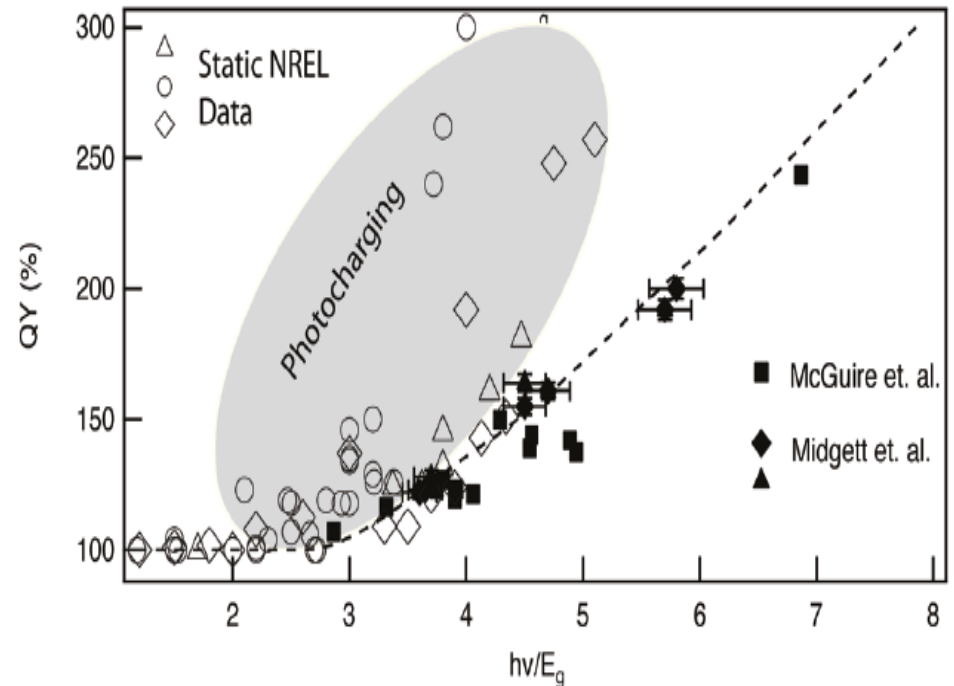


1. In **nanoparticles** electrons cannot avoid each other: screening is reduced, Coulomb interaction enhanced (Nozik 2001)
2. Use **Mott insulators**/perovskites! U large in bulk (Manousakis 2010)

CM in Nanoparticles: Discovery, Status



Klimov, Schaller (2004) quantum yield
(=#electrons/photon) up to 700%



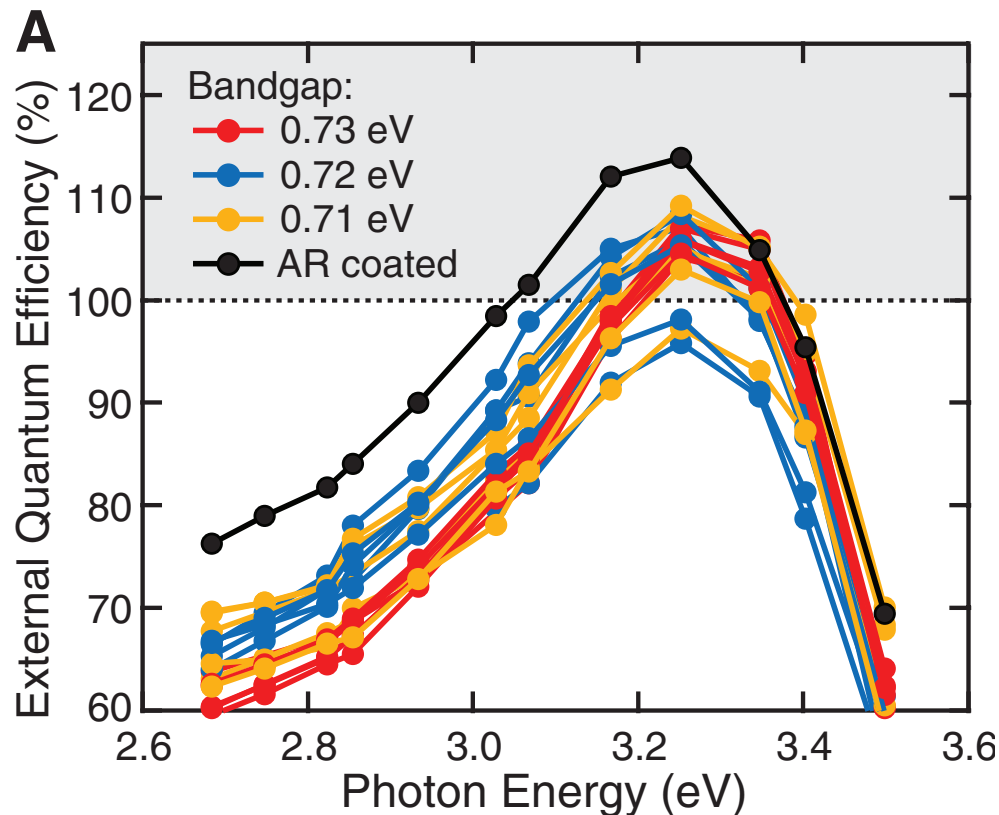
Beard (2011): CM present,
with lower efficiency

Nanoparticles in solution, not in solar cell

First working CM/MEG solar cell: Dec. 2011

Peak External Photocurrent Quantum Efficiency Exceeding 100% via MEG in a Quantum Dot Solar Cell

Octavi E. Semonin,^{1,2} Joseph M. Luther,¹ Sukgeun Choi,¹ Hsiang-Yu Chen,¹ Jianbo Gao,^{1,3} Arthur J. Nozik,^{1,4*} Matthew C. Beard^{1*}

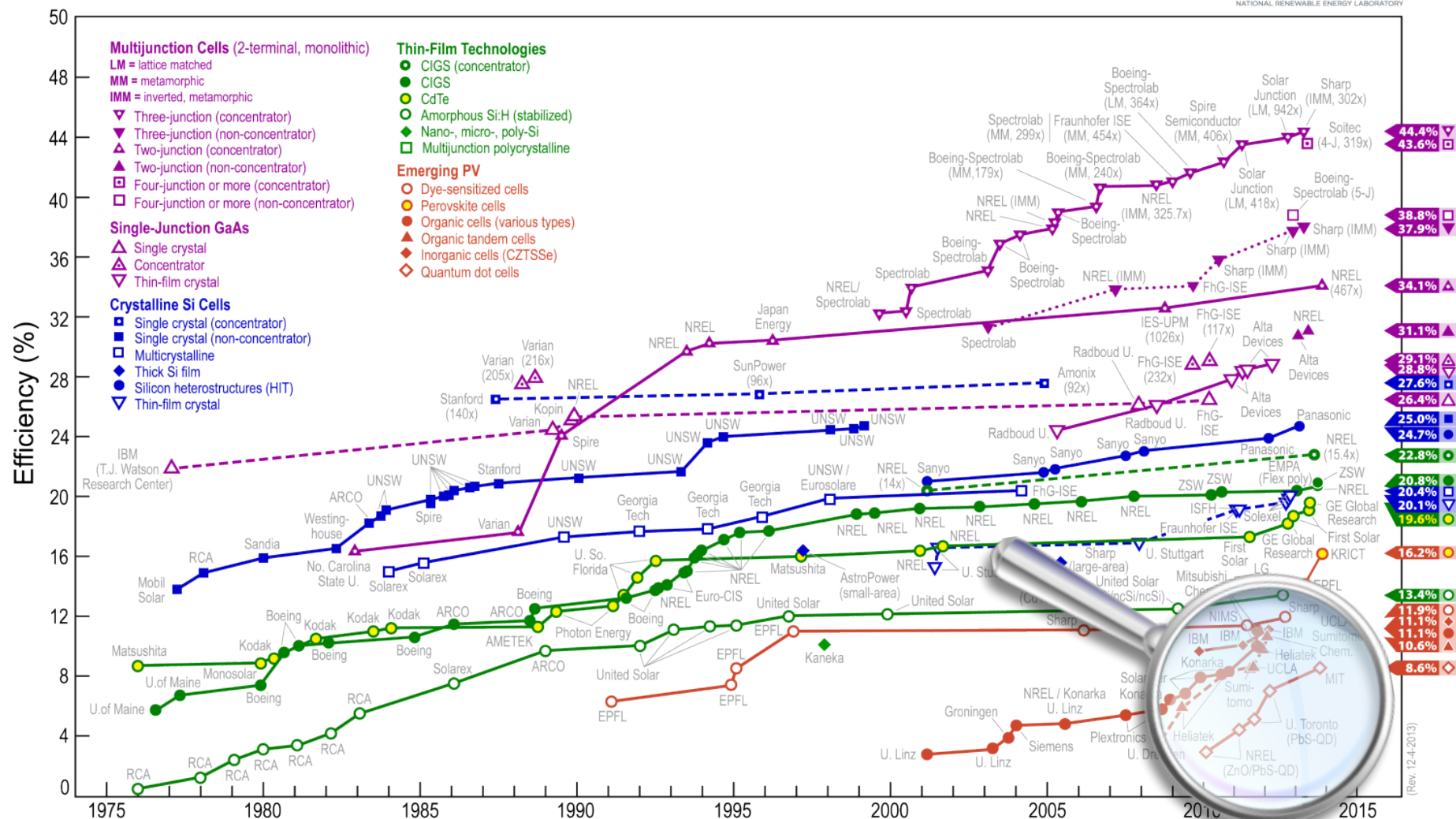


EQE>100%:

Proves presence of CM

Nanoparticle solar cells appeared on the NREL efficiency chart in 2010

Best Research-Cell Efficiencies

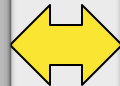


QCD - The Quantum Confinement Dilemma in Nanoparticle Solar Cells

Positives



Enhances Coulomb interaction:
Enhances CM

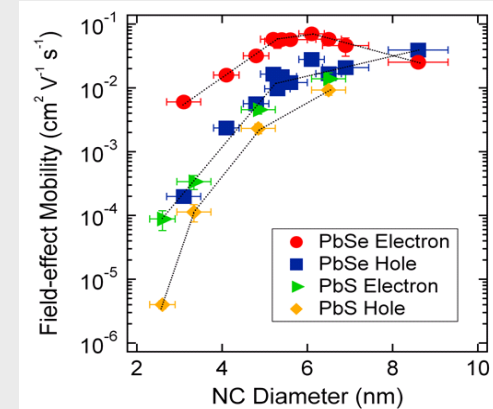
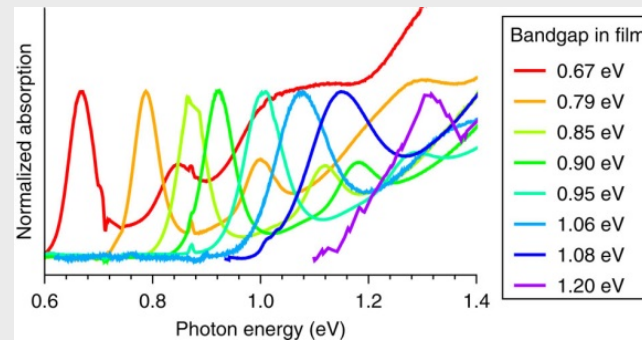
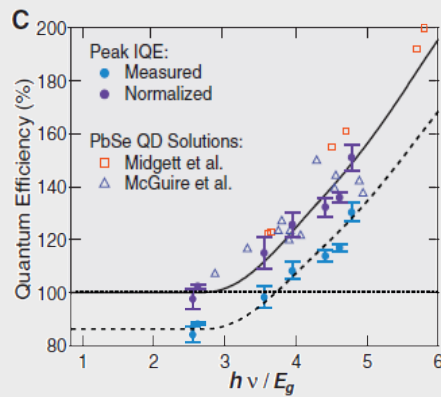


Negatives



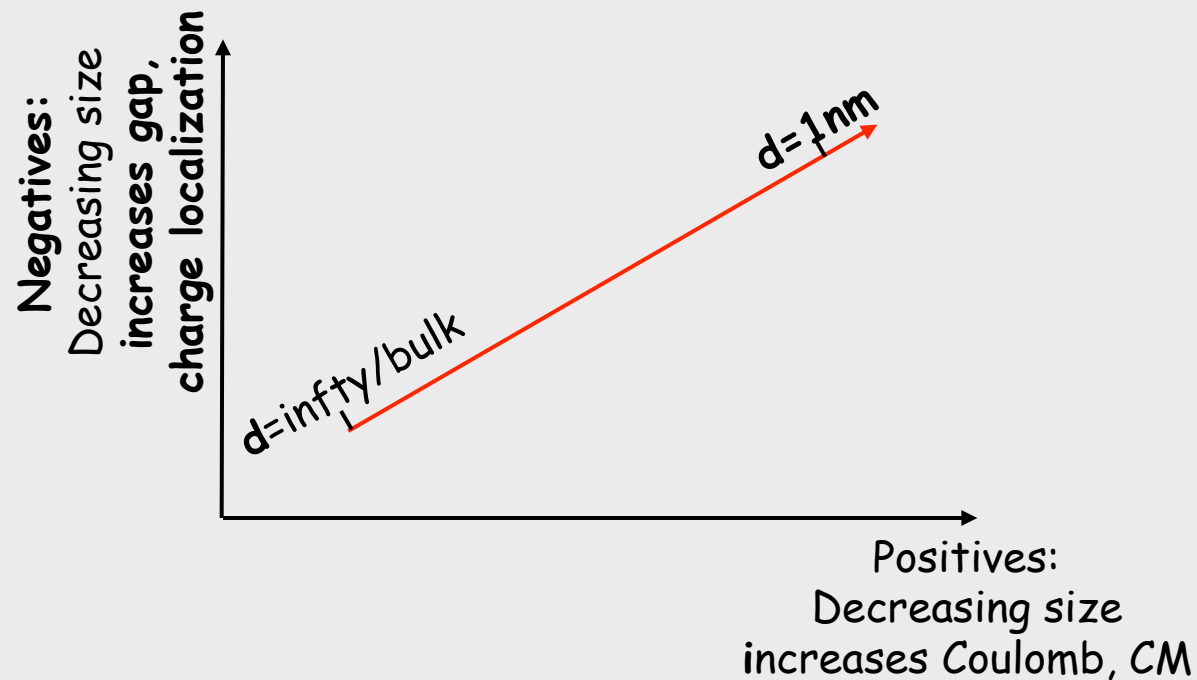
Widens gap:
Absorption is pushed out of solar spectrum

Localizes charges:
Hinders transport



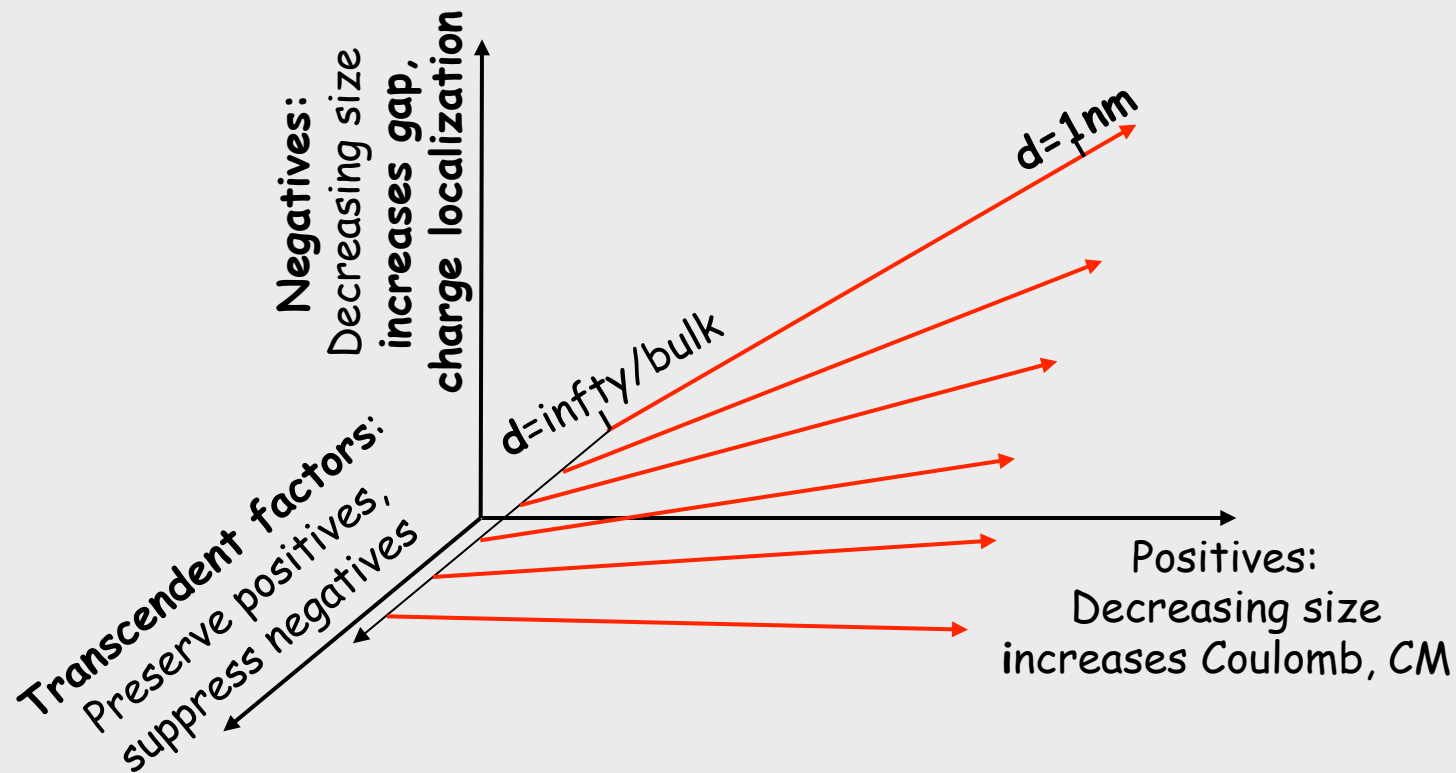
QCD - The Quantum Confinement Dilemma in Nanoparticle Solar Cells

