

Multi-Exciton Generation in Nanostructured Solar Cells

The energy challenge is one of the greatest moral and intellectual imperatives of our age

The science of energy is challenging, philosophically satisfying and fun

G.T. Zimanyi
UC Davis



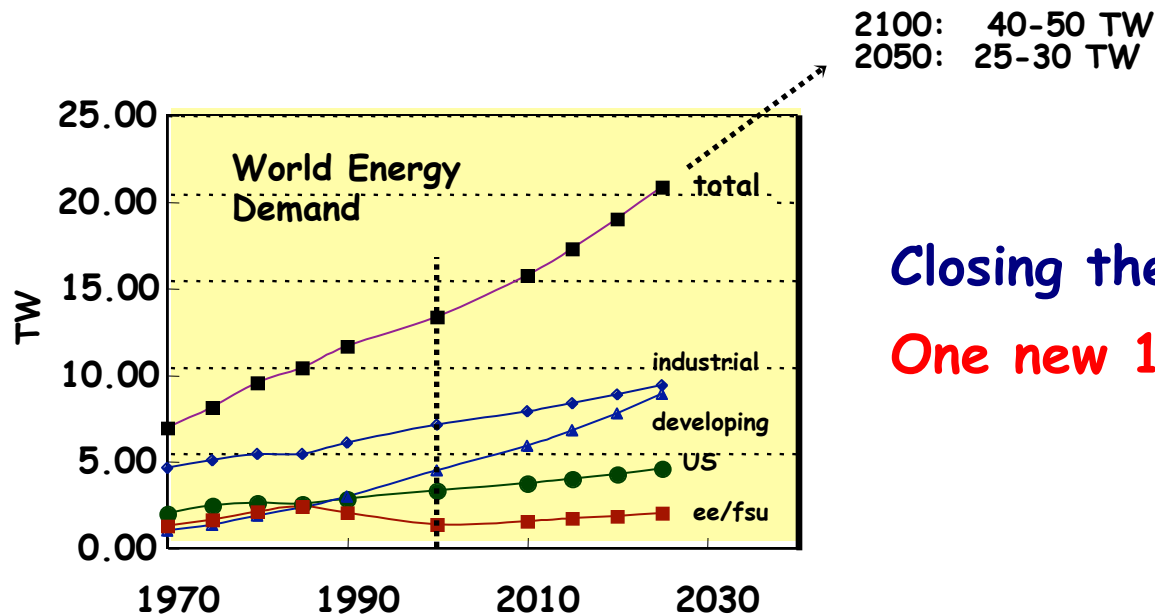
Multi-Exciton Generation in Nanostructured Solar Cells

- I. Why study Solar Energy Conversion?
- II. Entry points for physicists into Energy Science
- III. Multi-Exciton Generation: the UC Davis Solar Collaborative

Grand Energy Challenge

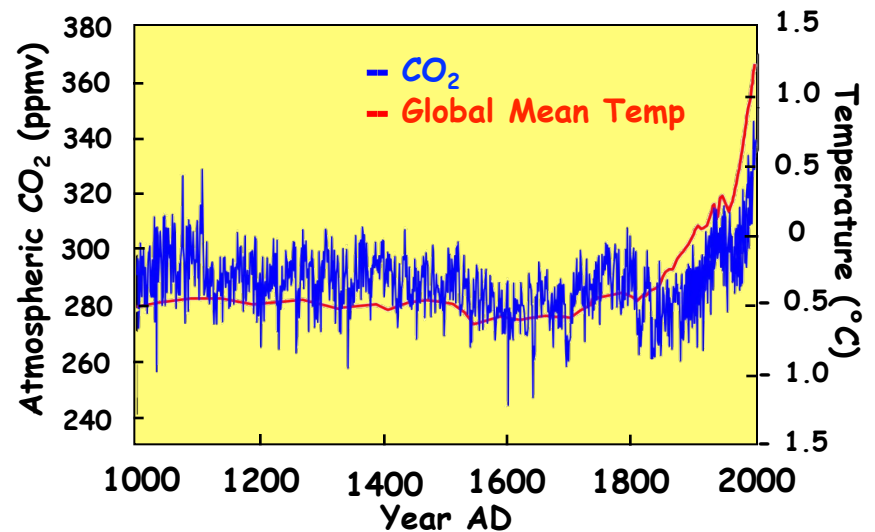
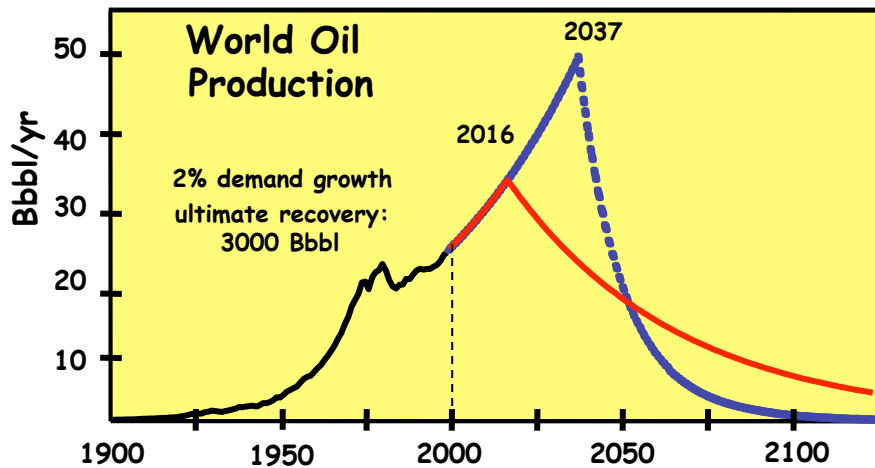
Demand gap

- double demand by 2050, triple demand by 2100
- gap between production and demand:
14TW(2050)-33TW(2100)



Closing the demand gap requires:
One new 1GW power plant/day!

Oil: Works today, Hurts tomorrow



1. Oil and coal will run out
2. Produced by regions of conflict
3. Uneven distribution of production, wealth
4. Primary cause of climate change:
5. We just crossed 400ppm CO₂ content

Sources of Renewable Energy

Solar

1.2×10^5 TW on Earth's surface
36,000 TW on land (world)
2,200 TW on land (US)

Wind

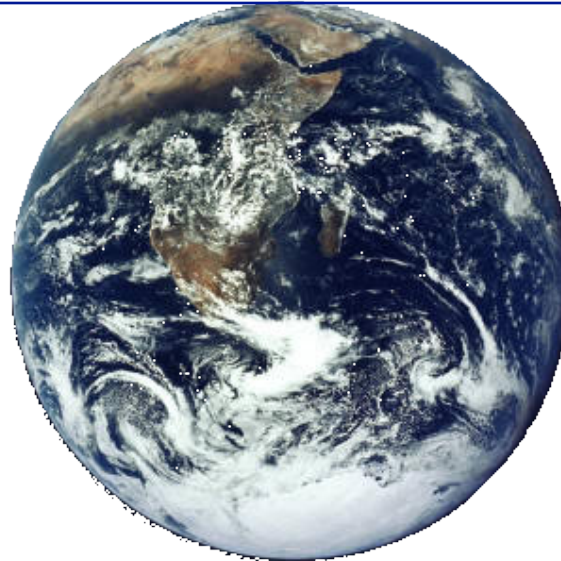
2-4 TW extractable

Tide/Ocean Currents

2 TW gross

Geothermal

9.7 TW gross (world)
0.6 TW gross (US)
(small fraction technically feasible)



Biomass

5-7 TW gross (world)
0.29% efficiency for
all cultivatable land
not used for food

Hydroelectric

4.6 TW gross (world)
1.6 TW technically feasible
0.6 TW installed capacity
0.33 gross (US)

Solar is the Most Promising Energy Resource

Sunlight is a singularly suitable energy resource

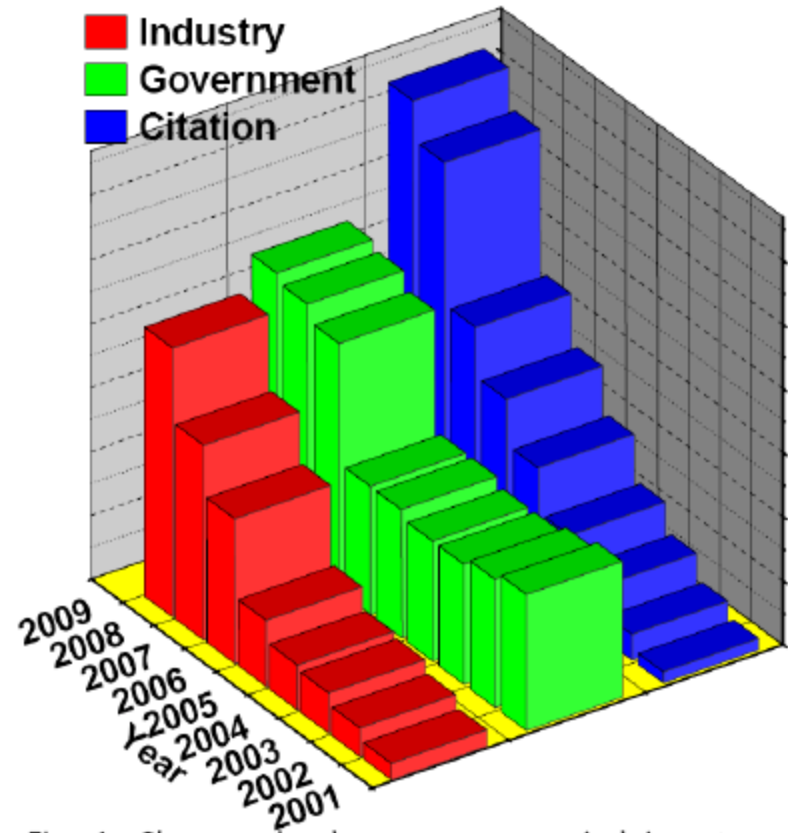
1. the only resource in sufficient quantity
2. environmental impact is minimal and benign
3. no catastrophic breakdown mode
4. politically safest, conflict-free
5. non-man-made price volatility is minimal

The Solar Opportunity: Recent Expansion

Venture capital investments

DOE solar technologies budget

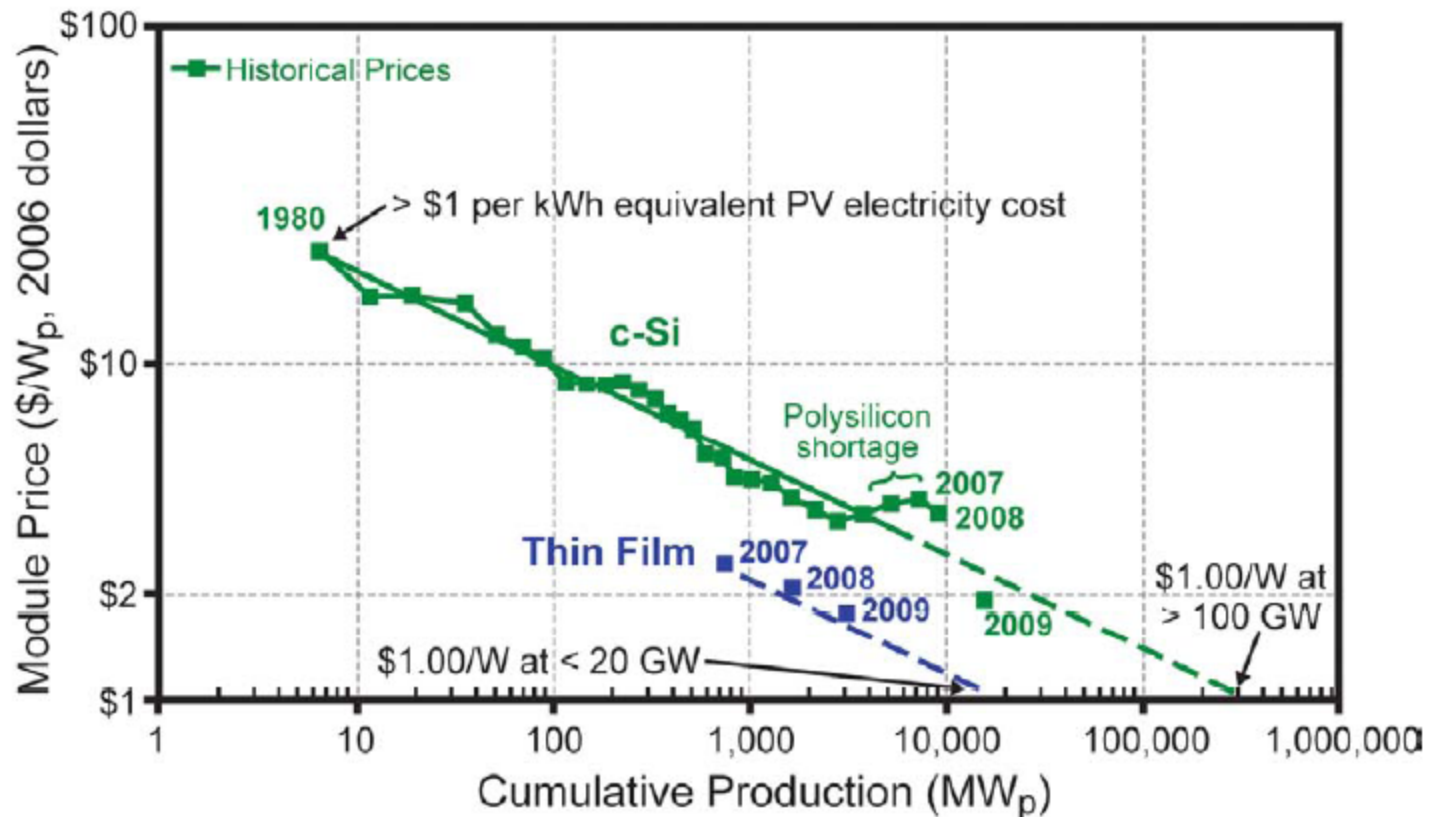
Photovoltaics citations in ISI
database



Opportunity, Lost

1. A 100x100 mile area covered with PV can provide all of the energy needs of the US, completely eliminating the need for burning oil
2. On today's prices installing this would be ~ \$500bn, 25-50% of the bank bailout of 2009!

The Solar Moore's Law



Price drops by 20% for every doubling of production
No doubling per 18 months as area is not scaled down as in chips

2011/2012 Developments

1. Market: PV reached presumed grid parity:

- Ampulse Energy: 0.92 \$/W (Mar. 2012),
- Since then 0.72 \$/W: Price of imported Si wafers plummeted because of Chinese over-production and market collapse: **SunShot goal achieved!**
- But: fracking of natural gas **moved grid parity to 0.3\$W**

2. Science:

- GaAs: Alta Devices: 28% lab, 23.5% NREL verified
- Organic solar cells: Sumitomo 10.6% efficiency

DOE Scientific Priorities - 2010

“Progress largely driven empirically, understanding of even existing cells is lacking” - The opportunity for physics

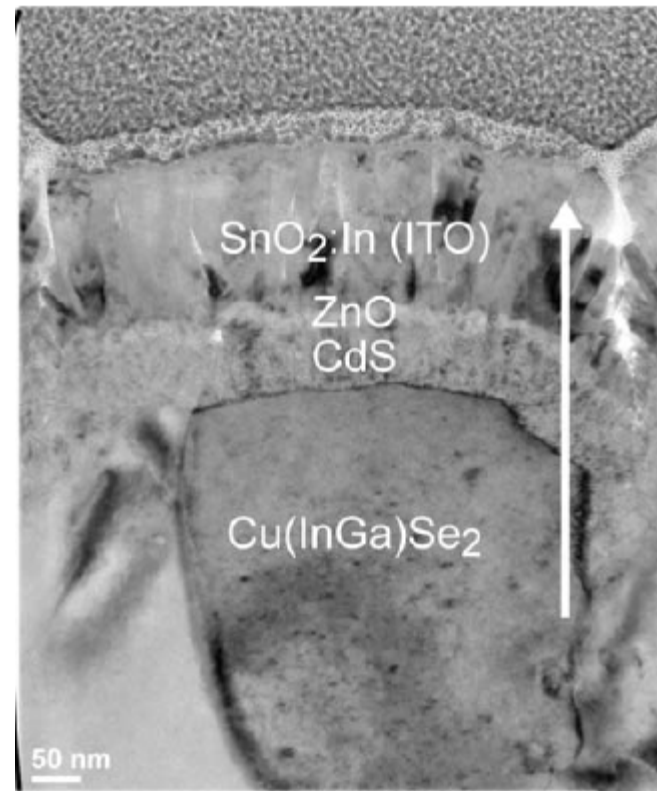
1. Characterization and modeling of interface processes:

- dopant diffusion,
- gap states caused by metal defects,
- real effect of laser lithography,
- band alignment

2. Defects, grain boundaries

3. Interface inhomogeneities

4. Processes at contact

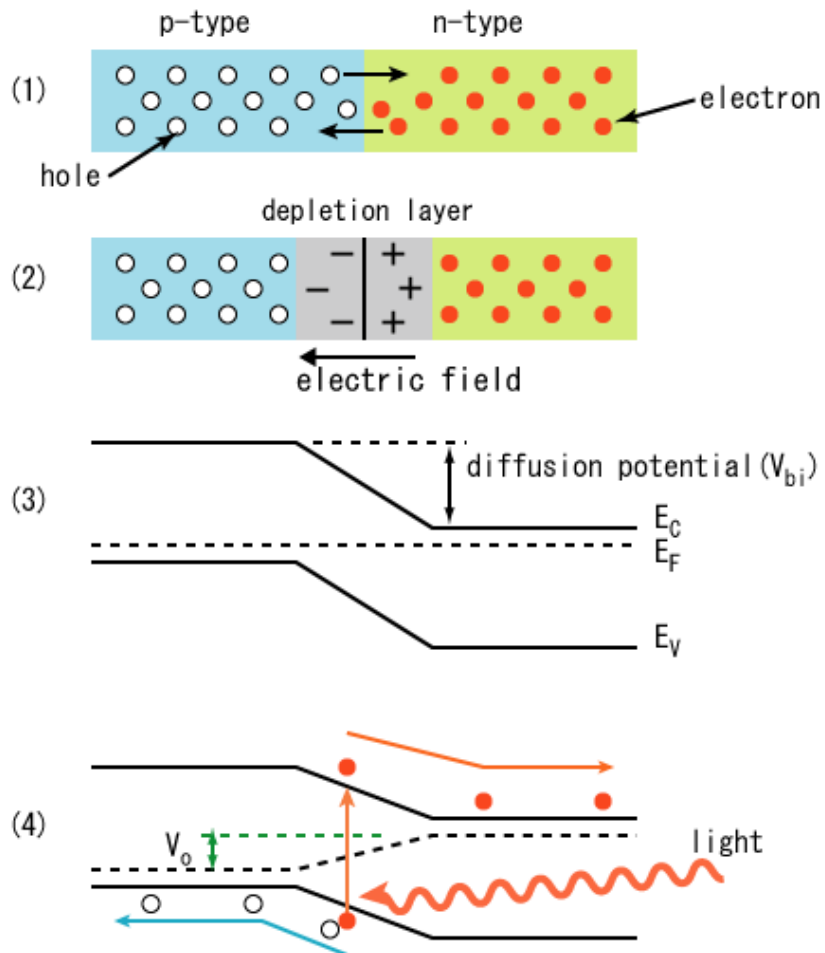


II. Entry Points for Physicists: Energy Science is Kool

“Progress largely driven empirically,
understanding of even existing cells is lacking”

1. Correlated impurities + Coulomb interaction
2. Multiple scattering theory
3. Plasmon-enhanced solar cells
4. Avalanches on driven Bethe-lattices
5. Path-breaking PV designs
6. Strong Coulomb interaction in nanoparticles

0. Solar Energy Conversion: Basics



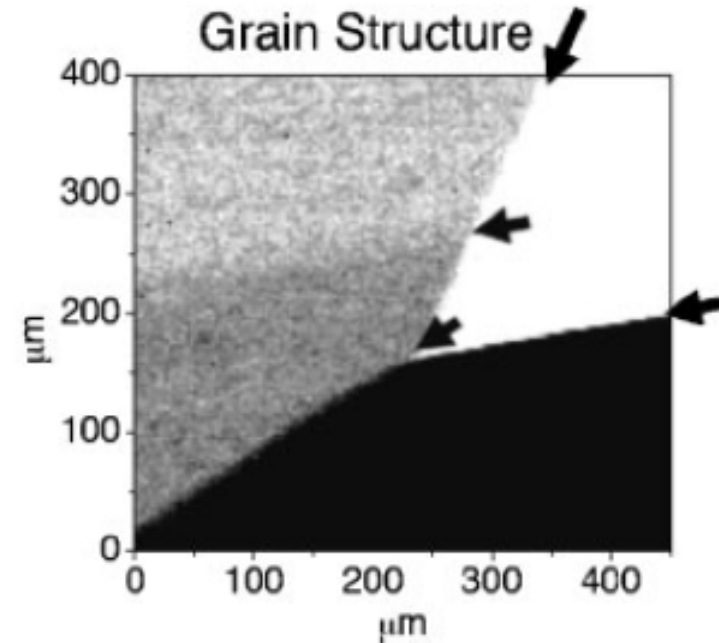
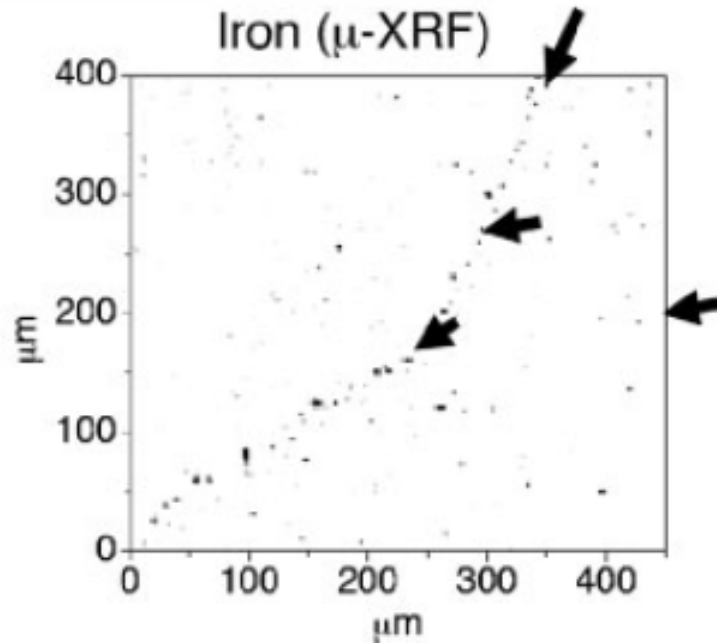
Challenges include:

1. Capture much of the solar energy in electronic sector
2. Drive photo-electrons to electrodes with little loss to recombination
3. Cell needs to be cheap
4. Cell needs to be durable (20 yrs!)