Decreasing size enhances CM but introduces negatives



Transcending QCD in Nanoparticle Solar Cells

Transcendent factors:
Preserve positives, suppress negatives

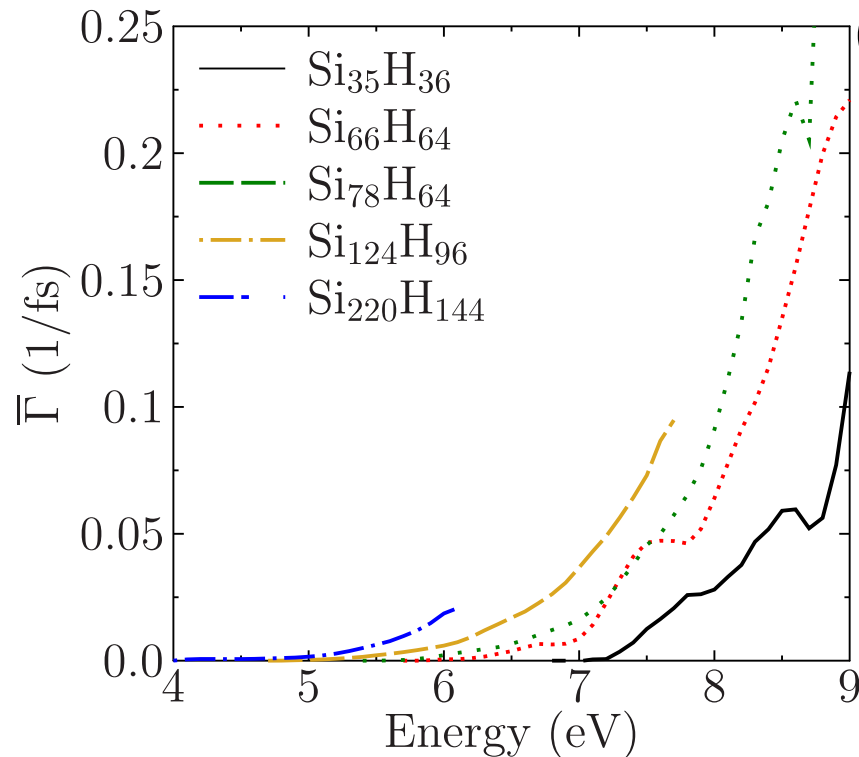


Transcending QCD in Nanoparticle Solar Cells

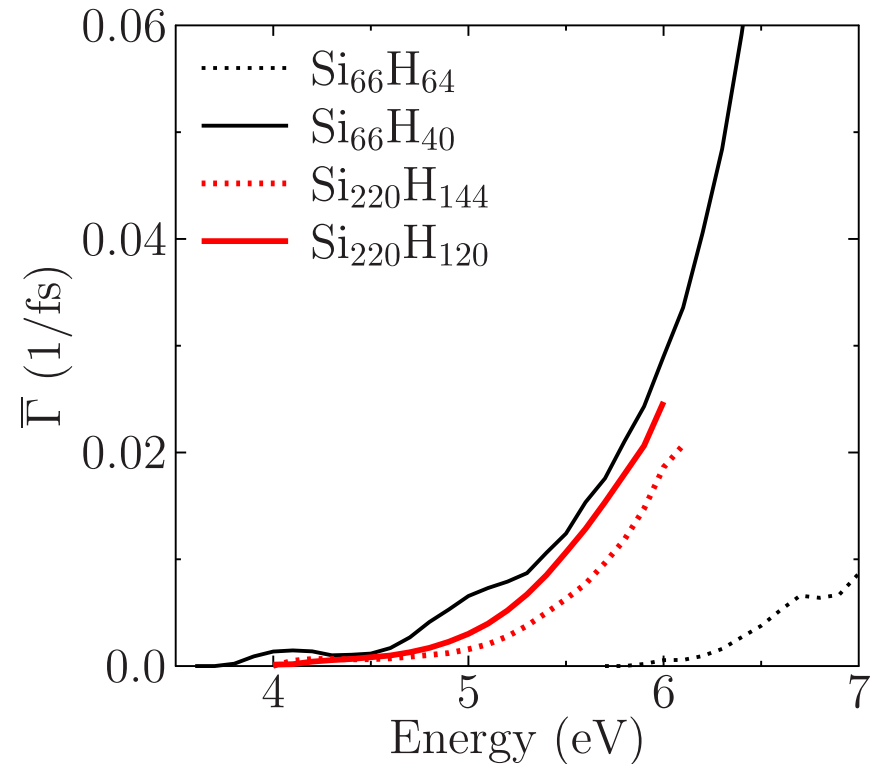
Transcendent factors:
preserve positives, suppress negatives

1. Surface reconstruction of nanoparticles
2. Shape engineering of nanoparticles: from dots to rods
3. Exotic core phase nanoparticles
4. Charge separation, transport and extraction

Reconstruction Compensates Gap-Enhancement without Reducing Coulomb Strength/CM



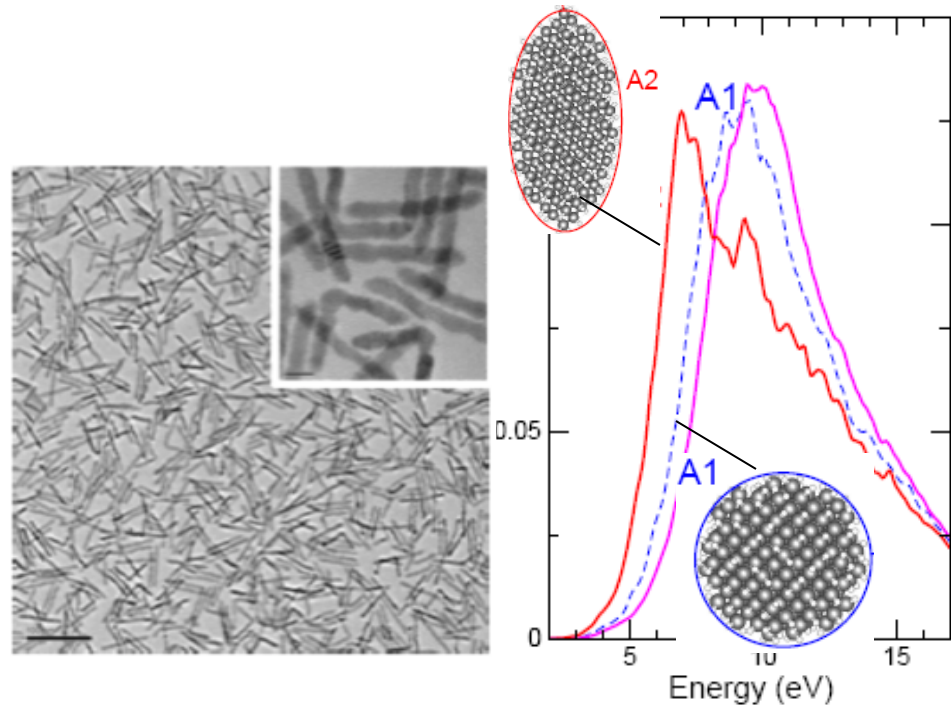
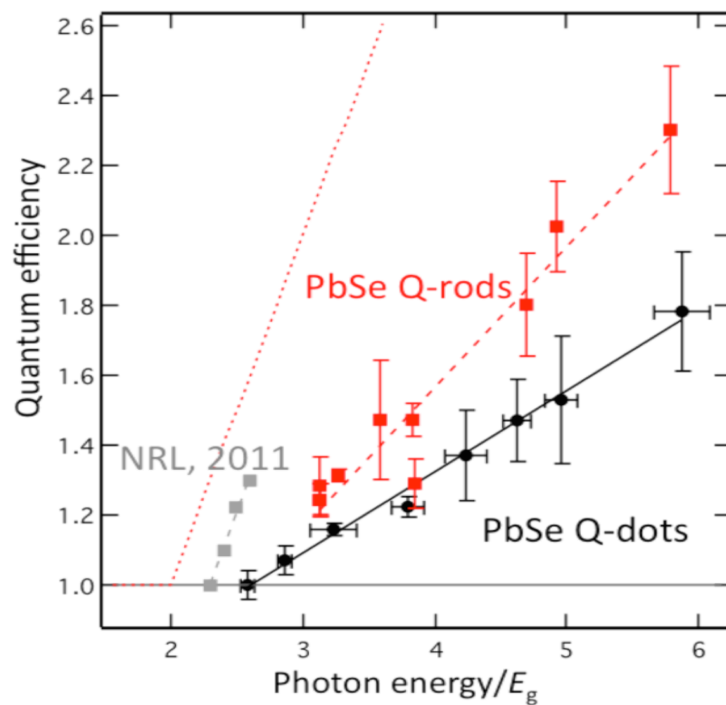
Quantum confinement enhances the gap in unreconstructed NPs



Reconstruction

- compensates gap enhancement
- preserves enhanced Coulomb/CM

2. Lowered Symmetry: Gap Reduction, More Allowed Transitions



Many transitions forbidden by symmetry-driven selection rules
Lowering symmetry of nanoparticles allows more transitions:

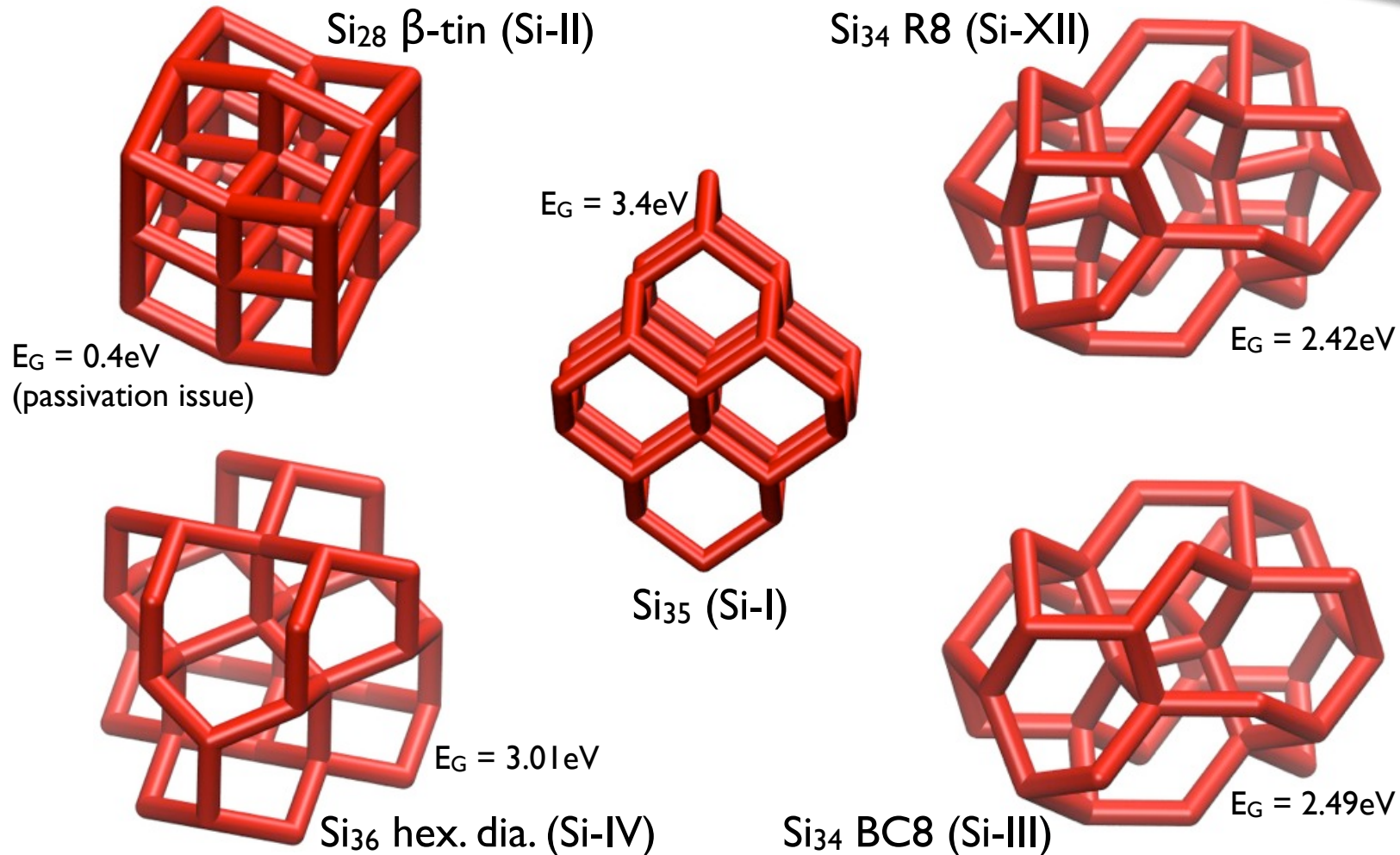
Nanorods: lower CM onset energy; enhanced CM at higher energy

Nanowires: Cui group

Gali, Kaxiras, Zimanyi, Meng, Phys. Rev. B 2010 25

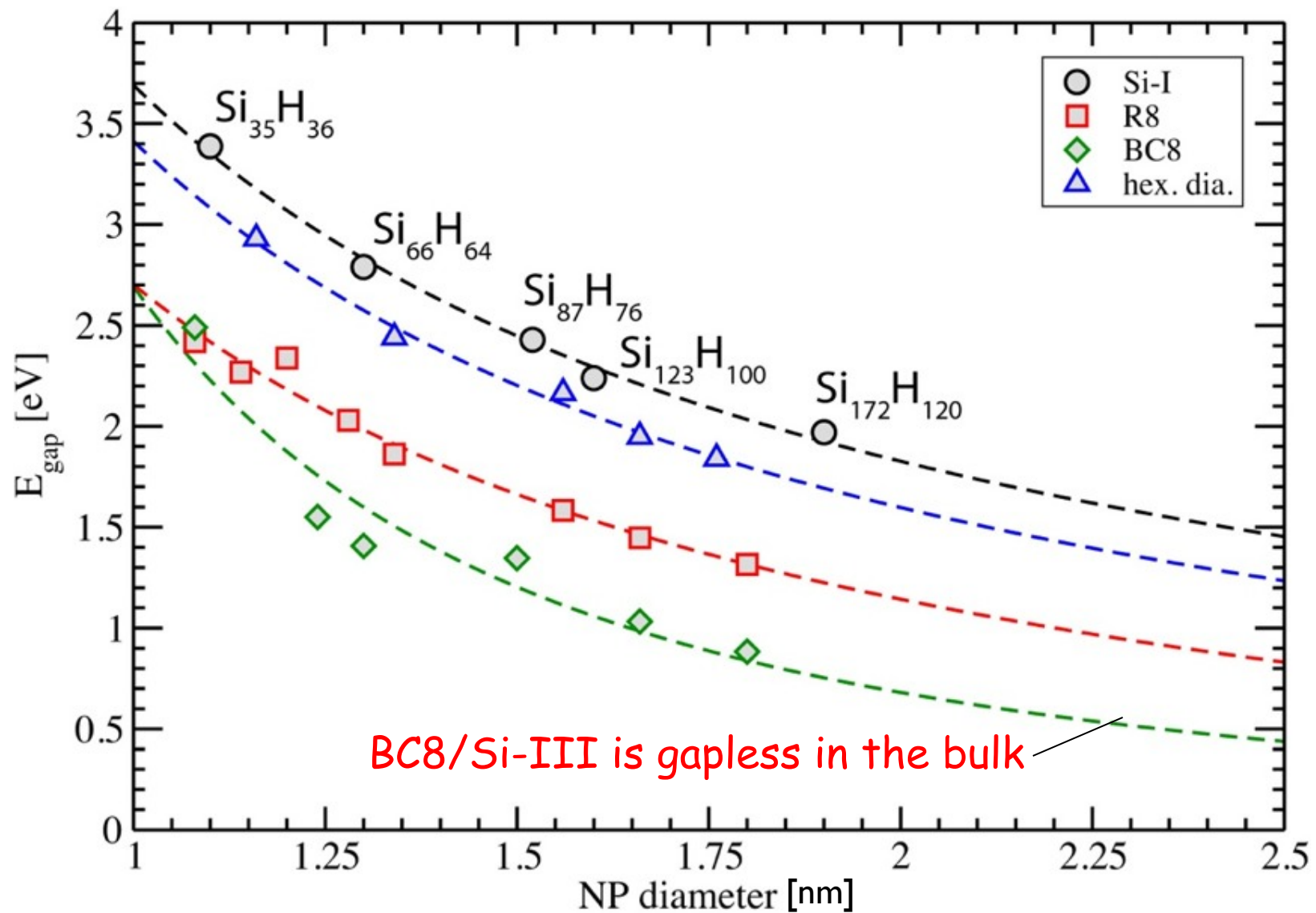
3. Exotic Core Phase Si/Ge NPs:

3.1. Reduce Gap by using Bulk-Gapless Phases

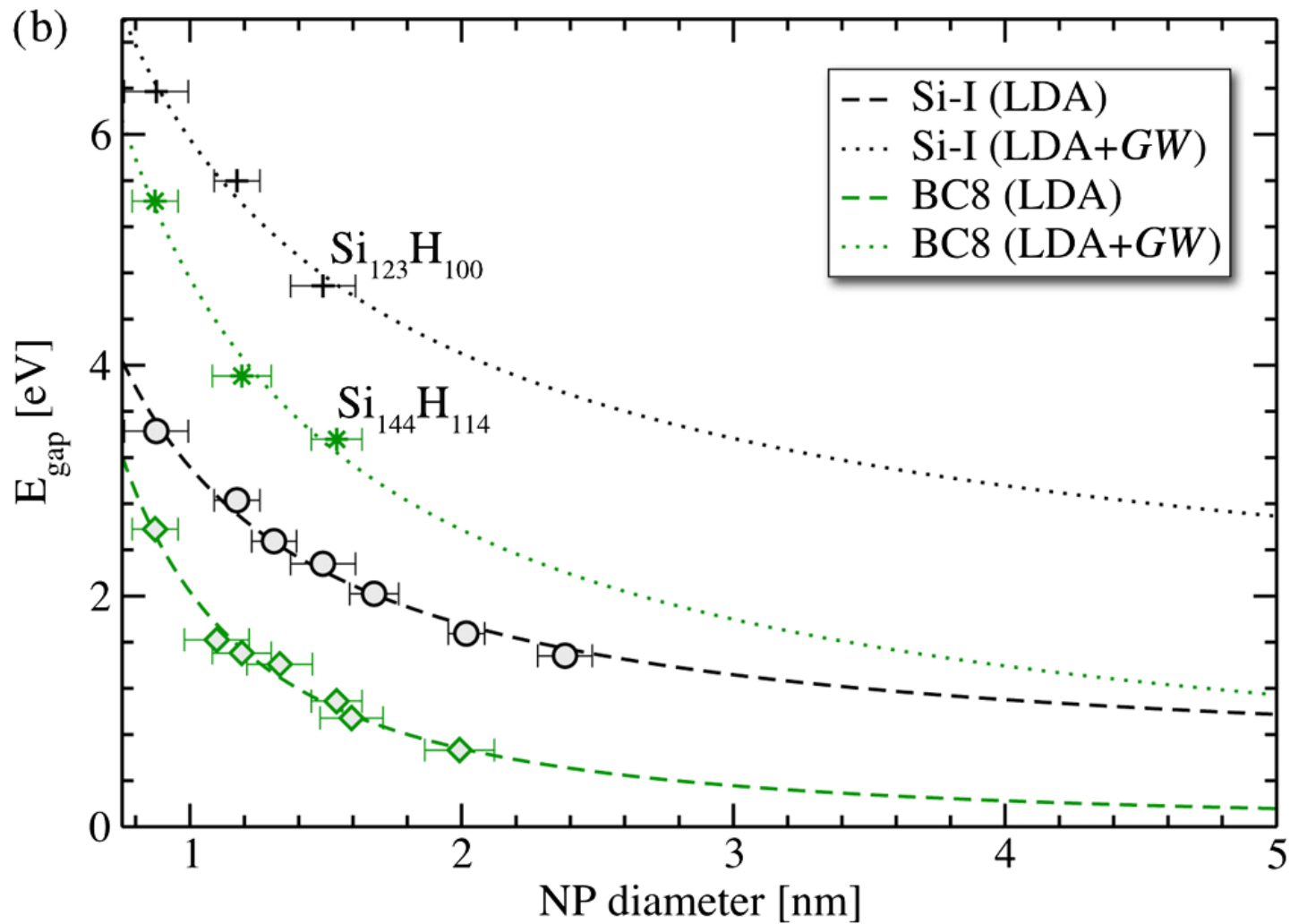


Wippermann, Voros, Gali, Rocca, Zimanyi, Galli Phys. Rev. Lett. **110**, 046804 (2013)

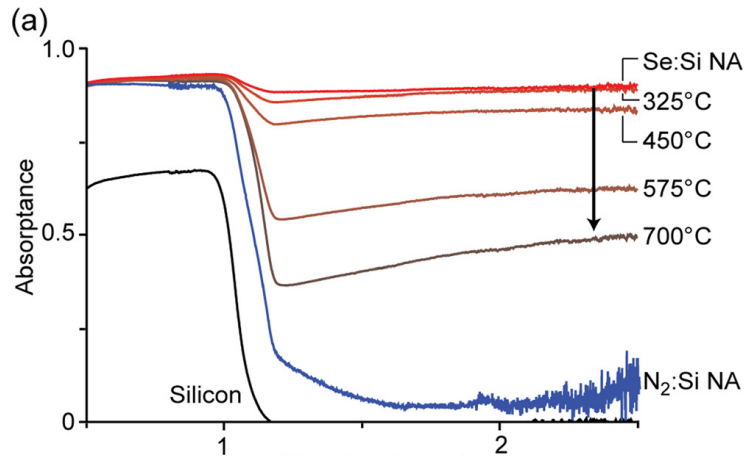
3.1. Gap reduction in BC8/Si-III



3.1. Comparison of LDA and GW



3.2. High Pressure Polymorphs in Black Si

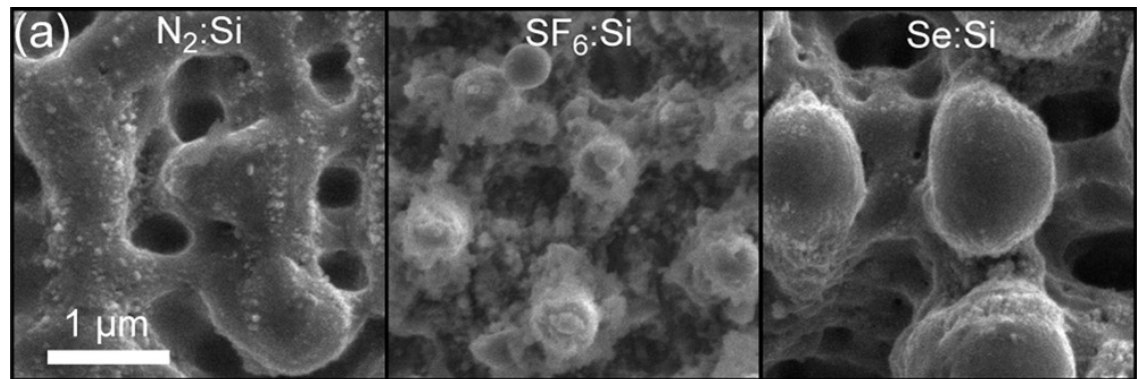
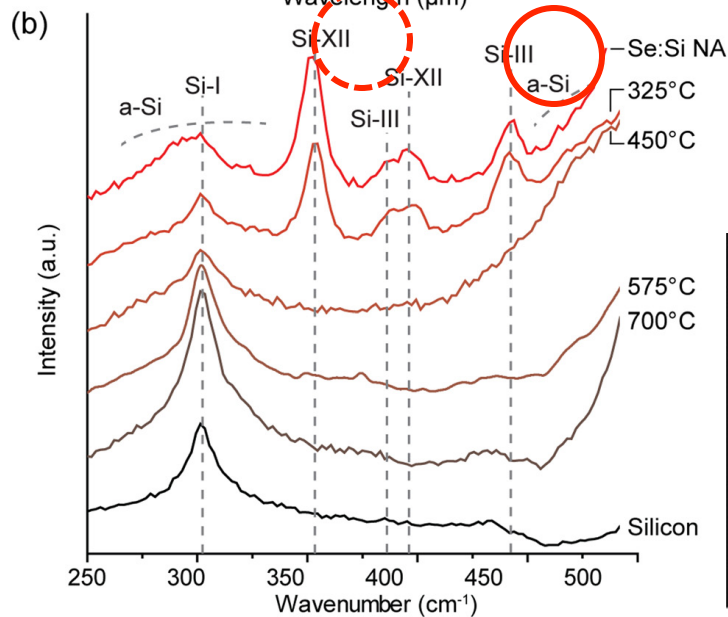


1. Top layer of PV cell transformed by high energy laser pulses (Mazur 2013)

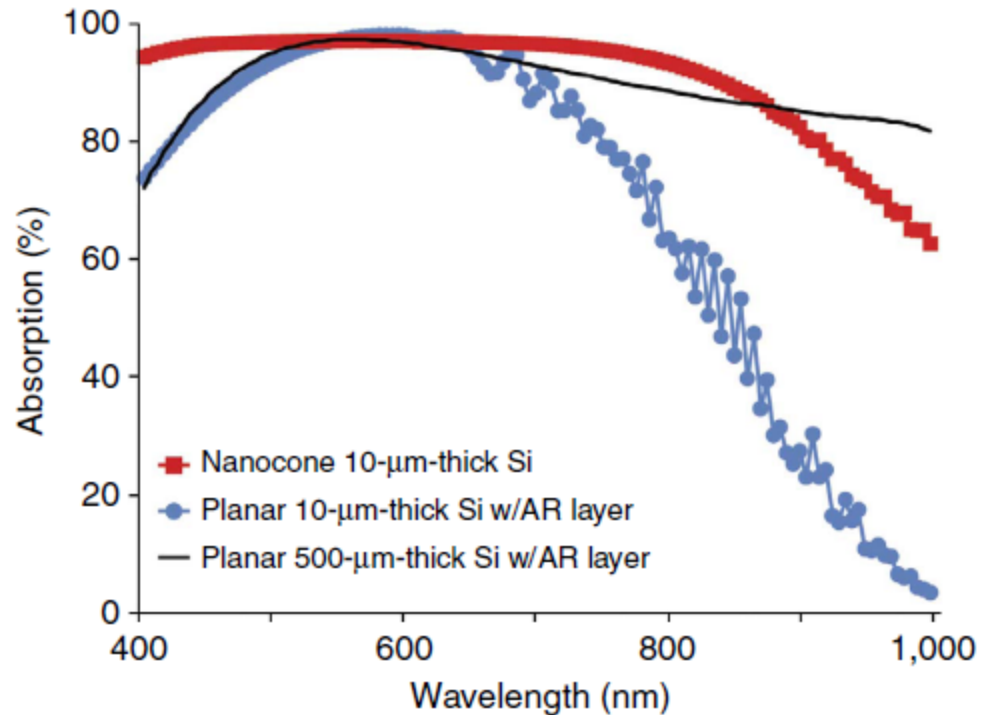
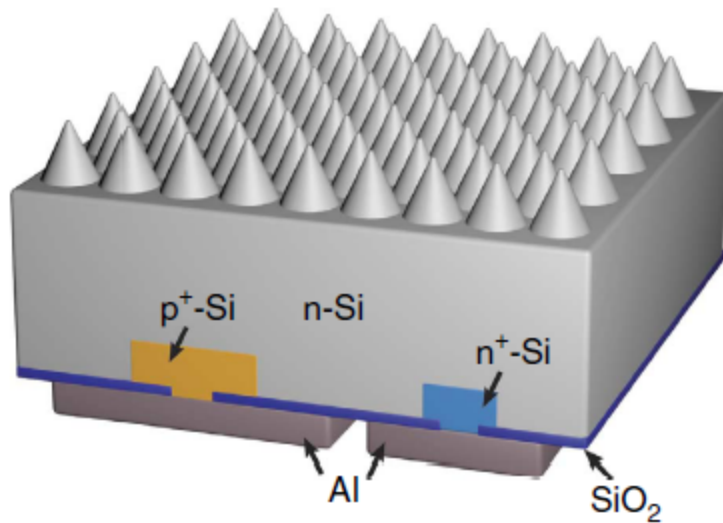
2. Observed large enhancement of sub-gap absorption

3. Observed the formation of BC8/Si-III phase by Raman scattering

4. When BC8/Si-III phase was annealed away, sub-gap absorption greatly reduced



Using nanocones to enable complete light absorption in thin Si

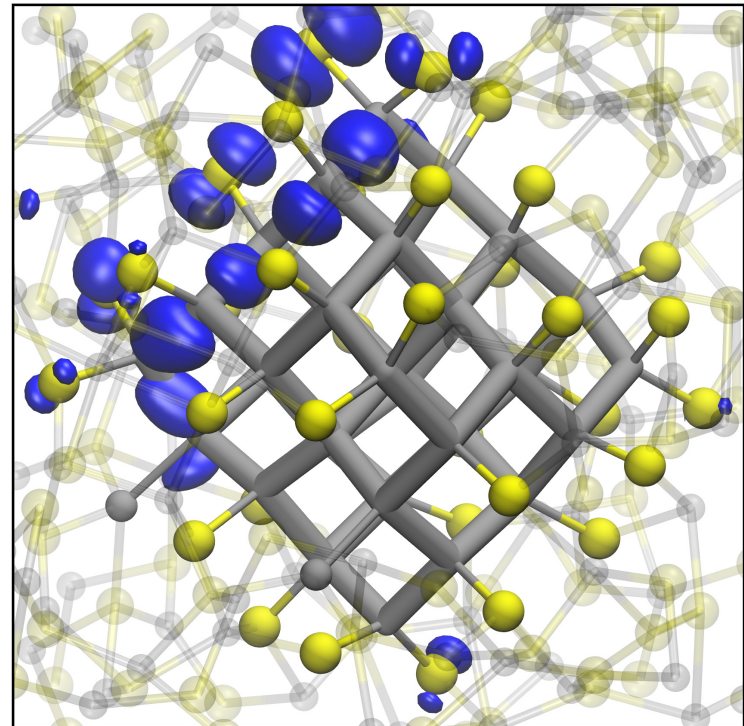


Sangmoo Jeung, Mike McGehee, Yi Cui, *Nature Comm.*

4. Charge Separation and Extraction:

4.1. Si NP in ZnS

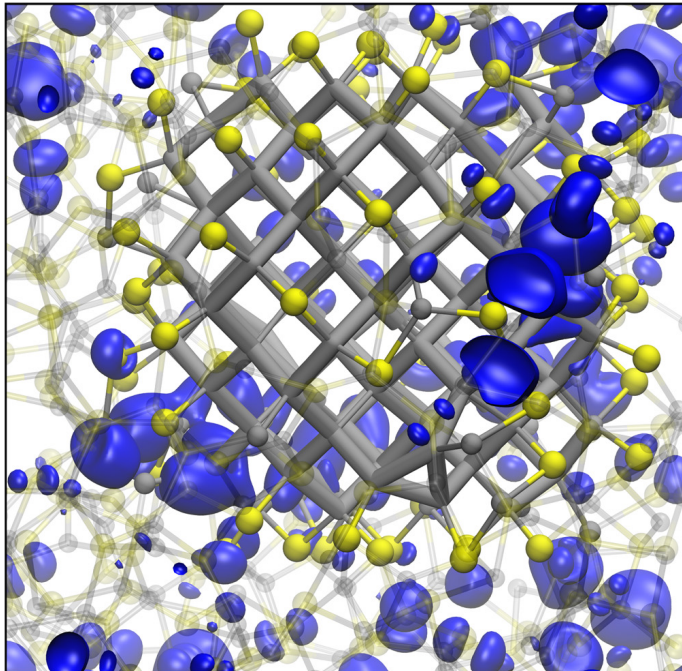
1. Create ZnS matrix with 512 atoms
2. Replace 35-172 Zn/S atoms with Si atoms
3. Relax structure with Qbox package
T(anneal) upto 1,000K
4. Calculate energy