1. Correlated Impurities + Coulomb Interaction

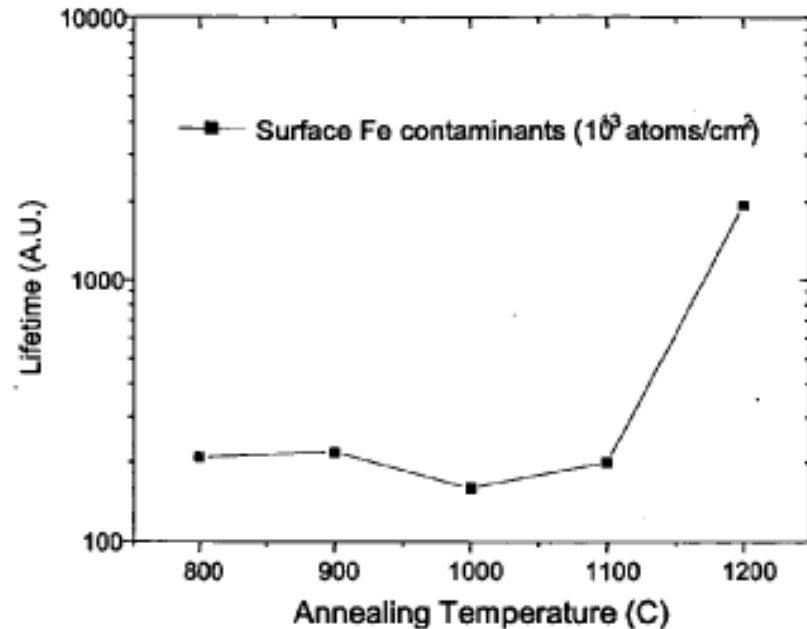
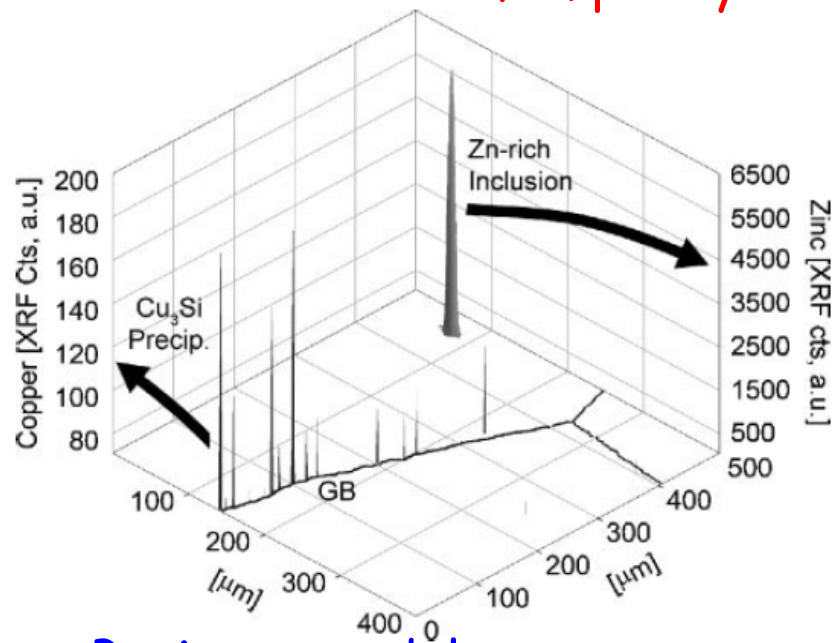
- Recombination is primary enemy of photo-electron extraction
- Driven by Coulomb interaction, enhanced by metallic impurities
- Metal impurities are lethal recombination centers even at $n=10^{16}\text{cm}^{-3}$

Weber: if you can't eliminate them, precipitate them to grain boundaries



Exciton Lifetime Extended

- Physics:
- electron-hole recombination driven by Coulomb attraction
 - enhanced by metallic impurity sites
 - location of impurity sites is correlated

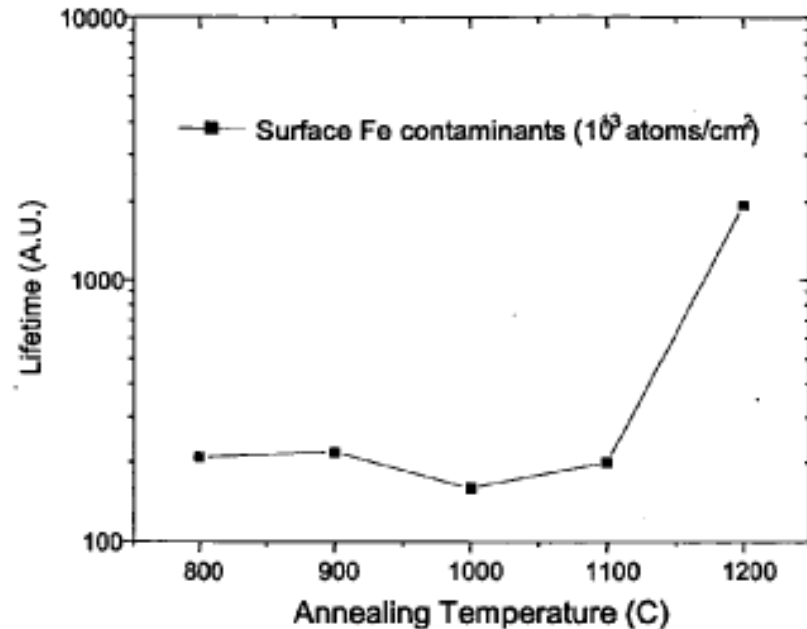
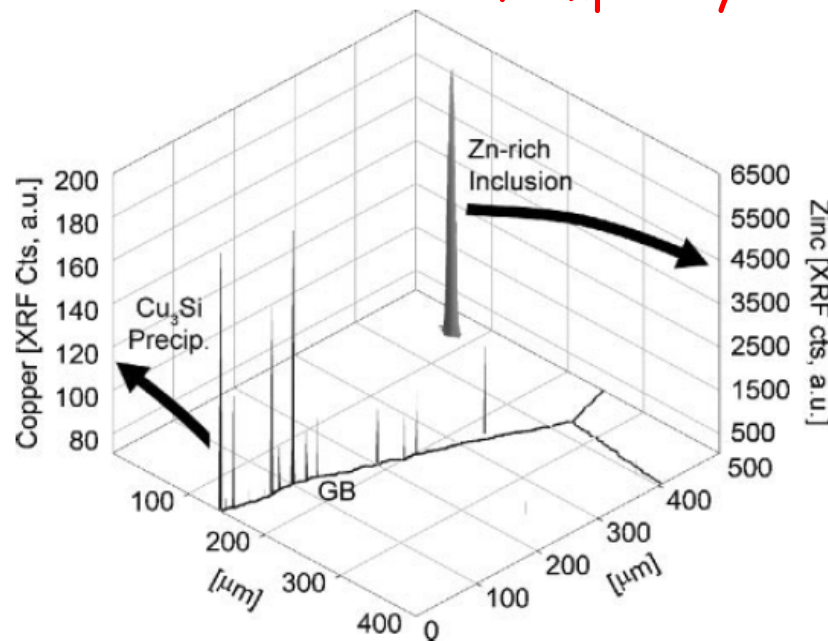


Business model:

- reduce costs by buying low grade ingots instead of expensive wafers
- precipitate impurities by gettering
- reach **16%** conversion efficiency

Exciton Lifetime Extended

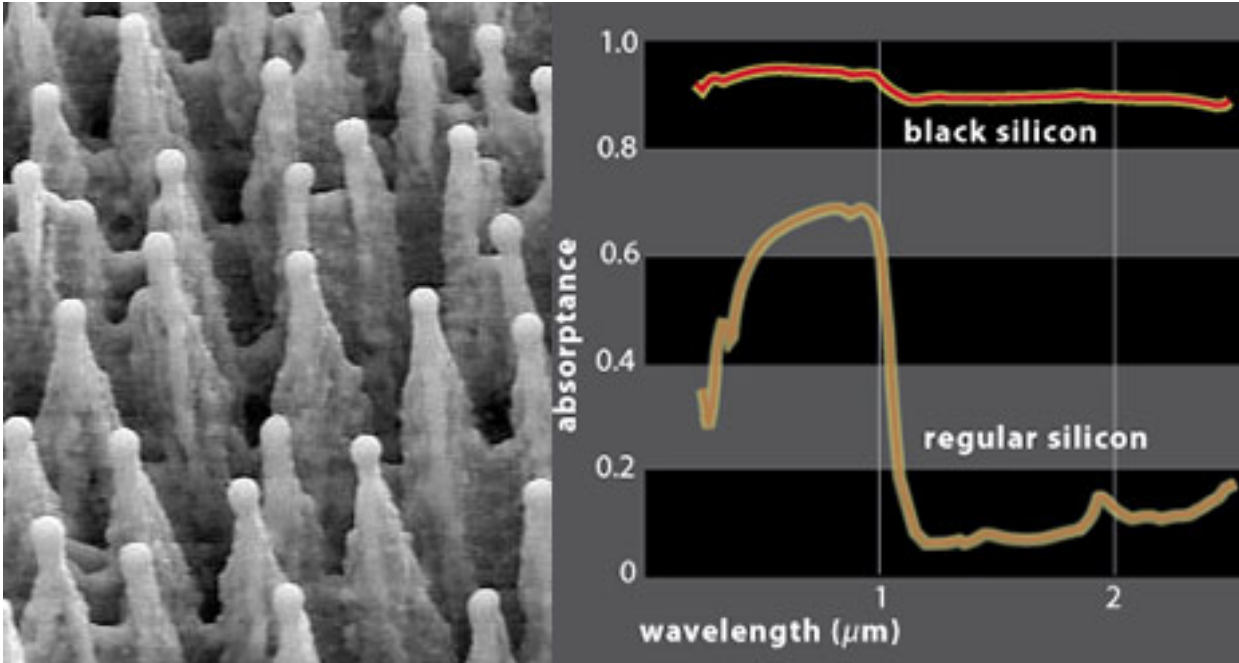
- Physics:
- electron-hole recombination driven by Coulomb attraction
 - enhanced by metallic impurity sites
 - location of impurity sites is correlated



Founded Calisolar Inc.
Shook hands with Schwarzenegger



2a. Multiple Scattering Theory: Black Silicon



E. Mazur (Harvard)

- blast crystalline Si with femtosecond laser pulses in a dense pattern

- in SF₆ atmosphere

Absorption increases close to unity!