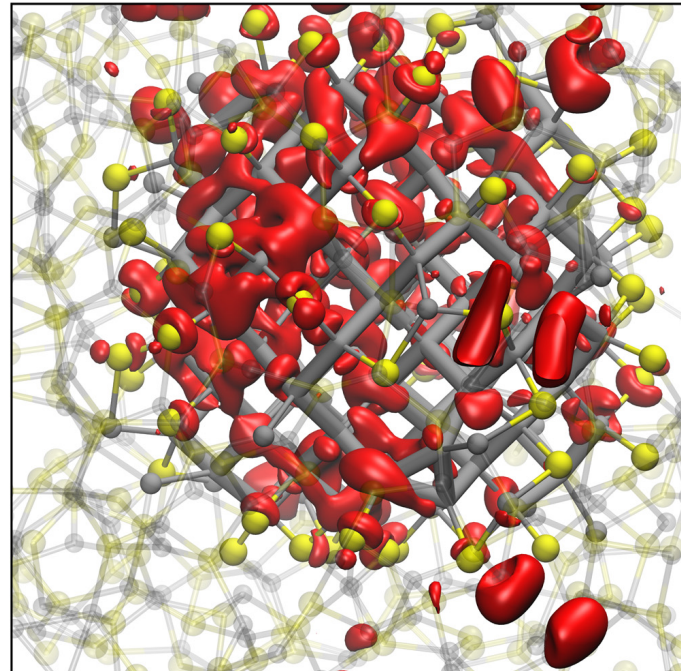
Cover of PRL, March 14, 2014

4.2. Complementary Charge Transport Channels

Top of Valence Band



Bottom of Conduction Band

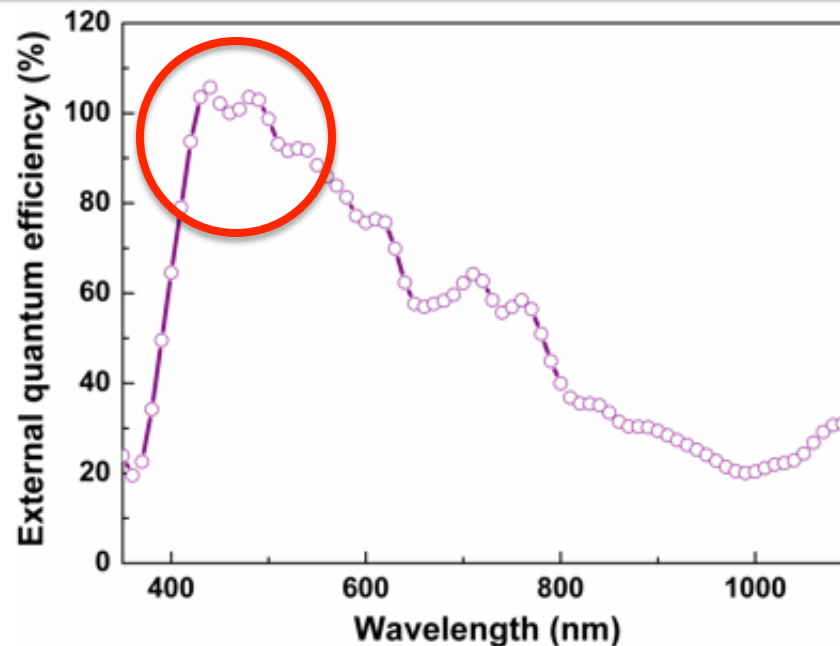
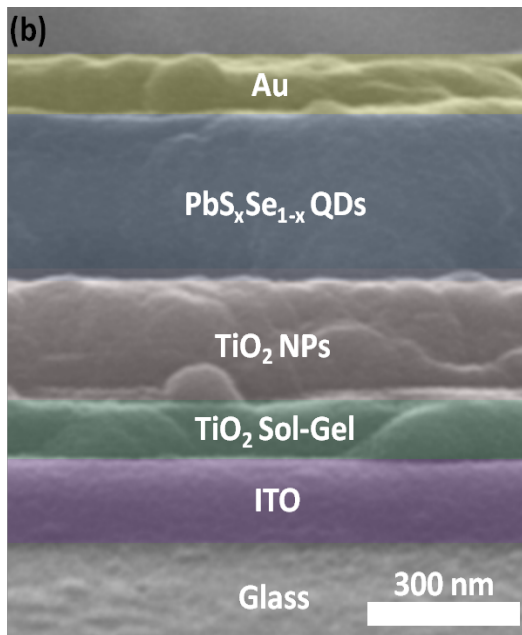
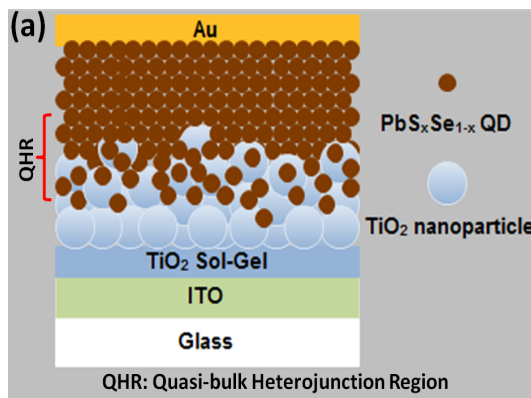


Electron transport: NP-NP transition

Hole transport: in host matrix

Complementary charge transport channels -
recombination reduced

Demonstration of Carrier Multiplication in a Functioning Solar Cell



Beard & Nozik
(2011):
CM in working
solar cell.
Used hydrazine:
combustible

Carter lab: EQE>100% in working solar cell

Optimized cell performance by varying the composition PbS_xSe_{1-x}.

Carrier Multiplication Summary

Carrier Multiplication is a promising solar paradigm

Quantum Confinement Dilemma: QC enhances Coulomb/CM, but enhances the gap and makes charge extraction harder

Transcending QCD possible:

1. Surface reconstruction of NPs: decreases gap, preserves MEG

2. Shape engineering of NPs (from dots to rods): decreases gap, increases number of allowed transitions

3. Exotic core phase NPs: decrease gap, increase Coulomb/CM

4. Embedding NPs in host matrix: interface changes type I -> type II: complementary charge transport channels form, reduce recombination

Plan of the Talk

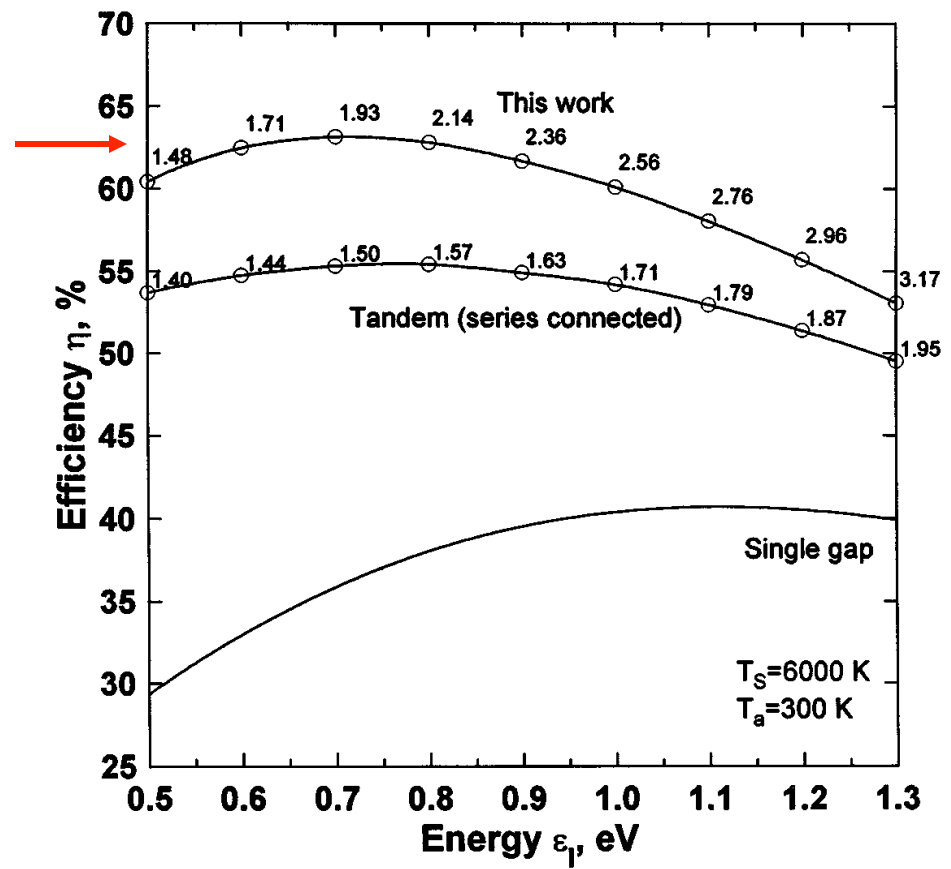
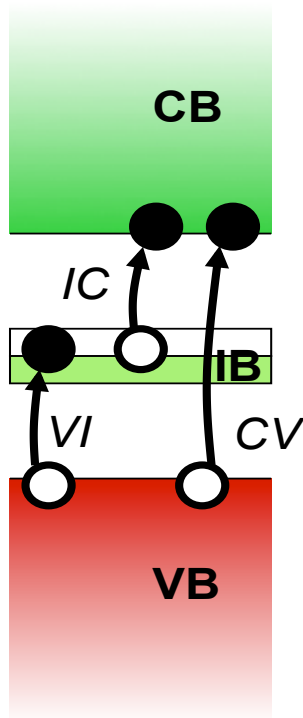
Carrier Multiplication Boost at high energies

Intermediate Band boost at low energies

Transport to extract photo-induced charge carriers

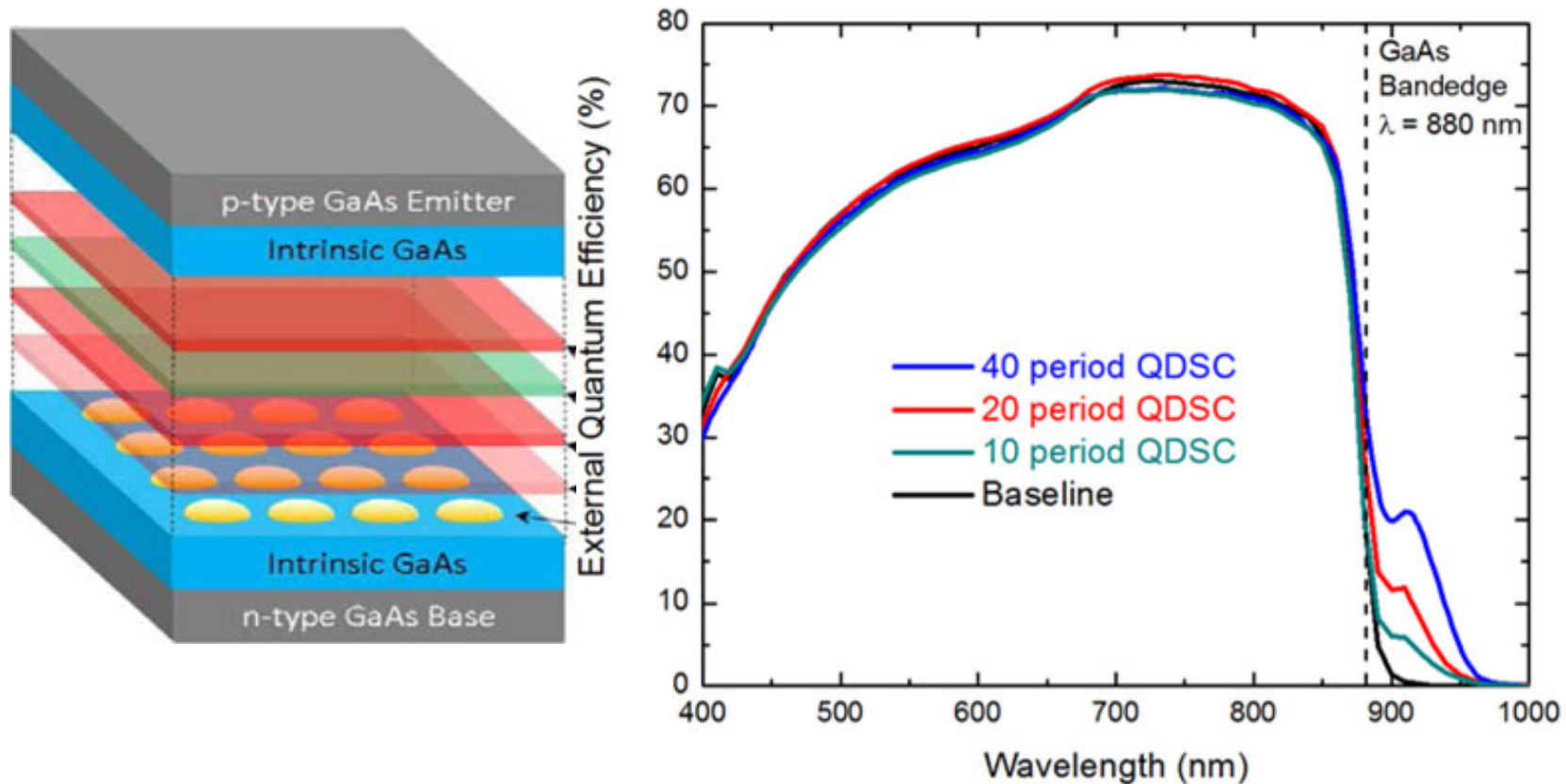
Up-conversion with Intermediate Band Solar Cells

1. Absorb photon with sub-gap energy: electron $IB \rightarrow CB$ & $VB \rightarrow IB$
2. Fill IB by chemical doping or by photo-doping



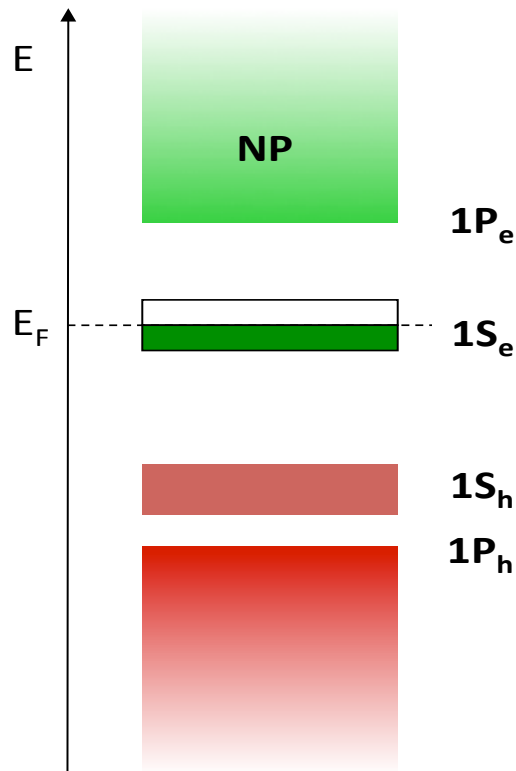
Up-conversion: Dionne group

Intermediate Band: Epitaxial Design



- (1) Process steps increase from ~10 to 50-100
- (2) Efficiency increase minimal

Intermediate Band: Colloidal Nanoparticle Design



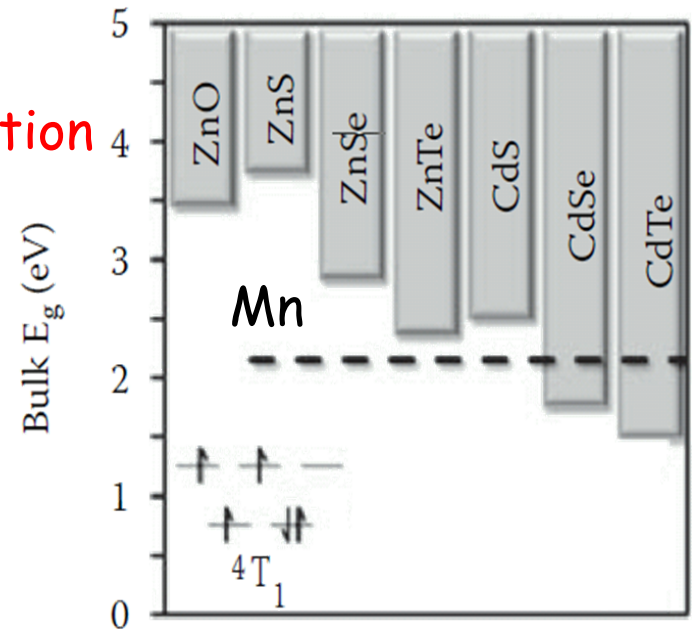
Core-shell NPs

Structural reconstruction

Quantum confinement

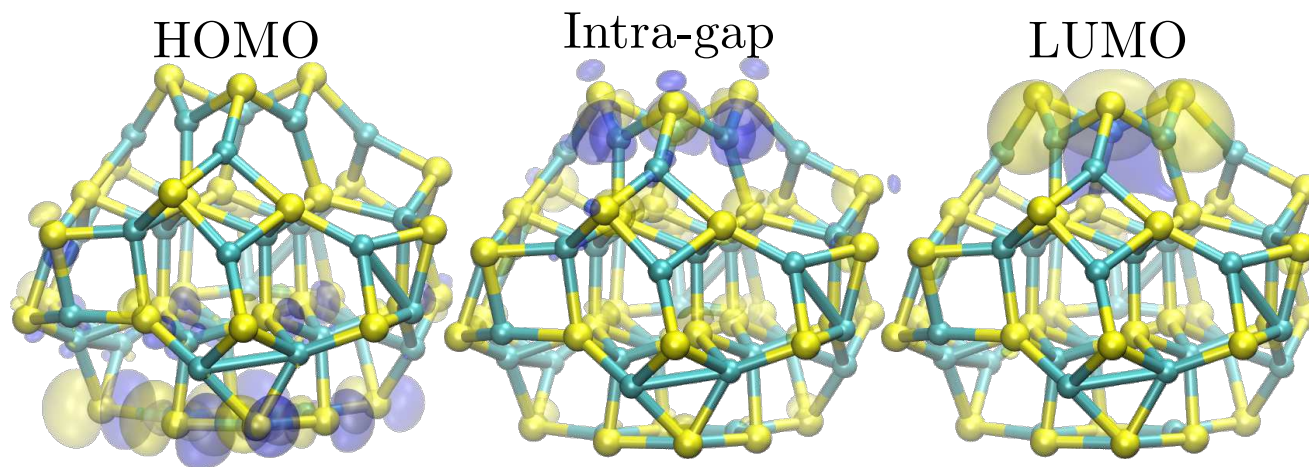
Surface doping

Core doping



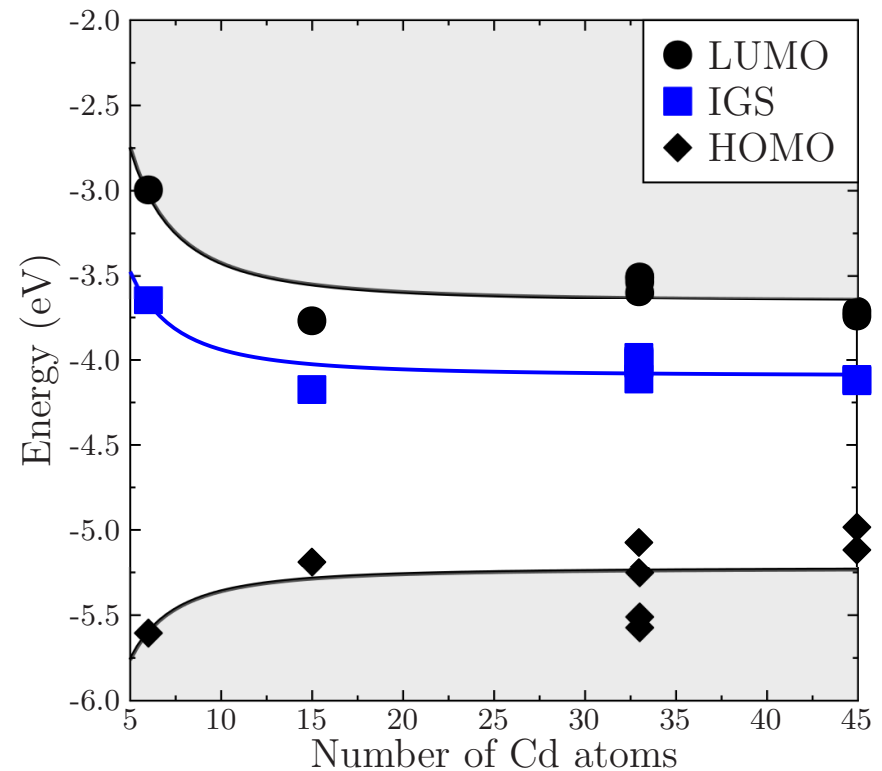
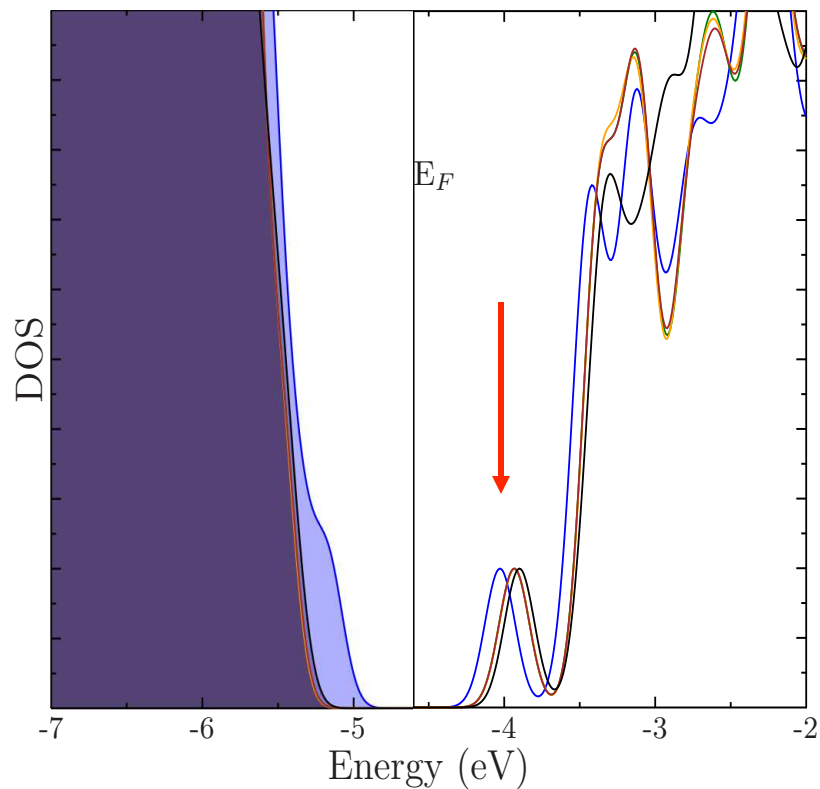
Intermediate Band from NP Surface Relaxation

$\text{Cd}_{33}\text{Se}_{33}$ NP



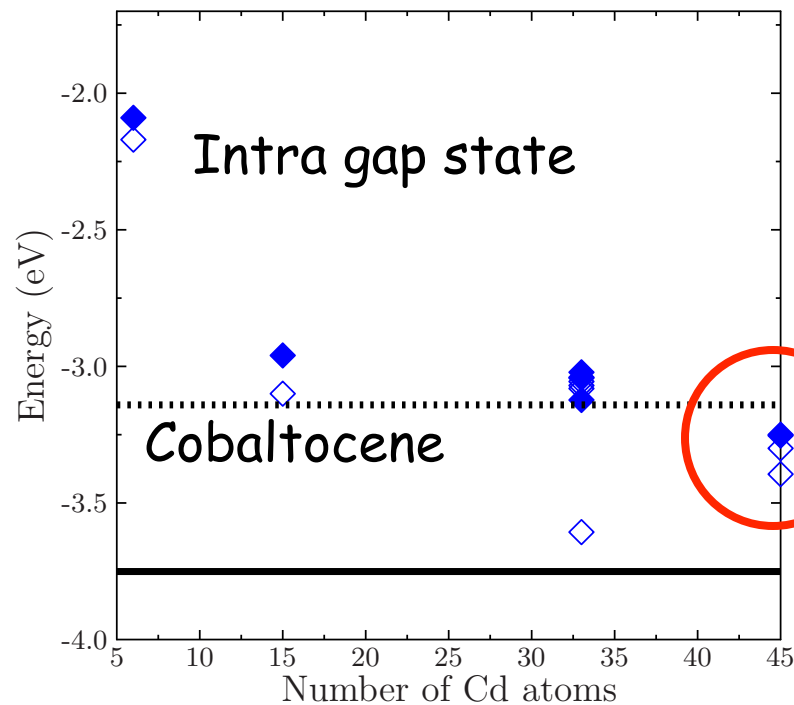
Intra-gap State from NP Surface Relaxation

Cd₃₃Se₃₃ NP: An intra-gap state is formed by NP relaxation

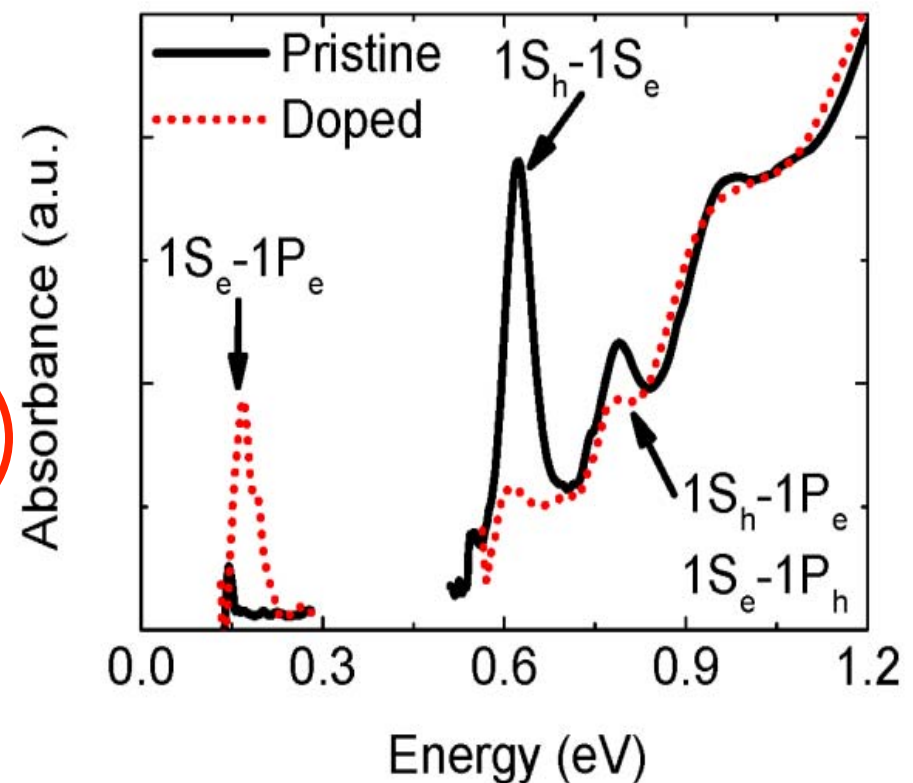


Intra-gap State Filling by Chemical Doping

Intra-gap state filled by cobaltocene doping



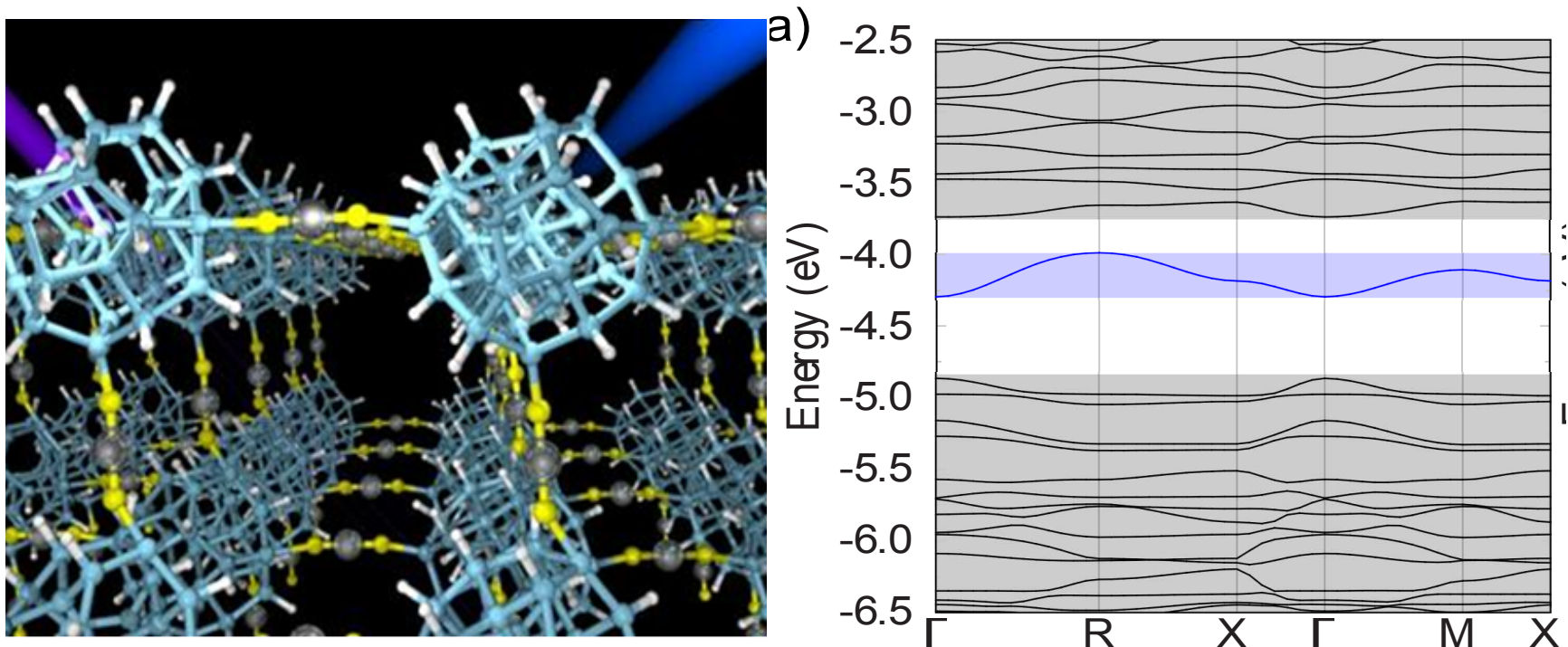
Voros, Galli, GTZ 2014



Klimov 2014

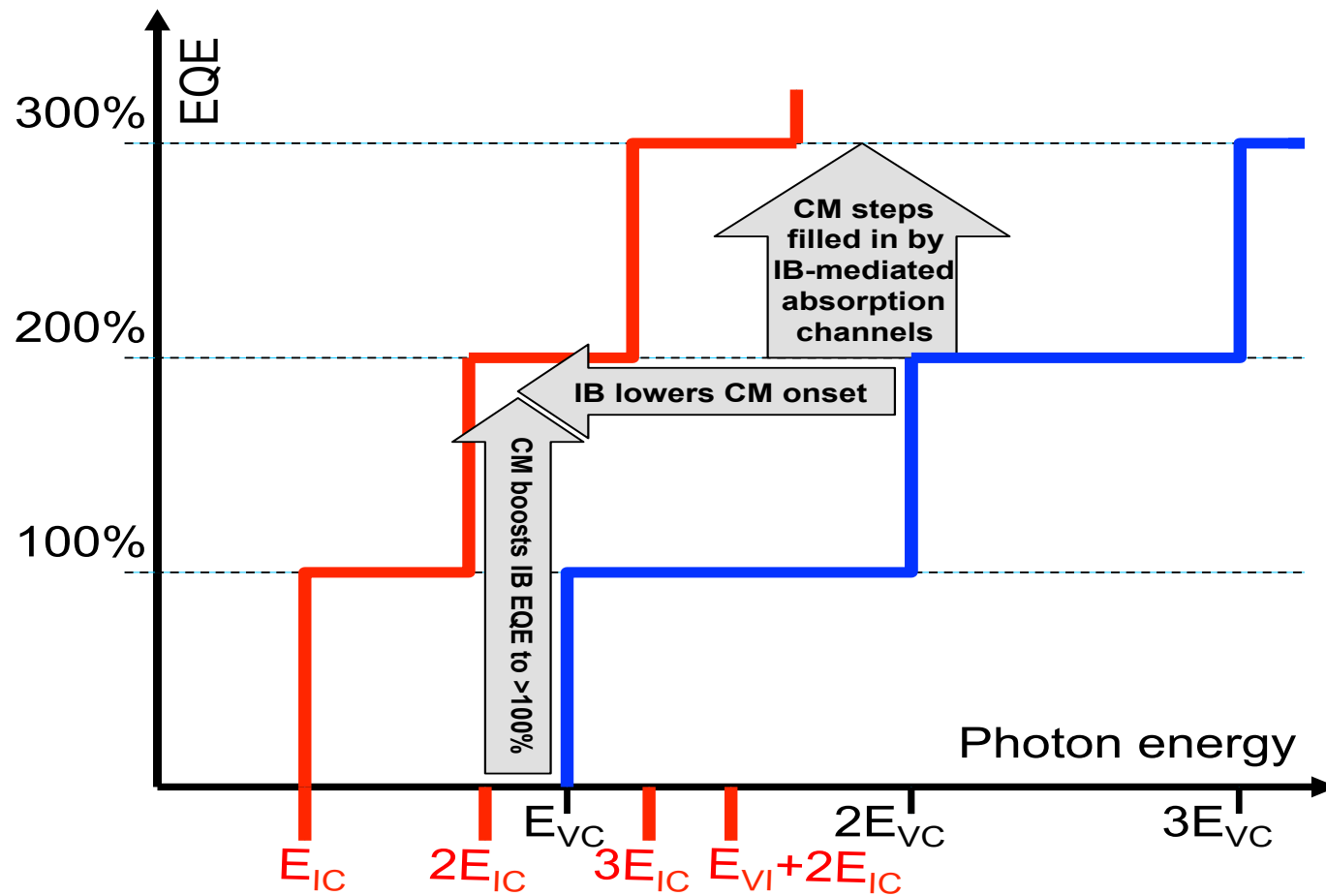
Intermediate Band Formed in NP Array

Intra-Gap states combine into Intermediate Band in Simple Cubic nanoparticle array