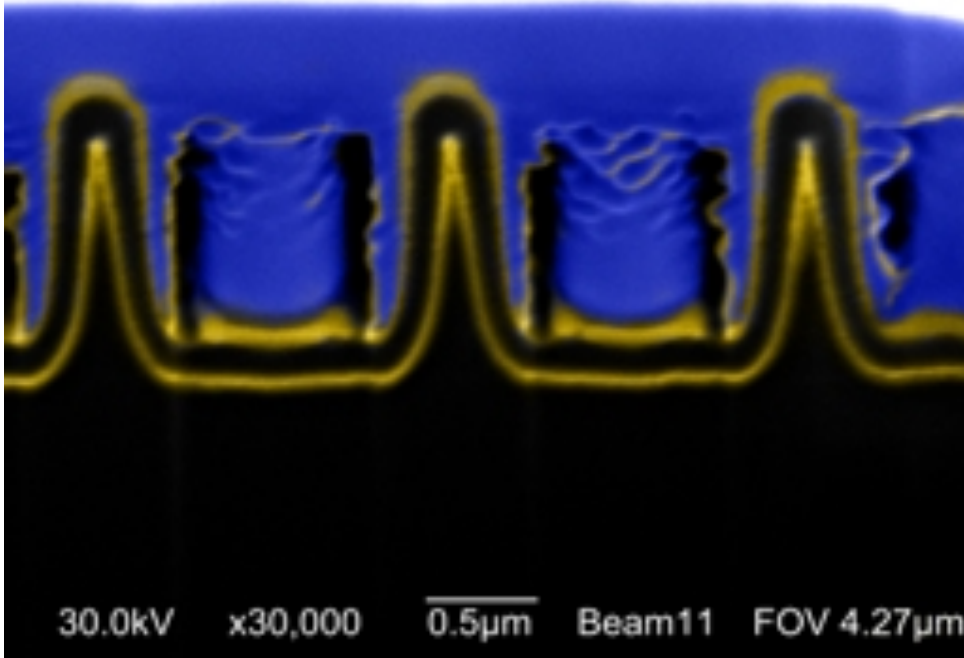
Absorption high in bandgap!

Founded **SiOnix Inc.**

Physics:

1. Nanostructure forms on surface, multiple reflections enhance absorption
2. High density of defect states in gap
3. “Hyper-doping” of top junction layer: sulfur

2b. Nano-Coaxial Cable



Achieved 8% efficiency
Founded **Solasta Inc.**

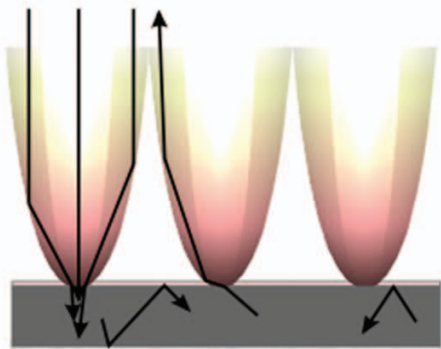
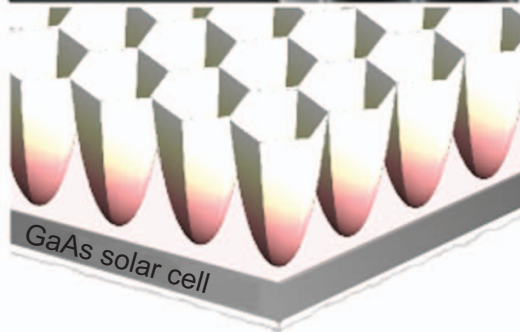
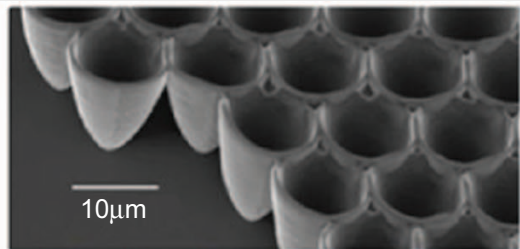
M. Naughton (BC)
Thick and thin problem

PV needs to be
thin to minimize material
cost, and
thick to still absorb light

Nano-sized “coaxial cable”
formed in amorphous Si
can optimize these
constraints

2.c. Photon management

Limiting re-emission angle - Atwater (Caltech)

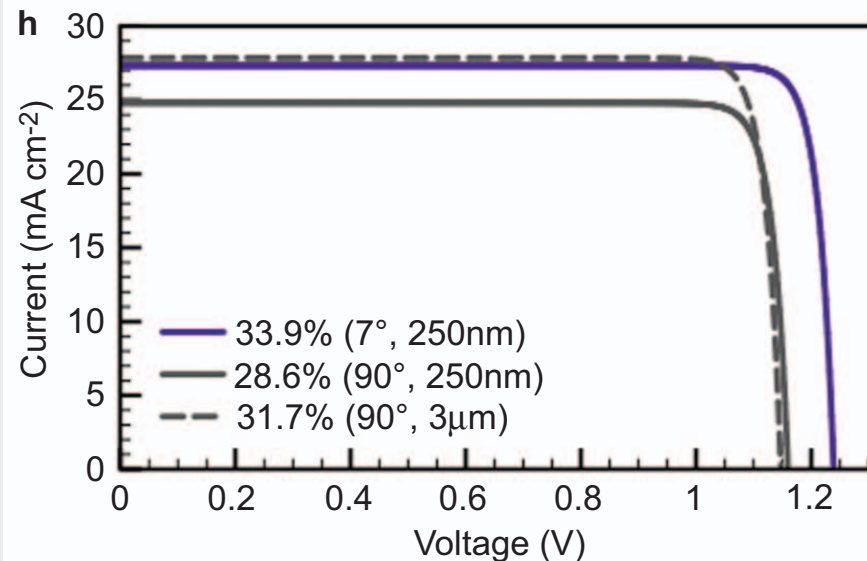


Balance with radiation field skewed:

Incoming radiation from narrow Sun disk

Re-emitted outgoing radiation to full spatial angle

Limiting re-emission angle improves balance:



3a. Plasmon-enhanced Solar PV Cells

“Thick and thin” redux:

Silicon is expensive

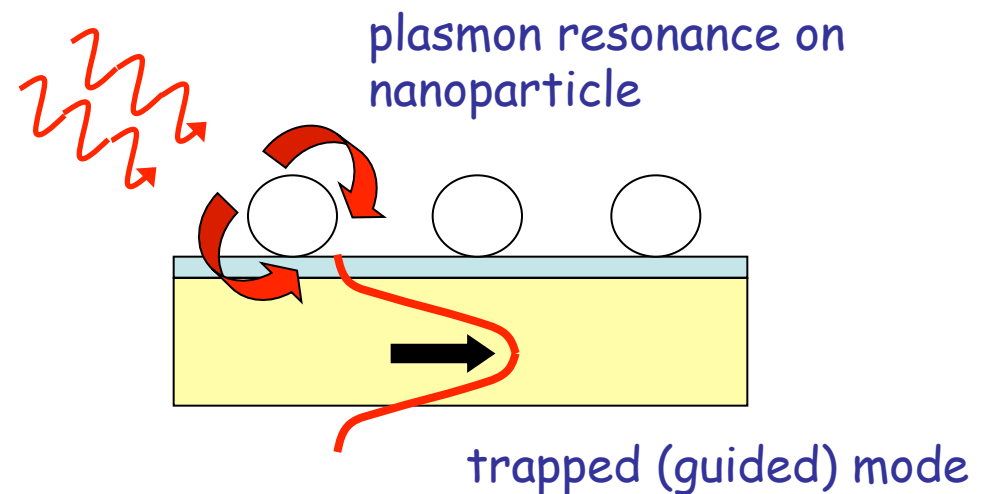
Today's solar cells: 300 micron thick

Make them 30 micron thick: cheaper

But: light will go through

Physics:

Redirect and capture light
with plasmon resonance of
nanoparticles

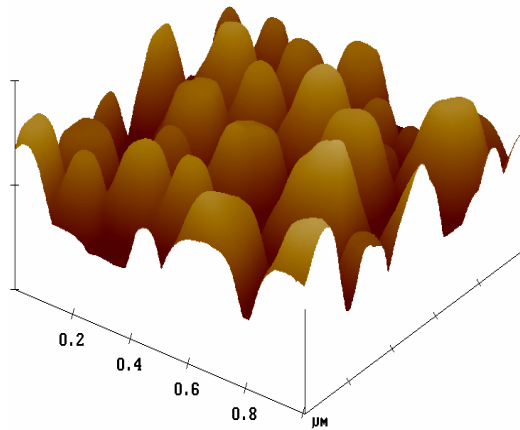


AFM/SEM Imaging

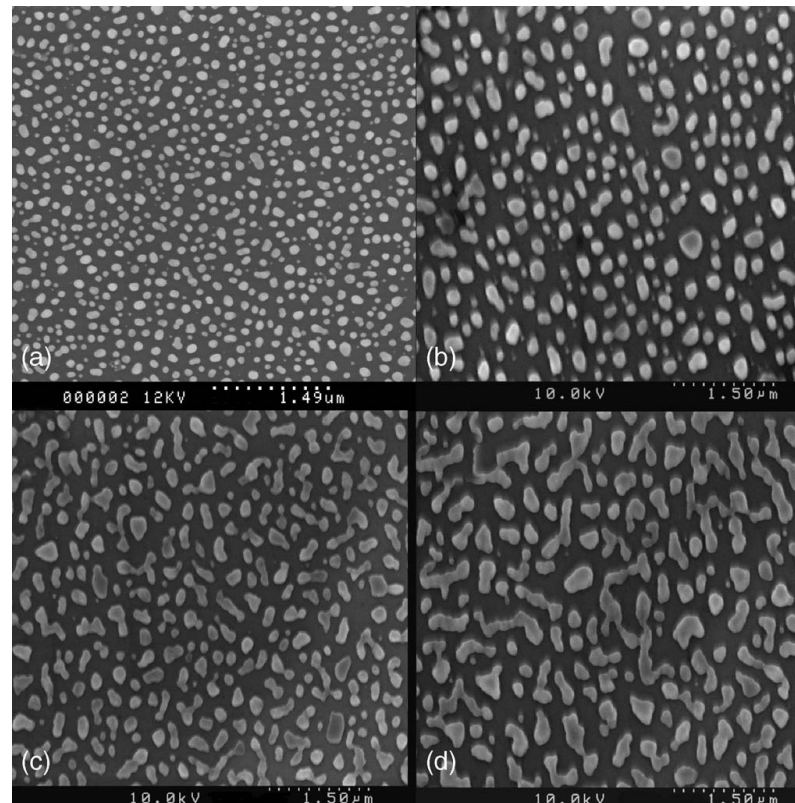
Islands on SOI formed by evaporation of silver followed by annealing for 1 hour at 200°C