Voros, Galli, GTZ 2014

Synergy between Intermediate Band absorption and Carrier Multiplication



Theoretical maximum: 55% at one-sun, 72% at full concentration

Intermediate Band Summary

IB is the most promising paradigm to boost sub-gap absorption

Epitaxial implementation yet to fulfill its promise

Proposed to use Colloidal Nanoparticles to implement IB

Several designs to form intra-gap states

Proof of Concept: Intra-gap state by NP relaxation

Chemical doping of intra-gap state by cobaltocene

Demonstrated formation of intermediate band in NP arrays

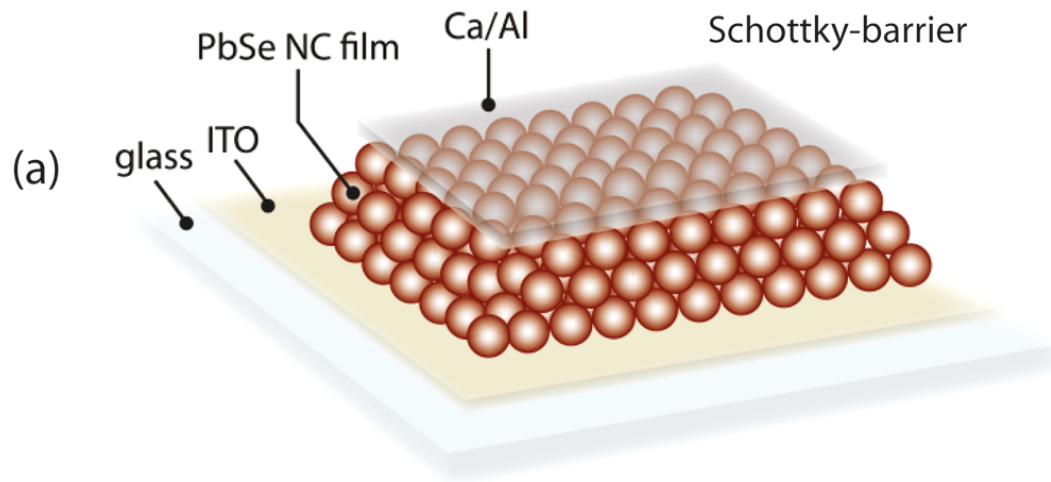
Plan of the Talk

Carrier Multiplication Boost at high energies

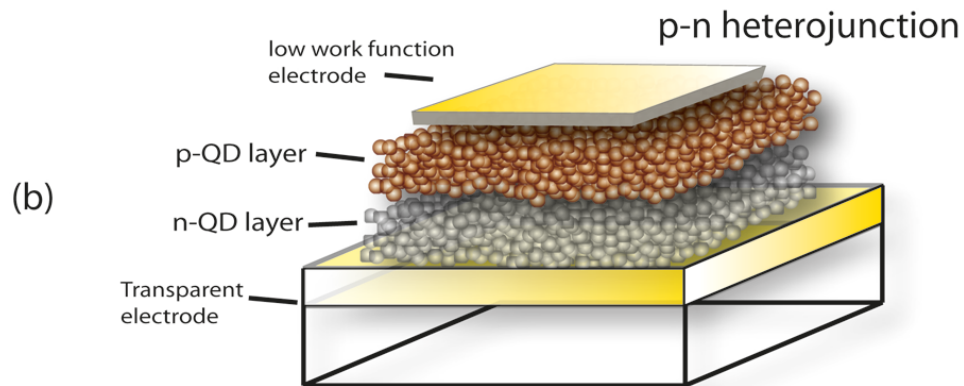
Intermediate Band boost at low energies

Transport to extract photo-induced charge carriers

Transport in Nanoparticle Solar Cells

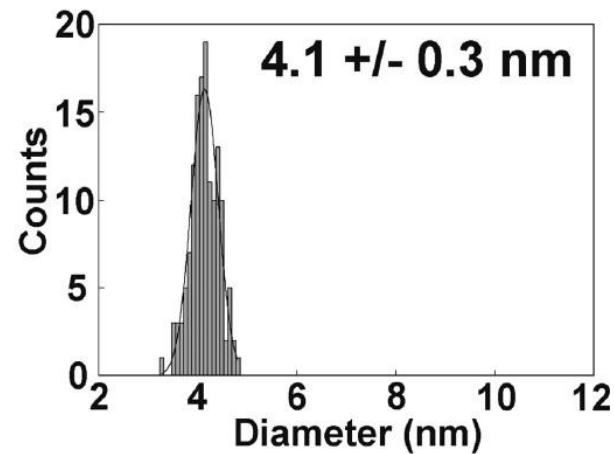
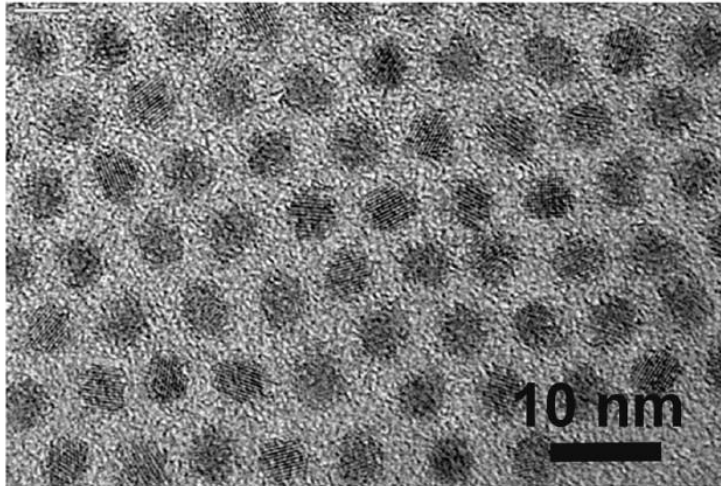


Built-in field generated by difference of electrode work functions

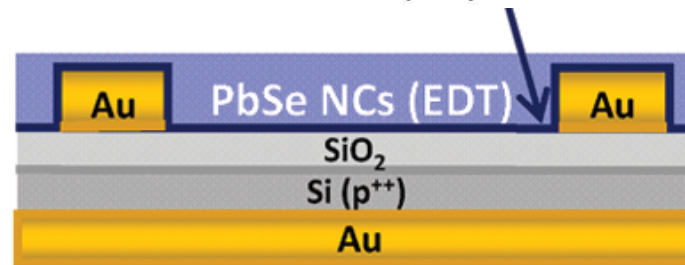
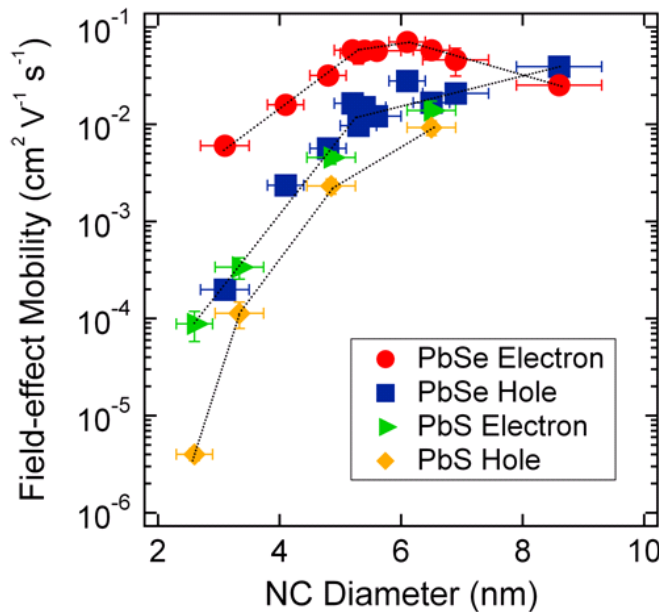


Built-in field generated by forming p- and n-doped nanoparticle layers

FET mobility in PbS and PbSe Nanoparticle films



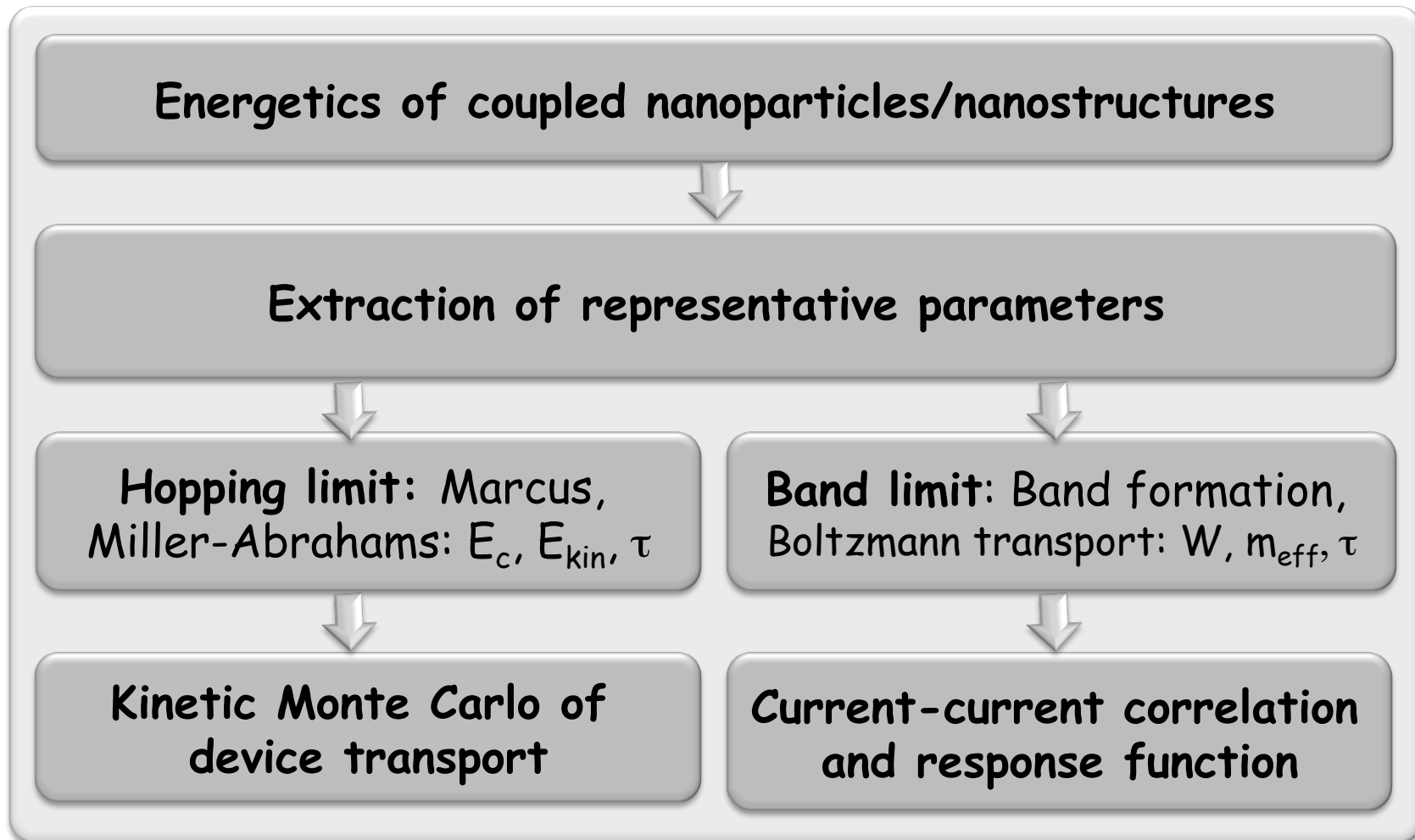
M. Law (2010)



Mobility(diameter D): rise->maximum

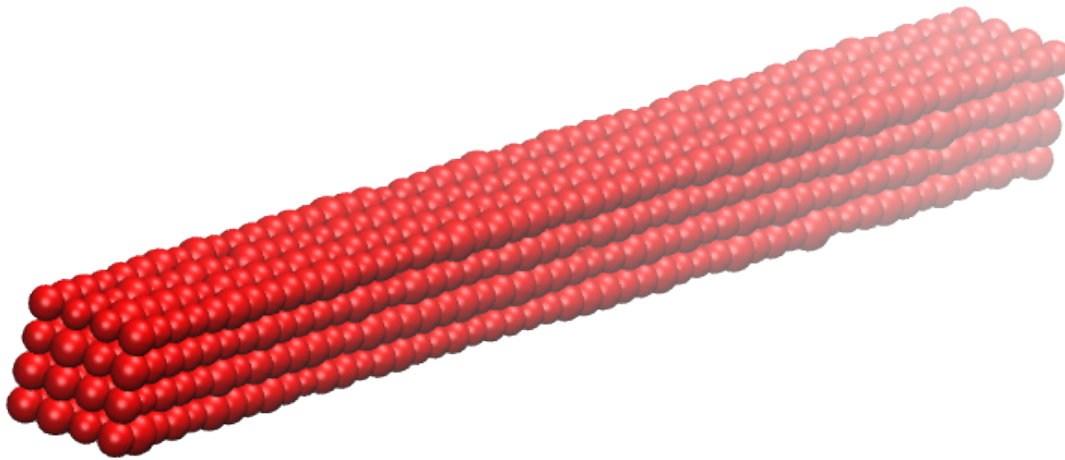
Mobility $\mu \sim 10^{-3} - 10^{-2}$ v. 10^3 cm²/Vs bulk Si

Hierarchical transport studies based on electron energy calculations



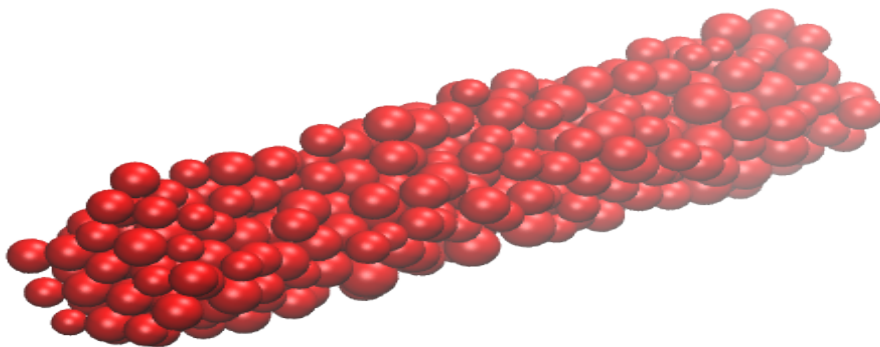
I. Carbone, S. Carter and GTZ J. Appl. Phys. 114, 193709 (2013)
M. Voros, I. Carbone, S. Carter, G. Galli and GTZ submitted

1. Define nanoparticle lattice



Nanoparticle radius selected with Gaussian distribution

Always six nearest neighbors, packing density $\sim \rho=0.52$



PackLSD: collision driven molecular dynamics

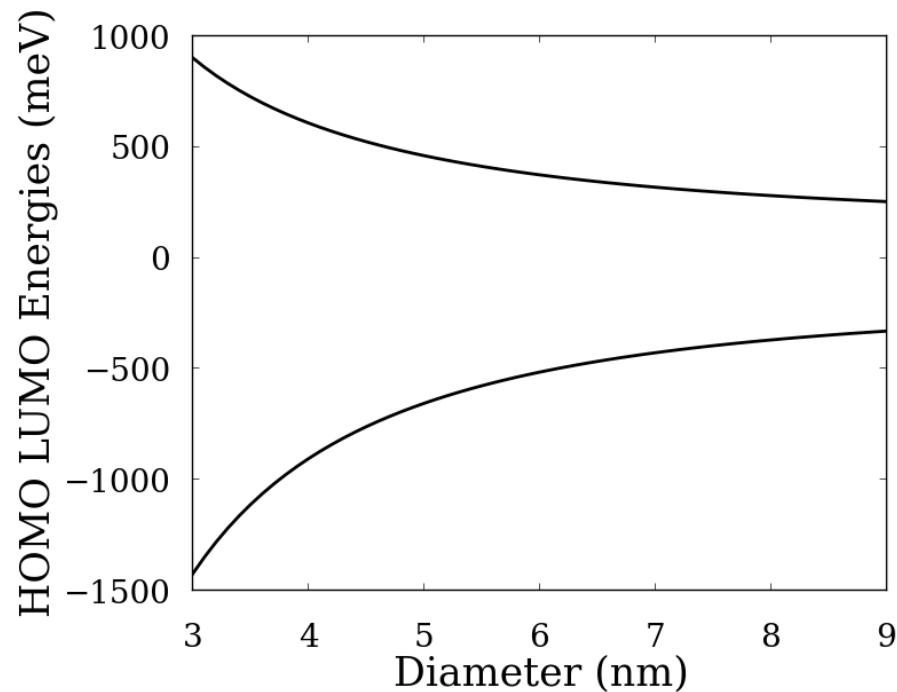
Generate disordered jammed packing, density: $\rho=0.62-0.63$

Donev et al, (2005)

2. Ab Initio Nanoparticle energetics

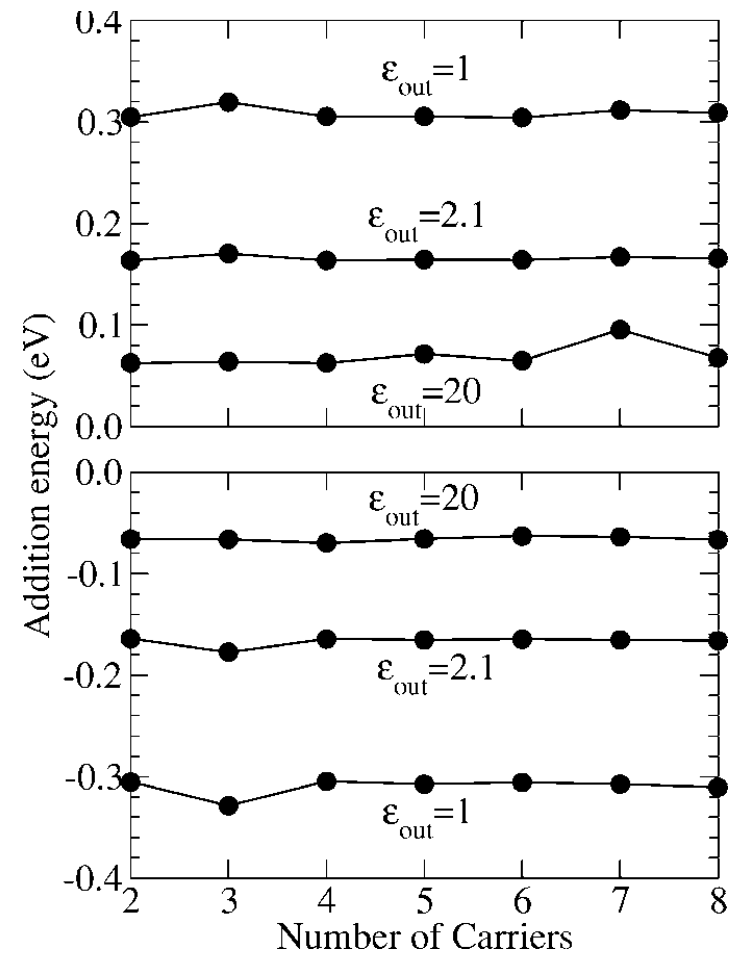
One-particle energy E^{1p}

Kang and Wise (1997)



Addition/charging energy E^c

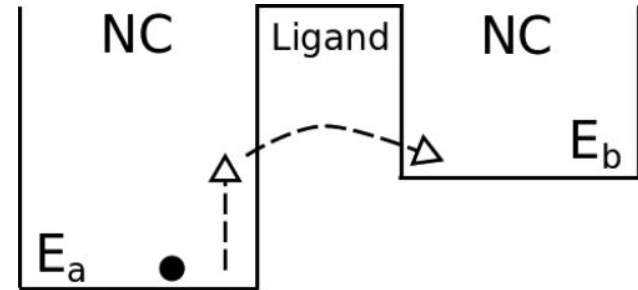
An, Franceschetti, Zunger (2007)



3. Dynamics: NP-NP Transition rates

Thermally activated
nearest-neighbor hopping

Miller-Abrahams: low T single phonon



$$\Gamma_{a \rightarrow b} = \Gamma_0 \exp(-2\beta\Delta x) \begin{cases} \exp\left(-\frac{E_b - E_a}{kT}\right) & (E_b > E_a), \\ 1 & (E_b \leq E_a). \end{cases}$$

$$\beta = \sqrt{\frac{2m^*(E_{vac} - E_{barrier})}{\hbar^2}}$$

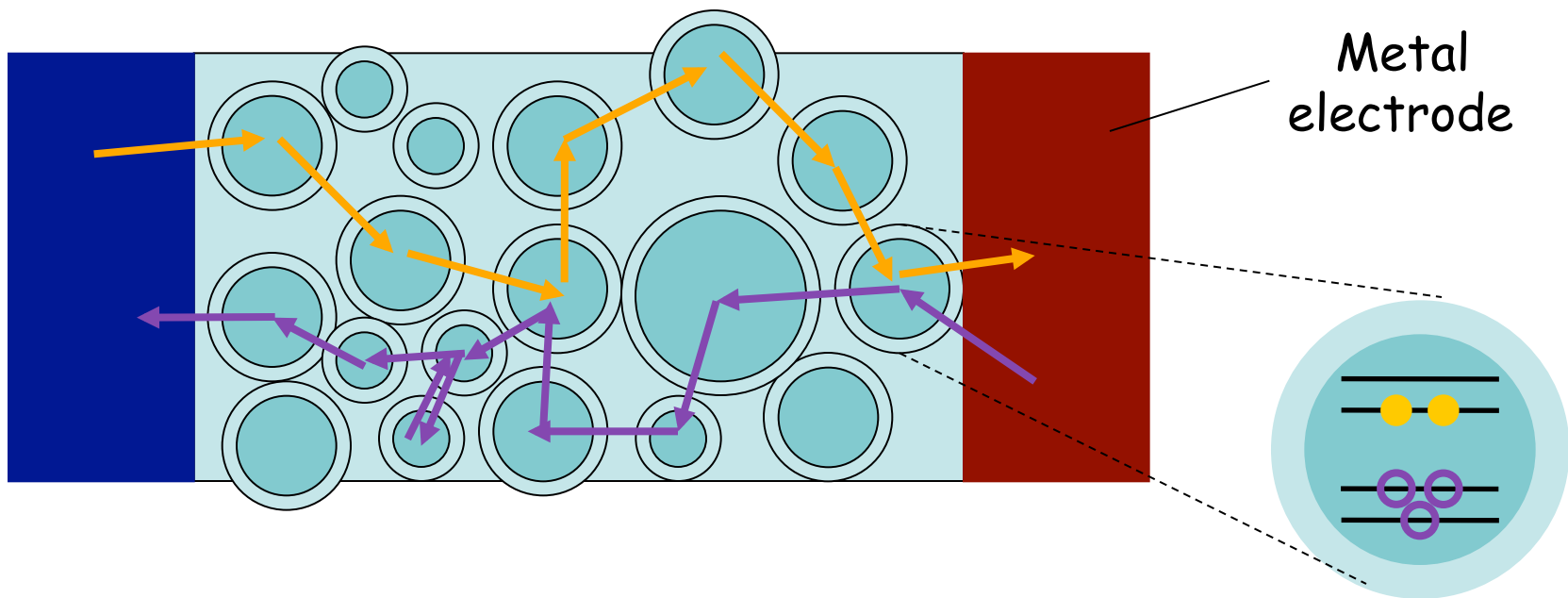
Marcus: high T "multi phonon"/polaronic

$$\Gamma_{a \rightarrow b} = \frac{2\pi}{\hbar} |H_{ab}|^2 \frac{1}{\sqrt{4\pi\lambda_{ab}kT}} \exp - \frac{(\lambda_{ab} + E_b - E_a)^2}{4\lambda_{ab}kT}$$

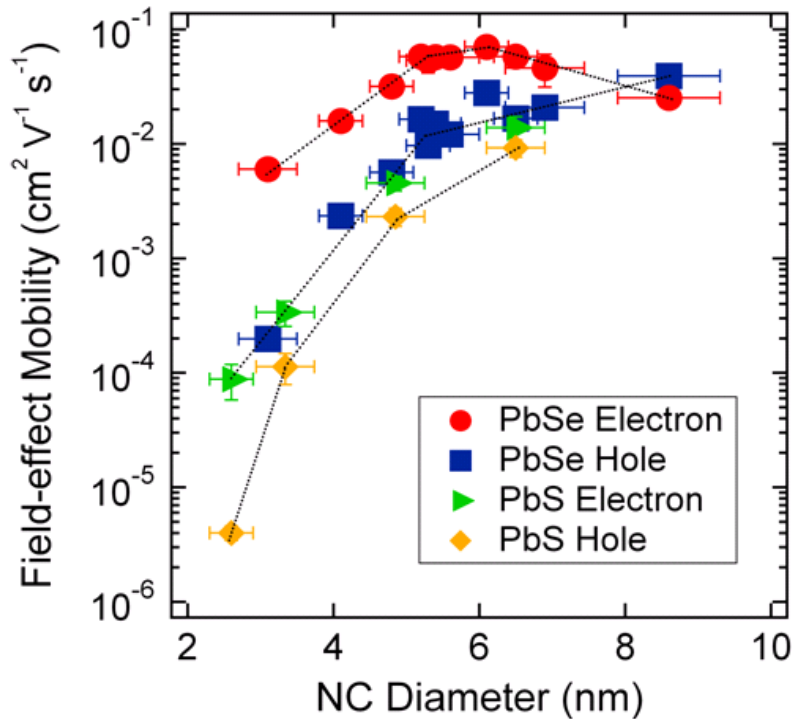
$$|H_{ab}|^2 \approx |H_0|^2 \exp(-2\beta\Delta x)$$

λ : reorganization energy
 H : "electronic coupling"

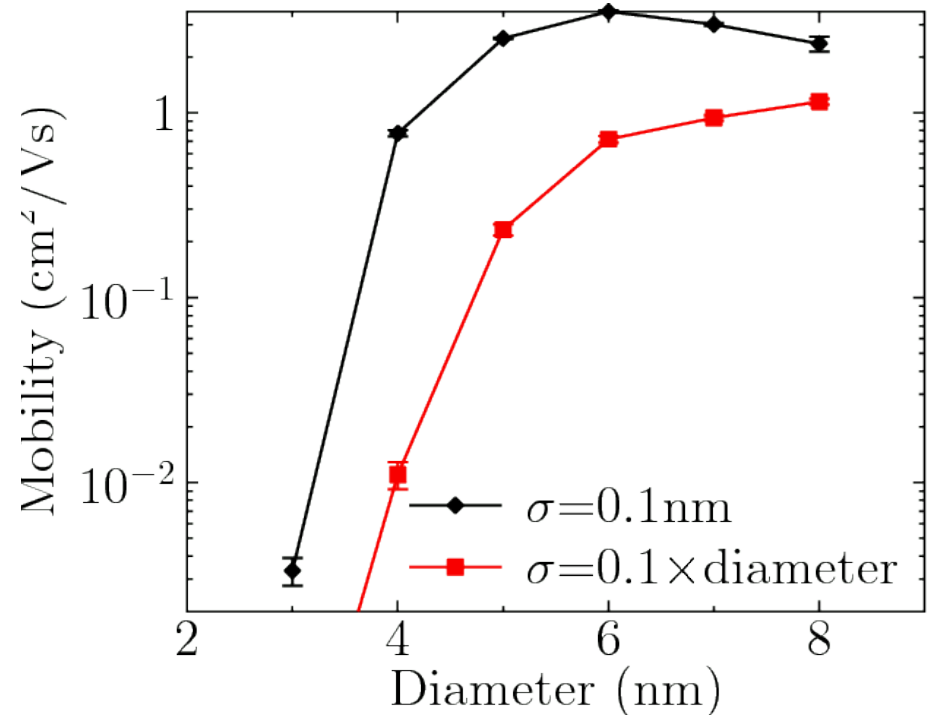
3. Dynamics: Device level modeling



RESULTS: Diameter dependence of μ



Small D: steep rise
Large D: plateau/decrease



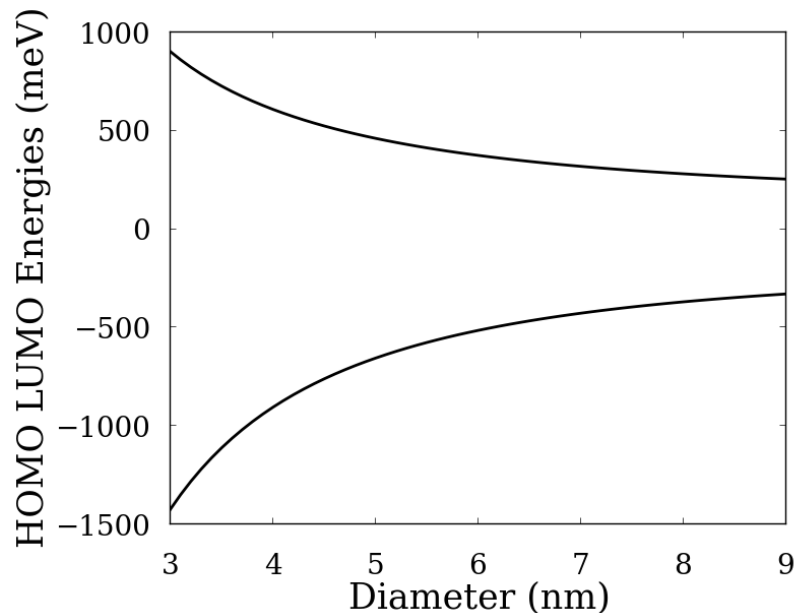
σ = width of NP size distribution

RESULTS: Diameter dependence of μ – Physics

Small D: steep rise

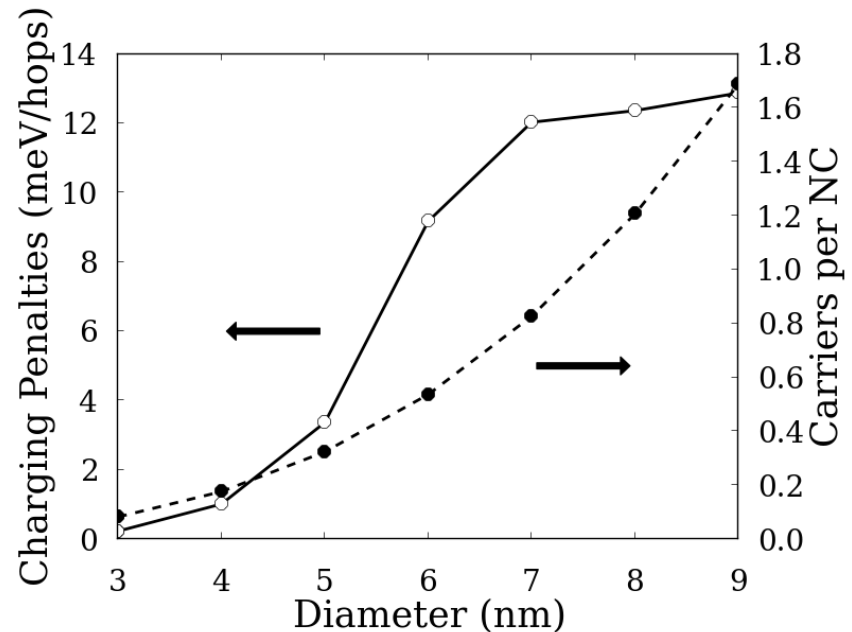
1. For increasing D less hops are enough to cross sample