film thickness $z=14$ nm

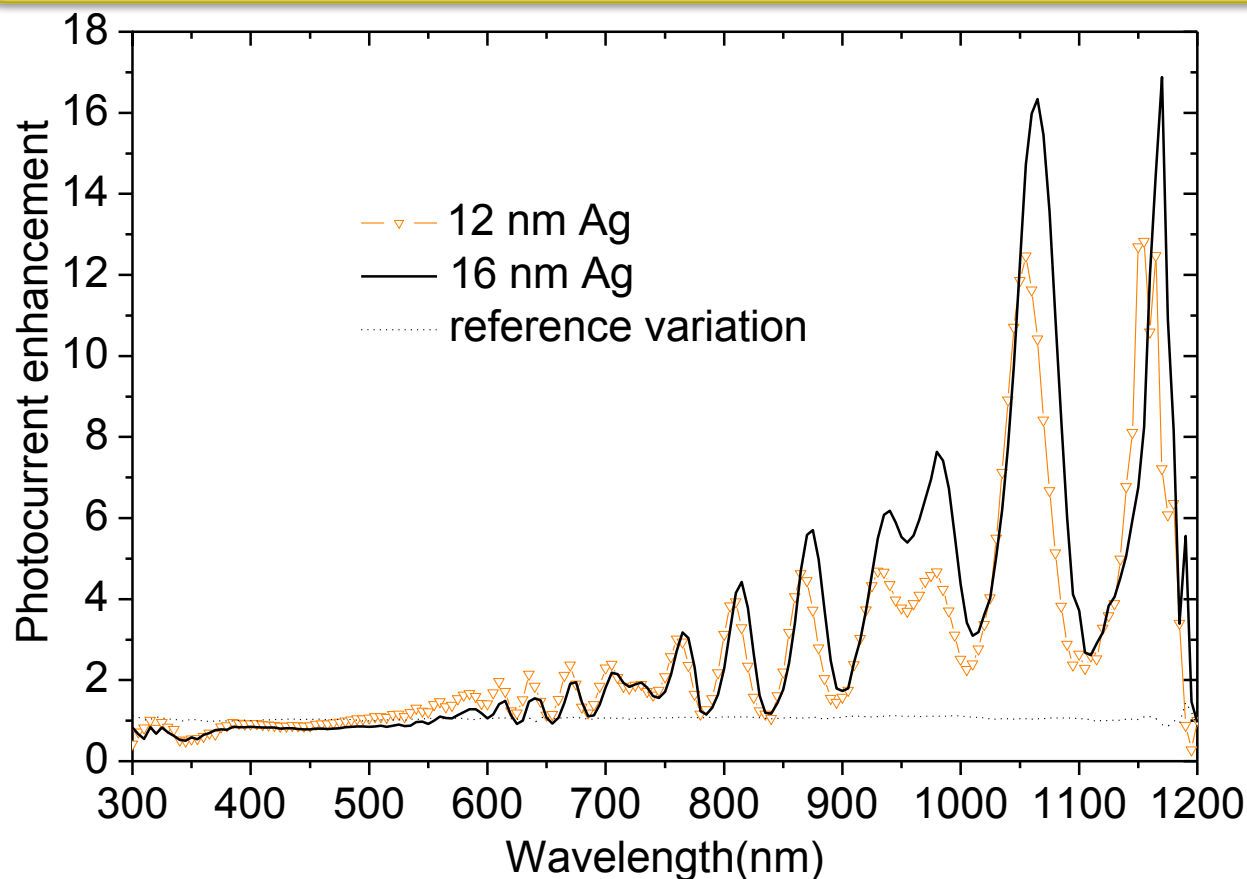
grain $d=120$ nm



$z=18$ nm



Plasmon-enhanced absorption in thin film cells



16X enhancement at 1050nm

30% enhancement over AM1.5G spectrum

Featured in the news section of Science, 2007: "New Solar Cells See the Light"

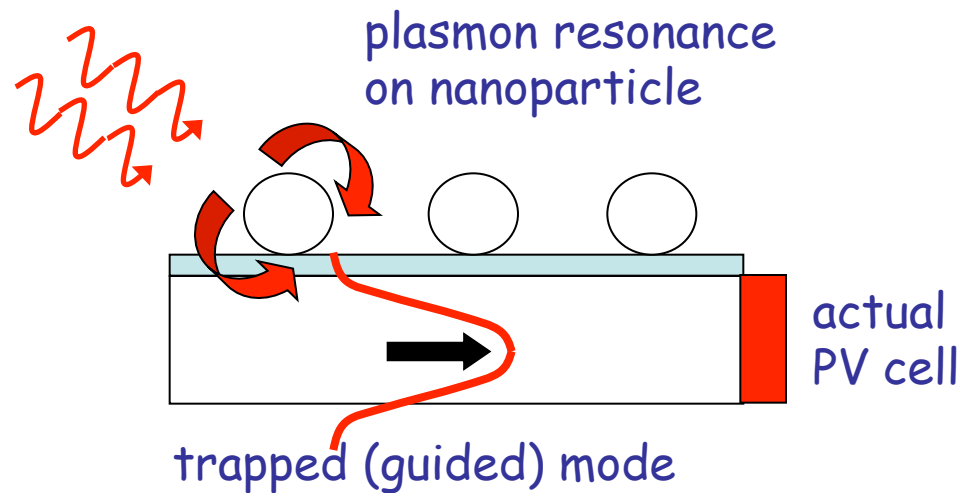
3b. Plasmon-enhanced Solar Concentrator Cells

“Thick and thin” max:

Silicon is expensive

Put small PV cell to

the edge of the glass!

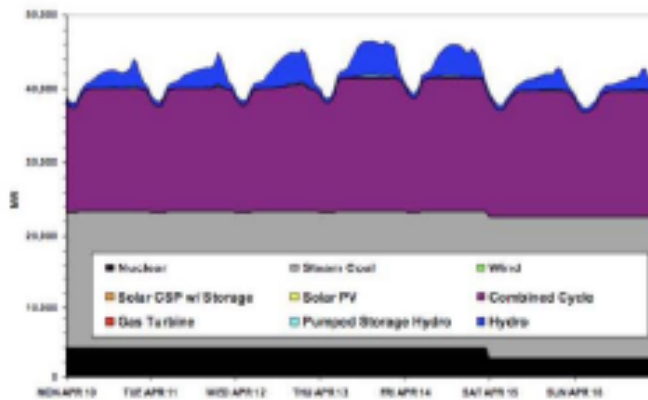


4. Renewables Can Induce Grid Instabilities

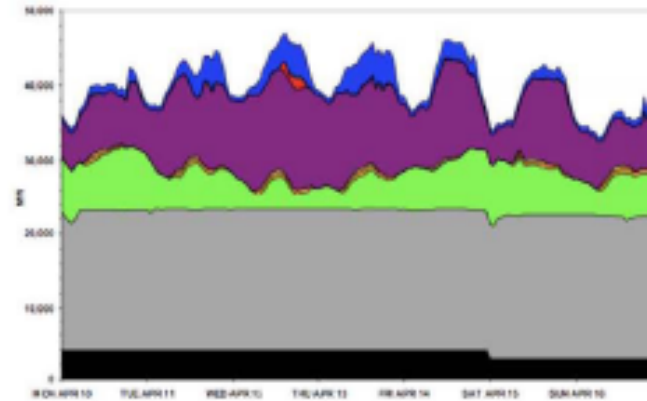


OE - Variable Generation Affects Grid Operations

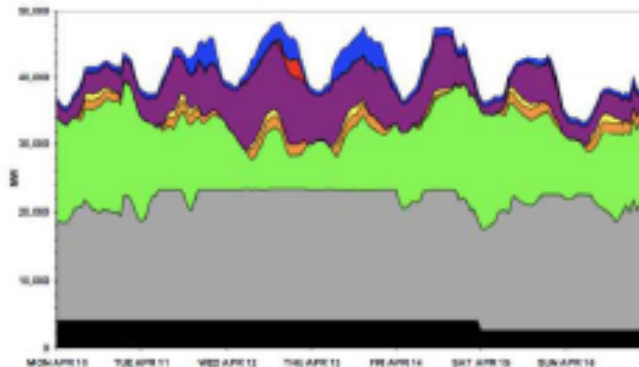
No wind



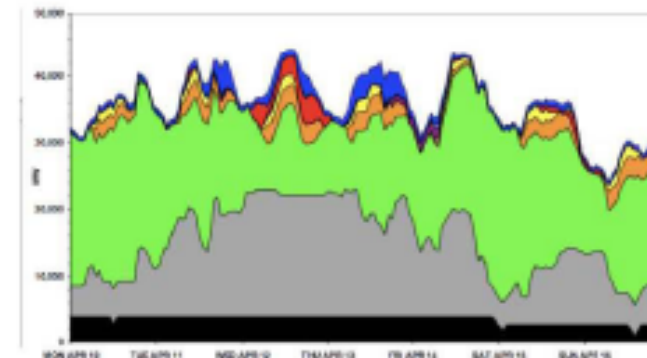
11% renewables



23% renewables



35% renewables



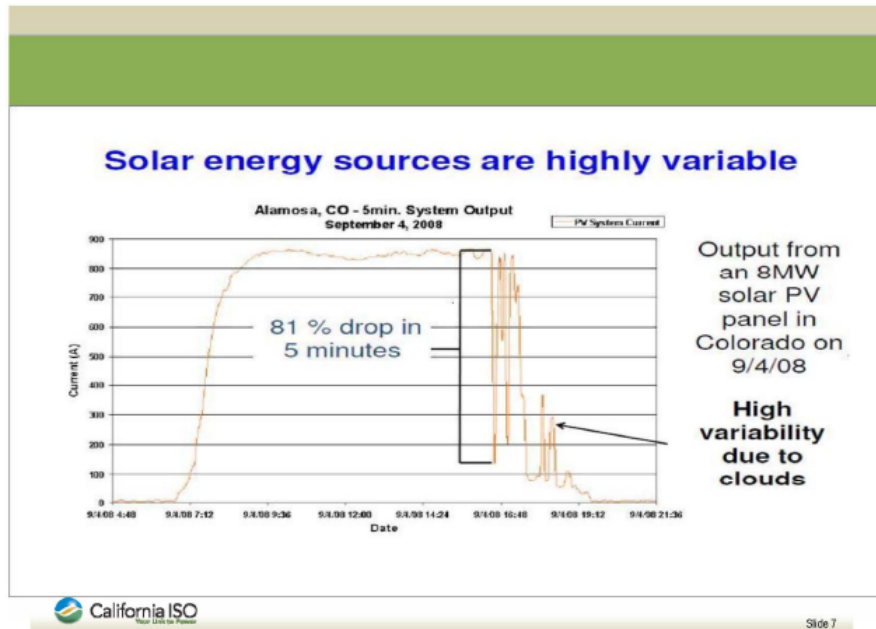
Lew et. al, "How do Wind and Solar Power Affect Grid Operations: The Western Wind and Solar Integration Study", National Renewable Energy Laboratory, (September 2009), p. 6

Up-Driven Bethe-trees

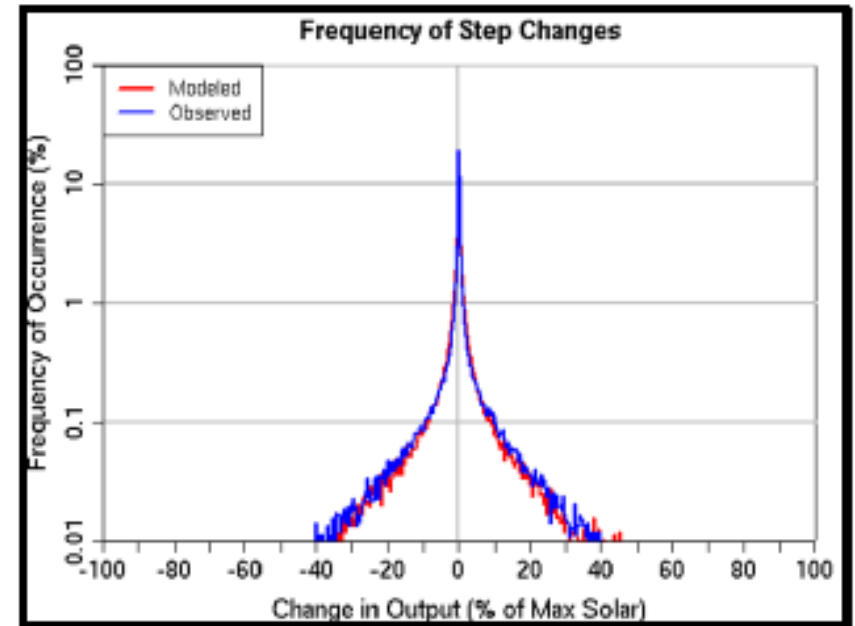


1. Power transmission systems are Bethe-lattices, formed for **downstream** energy transfer
2. PV cells feed energy
 - **upstream**
 - intermittently

Avalanches on Up-Driven Bethe-trees



Large fluctuations

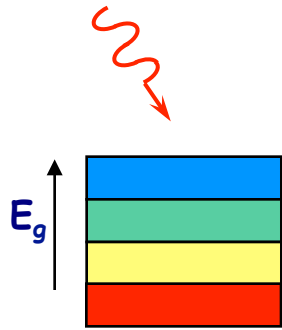
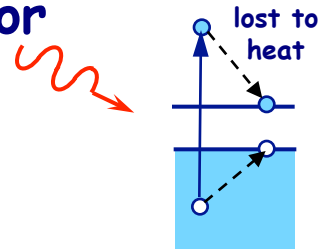


Broad distribution of avalanches

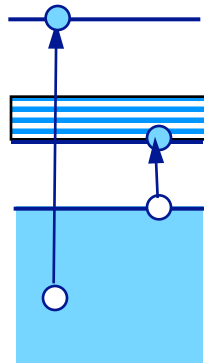
5. Other Path-breaking PV Designs

Present technology: 31% limit for

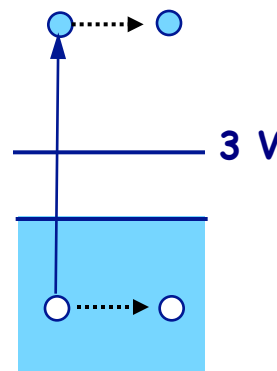
- single junction
- one exciton per photon
- relaxation to band edge



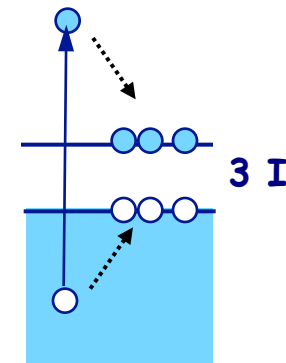
multiple junctions



multiple gaps



hot carriers



multiple excitons per photon

All Si Multi-junction Tandem Cell

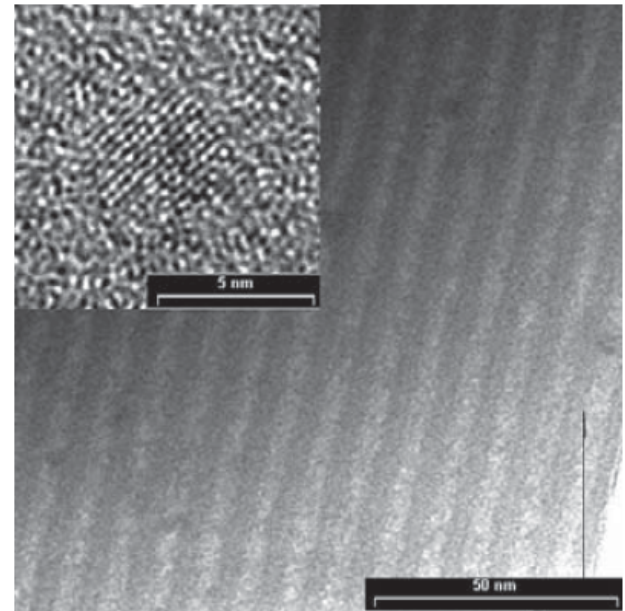
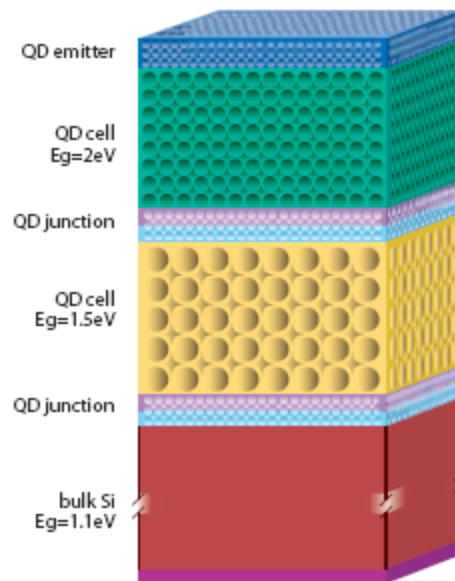
Layers of embedded quantum dots modify the Si bandgap:

-higher energy photons absorbed in top cell,

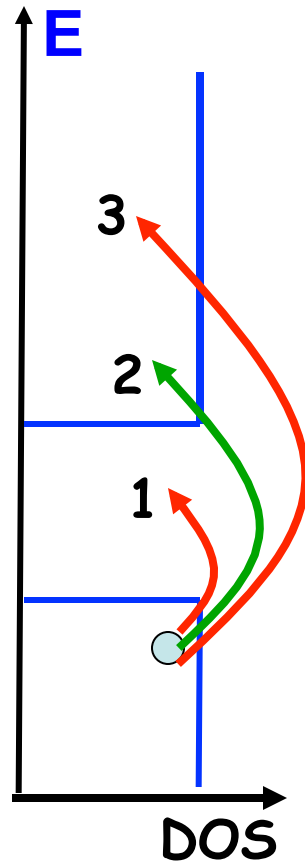
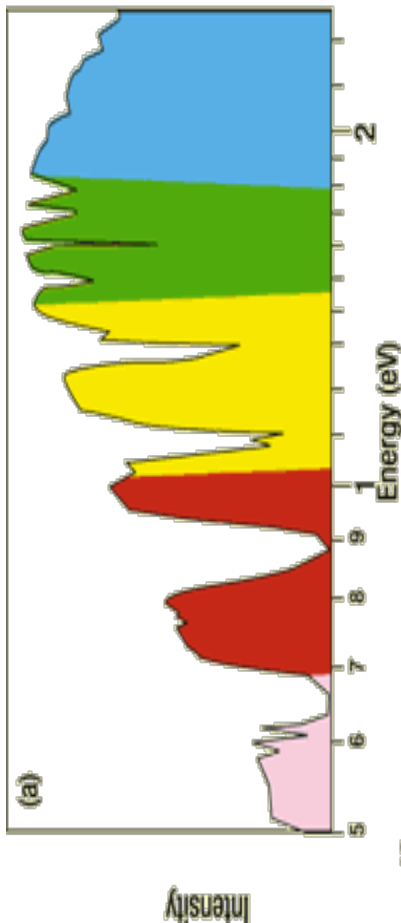
-medium energy photon in middle cell

-low energy photons in lowest cell

much less energy is wasted to phonons



IIIA. Multiple Exciton Generation: Basics



1. No absorption below gap:
photon wasted
2. Absorption to bottom of
conduction band: optimal
3. Absorption high into band:
excess energy to phonons: heats cell

Optimization of gap:
max efficiency: 31%
(Shockley Queisser 1961)

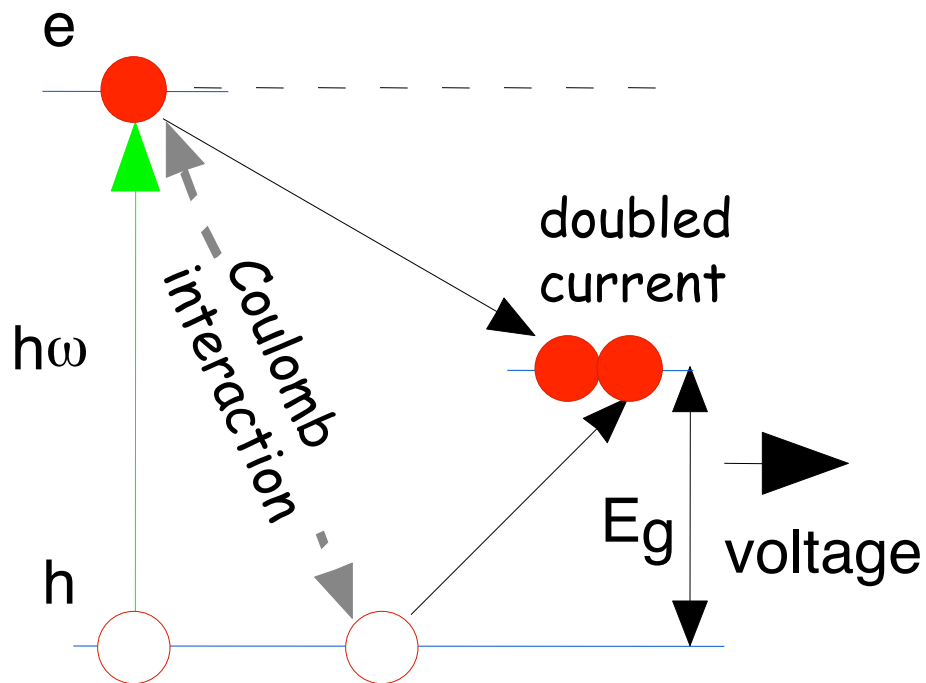
In real PV cells 80-85% of incident
solar energy is lost!!

Problem: 1 photon in-1 electron out

Multiple Exciton Generation

How to keep energy in electronic sector?

Photo-electron can relax by exciting second electron across gap



Need: stronger Coulomb interaction

1. In nanoparticles electrons cannot avoid each other ~ screening is reduced

(Nozik 2001-2005)