2. $E^{lp}(D)$ less steep for increasing D, energy disorder is decreases with D



Large D: plateau/decrease

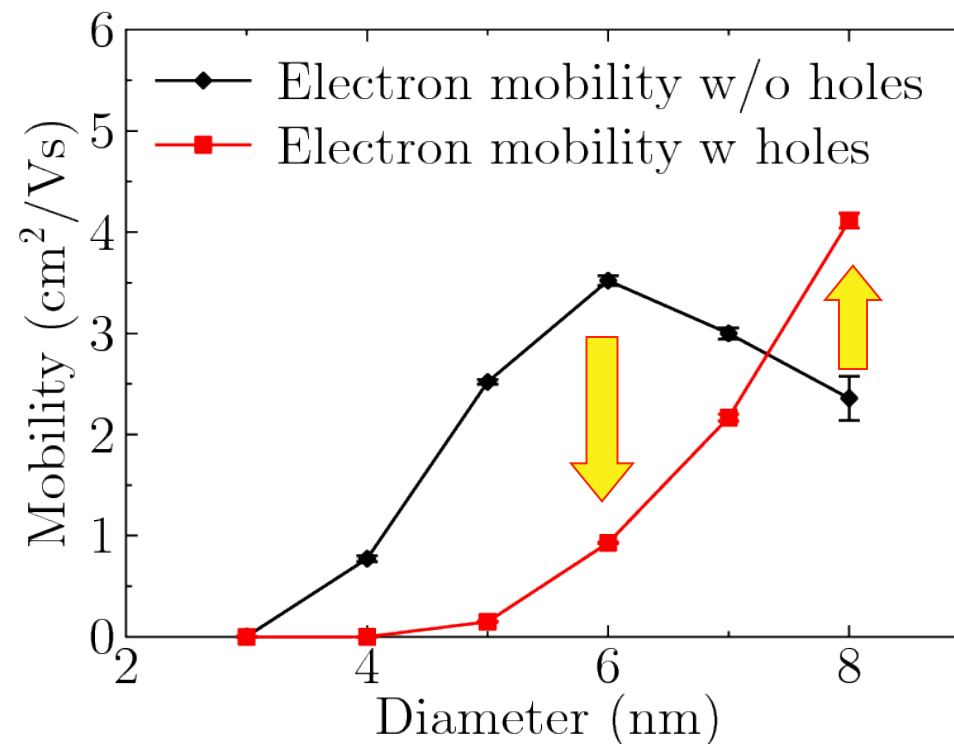
The electron density (#/unit volume) is kept constant, for increasing D the electron #/nanoparticle increases, increasingly blocking transport by Coulomb blockade/charging energy E^C



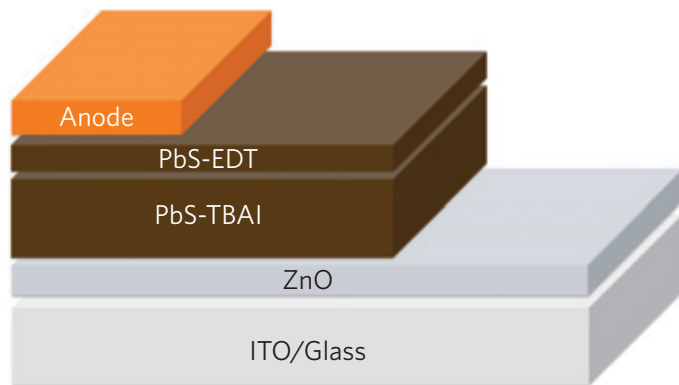
RESULTS: Verifying Electron-hole effects

Simulated equal electron and hole densities

Presence of holes neutralizes the Coulomb barrier:
conductivity grows instead of peaking

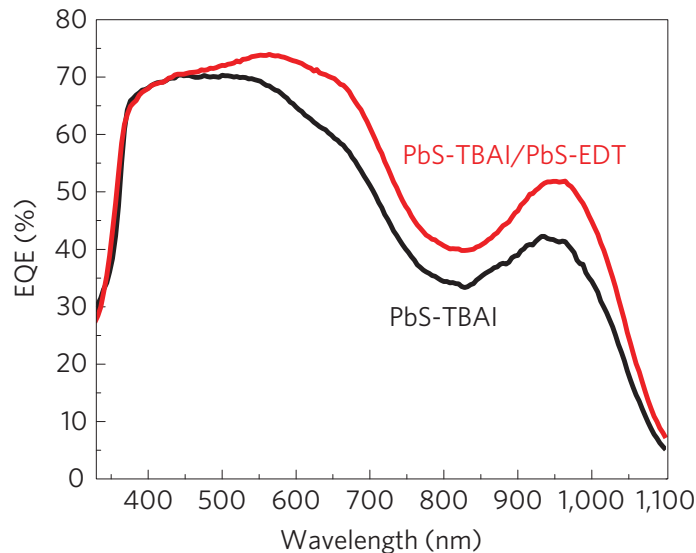


Transport optimization leads to 9% efficiency



Transport optimization by strategic

- ligand-exchange processes
- bandgap-engineering
- surface passivation and
- atomic layer deposition infilling



9.2% efficiency was reached in PbS-TBAI nanoparticle solar cells

Bawendi (2014)

2015: The year nanoparticle solar cells break 10% ?!

The Full Spectrum Boost Project

**Transcending competing paradigms in nanoparticle solar cells:
Integrating Transport and CM+IB boosted absorption**

**Unified Transport Theory:
Integrating band & hopping transport
Ab initio-based Multi-scale Modeling**

**Full Spectrum Boost:
Integrating the Intermediate Band &
Carrier Multiplication Paradigms**

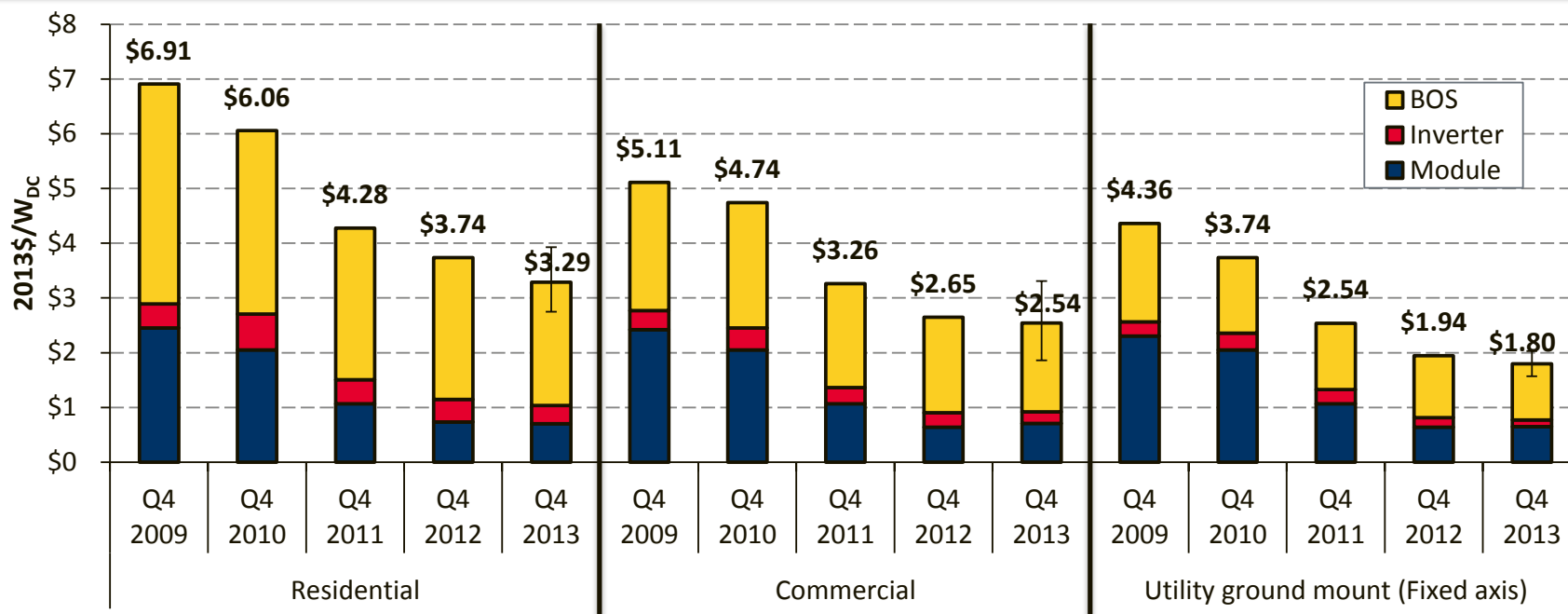
**Band transport:
ab initio-based
semi-classical
Boltzmann theory**

**Hopping transport:
ab initio-based
Marcus/Miller-Abr.
kinetic Monte-Carlo**

**Low energy boost:
Intermediate
Band in
NP solar cells**

**High energy boost:
Carrier
Multiplication in
NP solar cells**

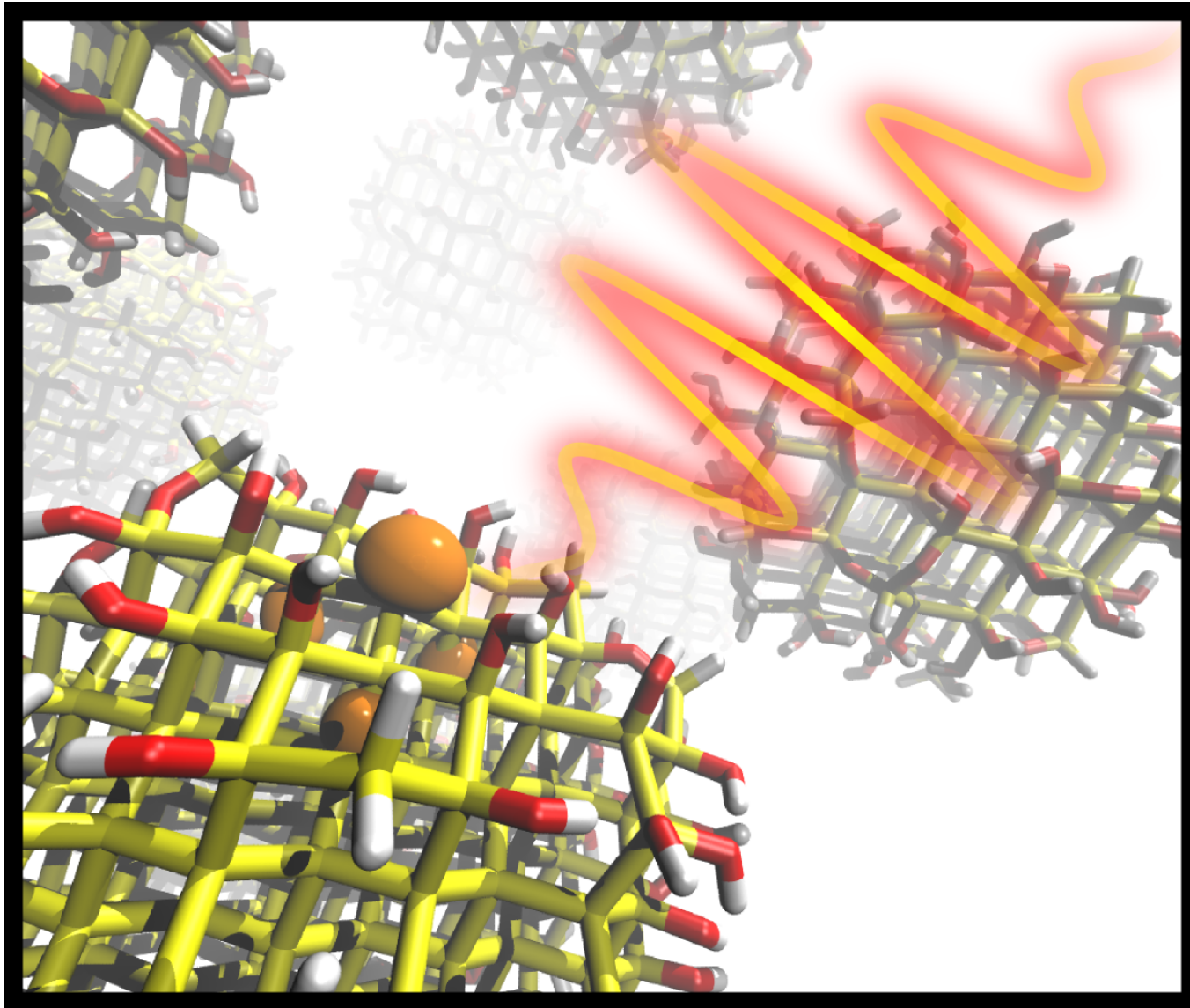
PV System Price, 2009-2013



- Since Q4 2009, modeled system prices fell between 16% – 19% per year
 - 1/2 - 2/3 of reduction attributed to module price reductions
- From Q4 '12 to Q4 '13, modeled system prices fell between \$0.07/W - \$0.44/W, or 3-12%
- Q4 2013 bottom-up modeled residential system price of \$3.29/W is consistent with leading residential installers' pricing, such as SolarCity's reported Q2 2014 costs (\$3.03/W), plus a reasonable operating profit margin.

Note: Standard crystalline silicon modules (13.5% efficiency in Q4 2009 to 15.0% in Q4 2013). System sizes: residential: 5 kW in Q4 2009 through Q4 2013; commercial: 202 kW in Q4 2009 to 223 kW in Q4 2012 (200 kW in Q4 2013); utility-scale: 175 MW in Q4 2009 to 185 MW to Q4 2013). Modeled system sizes in the residential and commercial rooftop sectors were chosen based on typical system sizes, then adjusted for optimal inverter configuration. System sizing for utility-scale benchmarks were chosen for comparison purposes against pricing reported from DOE's Energy Information Administration (2010).
 Source: SolarCity. (2014). "Cost Calculation Methodology." Accessed September 2, 2014: <http://investors.solarcity.com/events.cfm>.

Reduction of Nonradiative Recombination by Strain in Nanoparticle Arrays



Reduction of Nonradiative Recombination by Strain in Nanoparticle Arrays

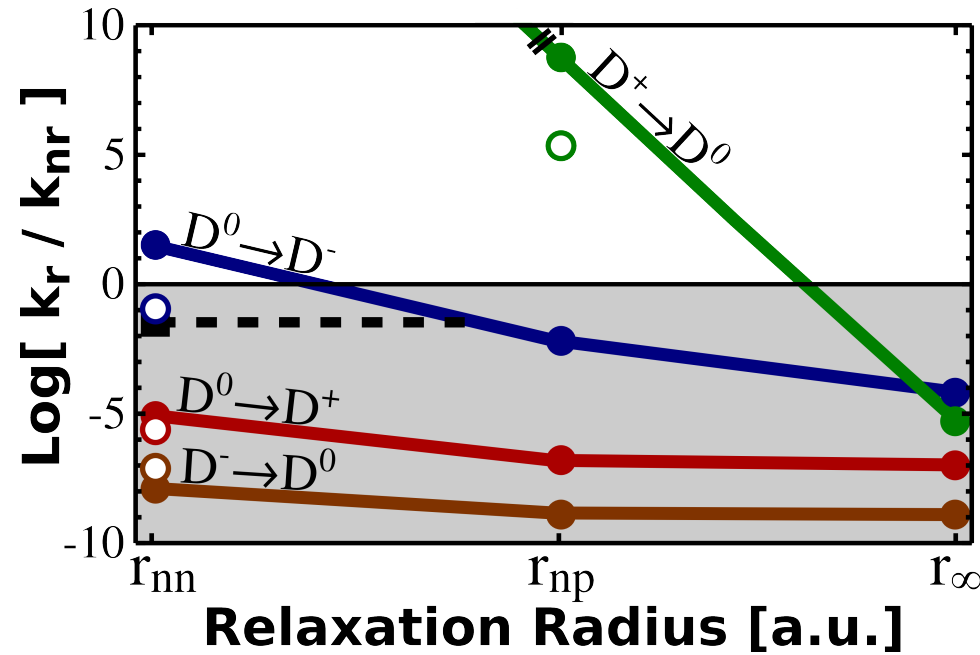


Figure 5: The logarithm of the ratio between radiative (k_r) and nonradiative (k_{nr}) decay rates for the four capture processes outlined in Figure 4, as a function of decreasing strain on the NP (see text), for a P_b defect at the surface of a 1.3 nm Si NP terminated by an oxide layer. The black horizontal line represents the boundary between radiative (white area) and nonradiative (gray area) recombination processes. Configurations representing different relaxation schemes around the defect (and hence different amount of strain) are shown on the x axis: r_{nn} (nearest neighbor), r_{np} (Si NP and first layer of oxygen) and r_{∞} (all atoms in the system). Nonradiative rates given by Equation 7 and 3 are indicated by the dots and open circles respectively.

4.2. Projected DOS

Projected states to atomic orbitals to determine character of states

$$EDOS_{\text{region}}(E) = \sum_j \sum_{i \in \text{region}} |\langle \phi_i | \psi_j \rangle|^2 \delta(E_j - E)$$