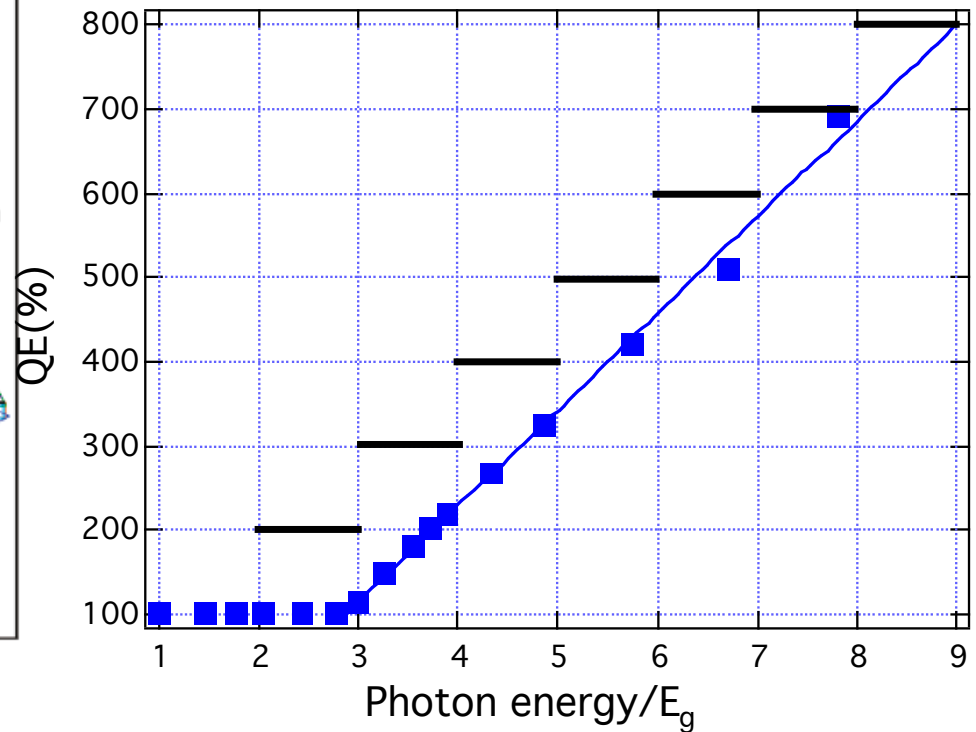
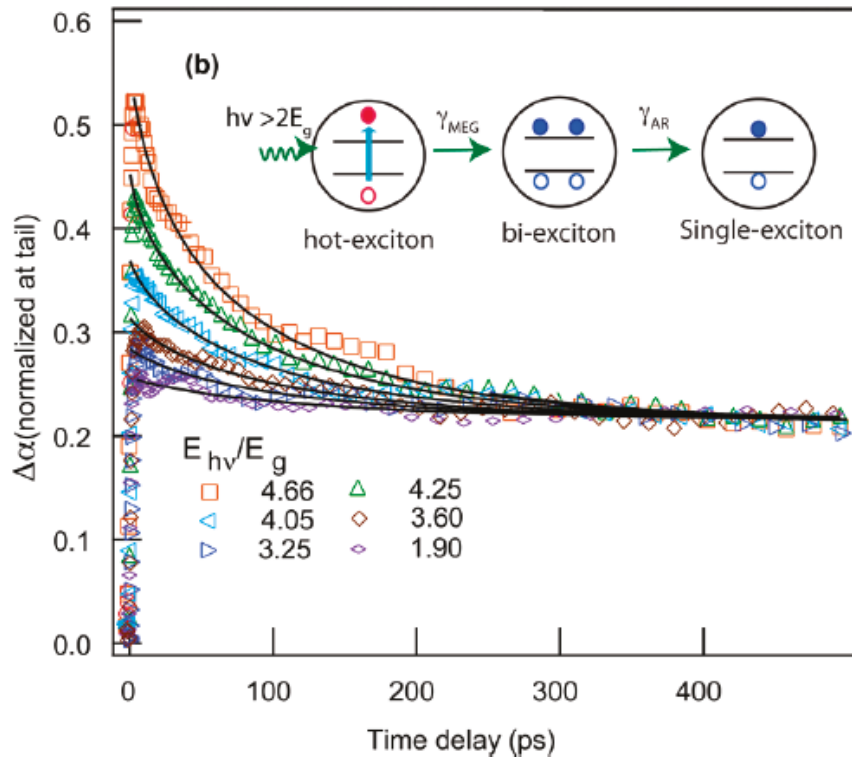
2. Alternative: Use Mott insulators - Manousakis

Max efficiency: 44-70%

MEG in Nanoparticles: The Discovery

Klimov, Schaller (2004) pump & probe:

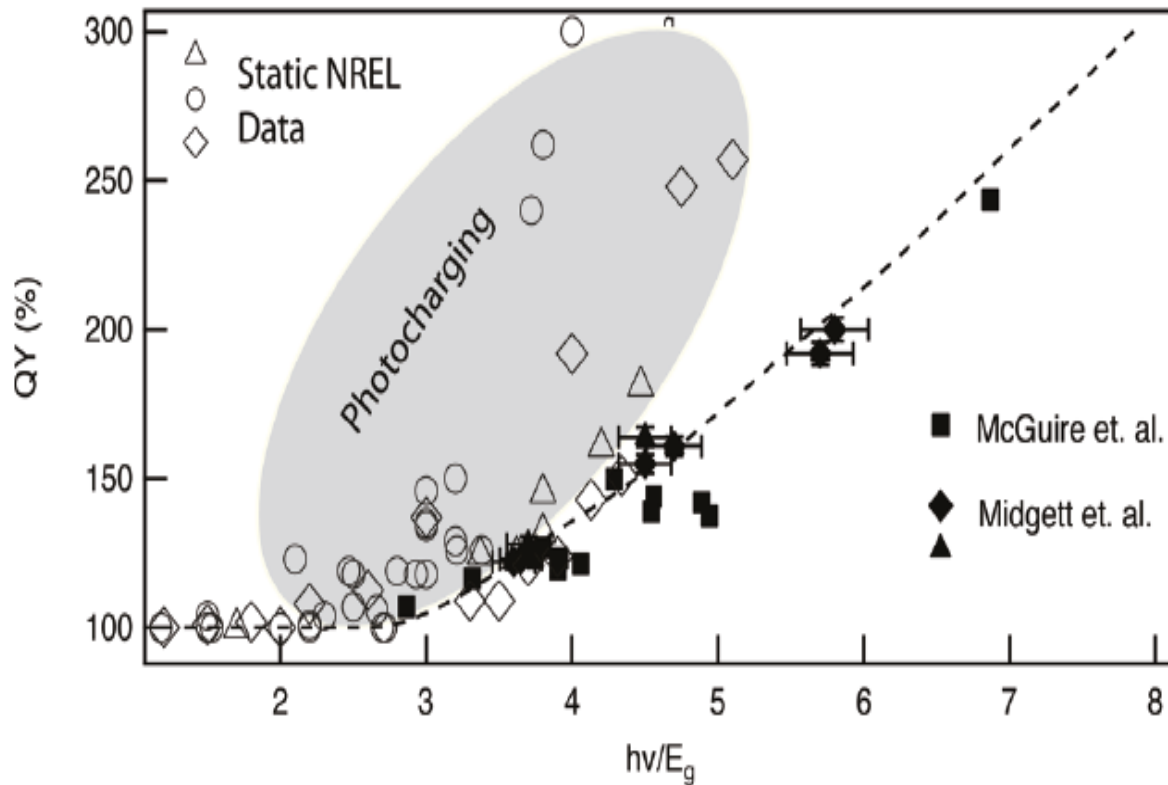
Quantum Yield (QY=#(electrons)/photon) up to 700%



MEG: Consensus Status

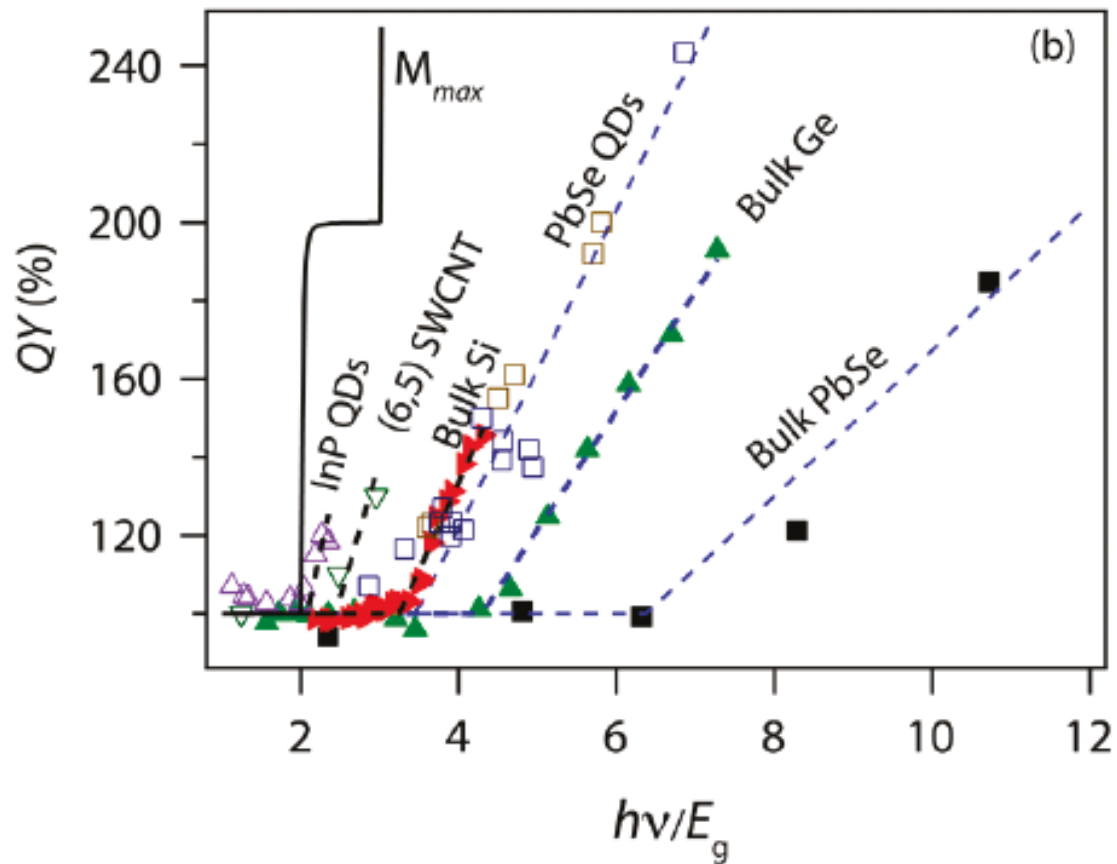
Beard(2011):

MEG is certainly present in NPs, albeit with lower efficiency



MEG: Efficient on Relative Scales, but Gap Big

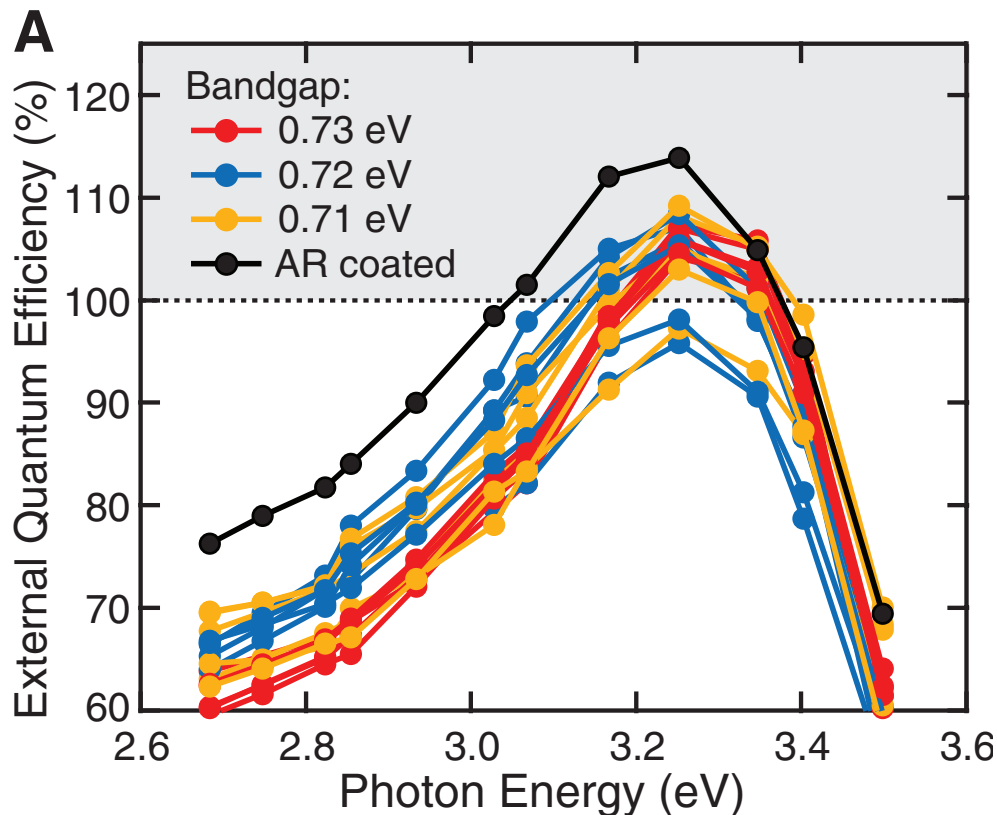
- * **Conversion efficiency good:** MEG more efficient in NPs than in bulk, as slope on **relative** energy scale $h\nu/E_g$ is closer to theoretical max.
- * **Threshold energy bad:** But E_g is larger in NPs, so on **absolute** energy scale NP solar cells absorb smaller fraction of solar spectrum



First working MEG solar cell: Dec. 2011

Peak External Photocurrent Quantum Efficiency Exceeding 100% via MEG in a Quantum Dot Solar Cell

Octavi E. Semonin,^{1,2} Joseph M. Luther,¹ Sukgeun Choi,¹ Hsiang-Yu Chen,¹ Jianbo Gao,^{1,3} Arthur J. Nozik,^{1,4*} Matthew C. Beard^{1*}



EQE > 100%:

Good

Fabrication needed
flammable hydrazine:

Not so much

IIIB. The Solar Collaborative at UCD/UCSC

1. Optimize/resolve competing demands/processes:

Quantum Confinement enhances Coulomb and thus MEG

Quantum Confinement increases gap out of solar spectrum

Quantum Confinement reduces mobility & charge extraction

2. MEG primarily demonstrated with toxic materials:

Environmental regulations discourage their use

The Solar Collaborative at UC Davis/UCSC

Experiment:

S.Kauzlarich - synthesize NPs

D.Larsen - photoluminescence (PL/TA) characterization of NPs

S.Carter - assemble NPs into working solar cells

Theory:

G.Galli, G.Zimanyi - gap reduction by manipulating NP shape,
A.Gali, M.Voros reconstruction, embedding

S.Wippermann,

D.Rocca

Z.Bai - code development for Bethe-Salpeter

D.Paul - multivariate analysis of PL/TA data

Experiment: Synthesize Si, Ge Nanoparticles

- synthesize Si, Ge, core-shell NPs with good yield
- narrow size distribution
- stable over long term

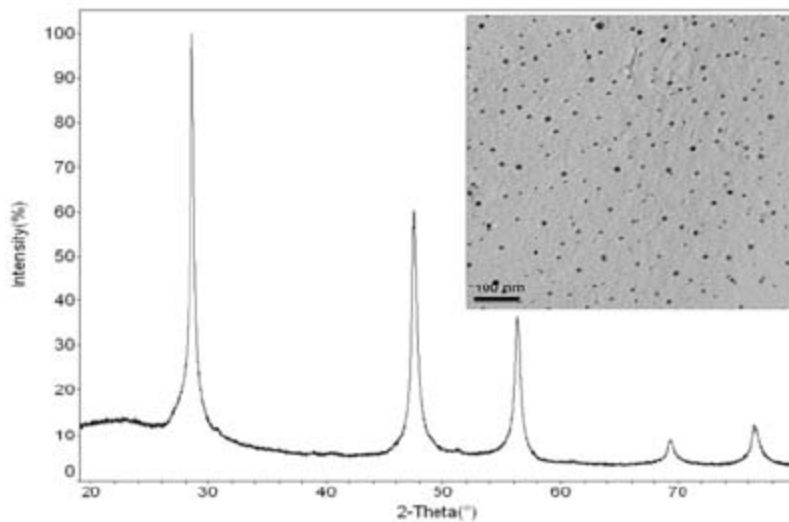
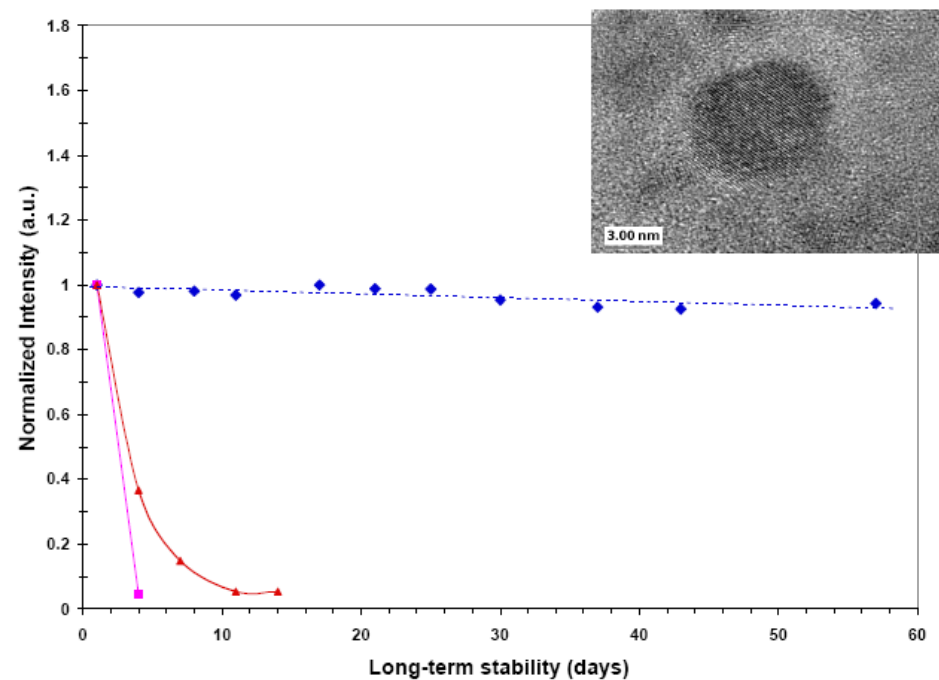
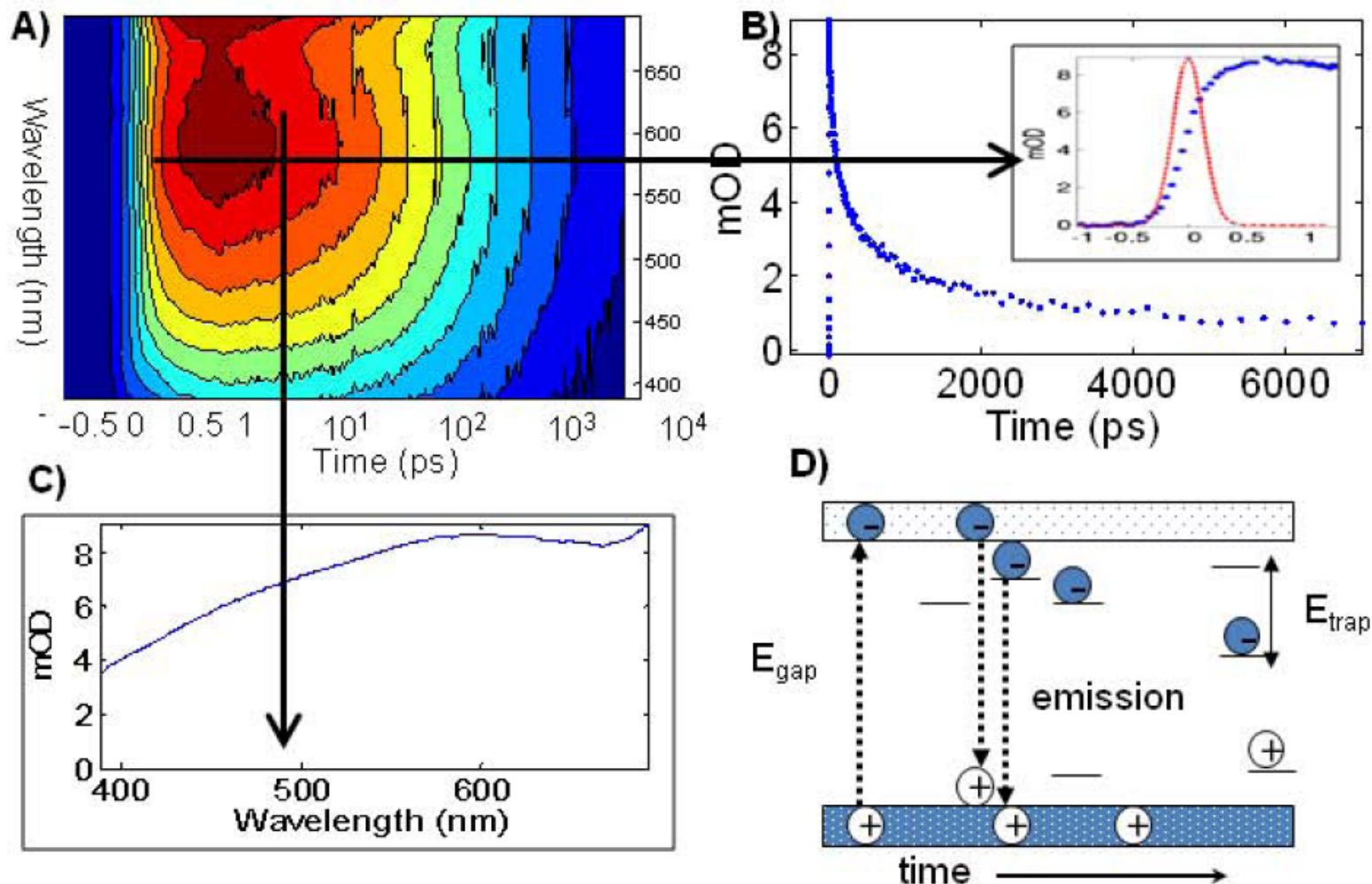


Fig. 5. Powder XRD pattern and corresponding TEM of Si NPs capped with APS prepared by a colloidal solution route.

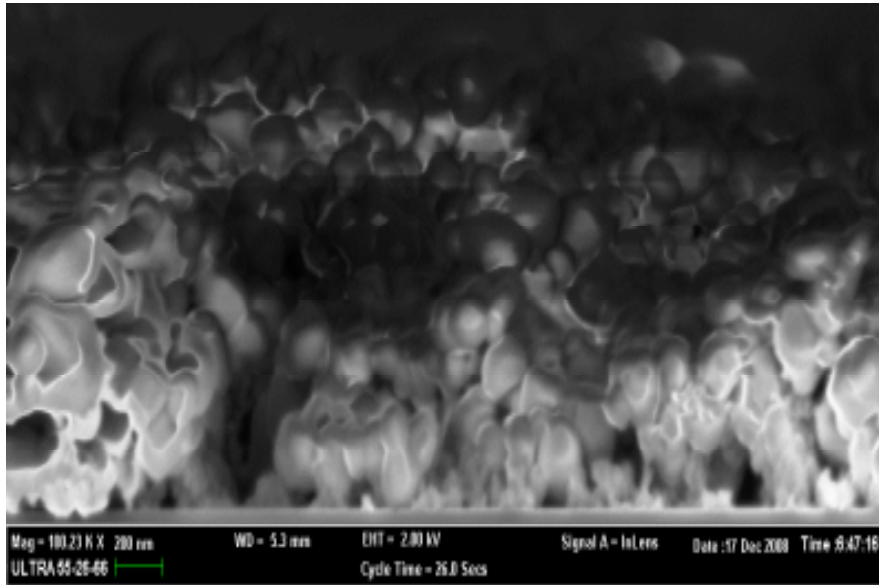


Multivariate Time Domain Analysis with Pump & Probe Lasers

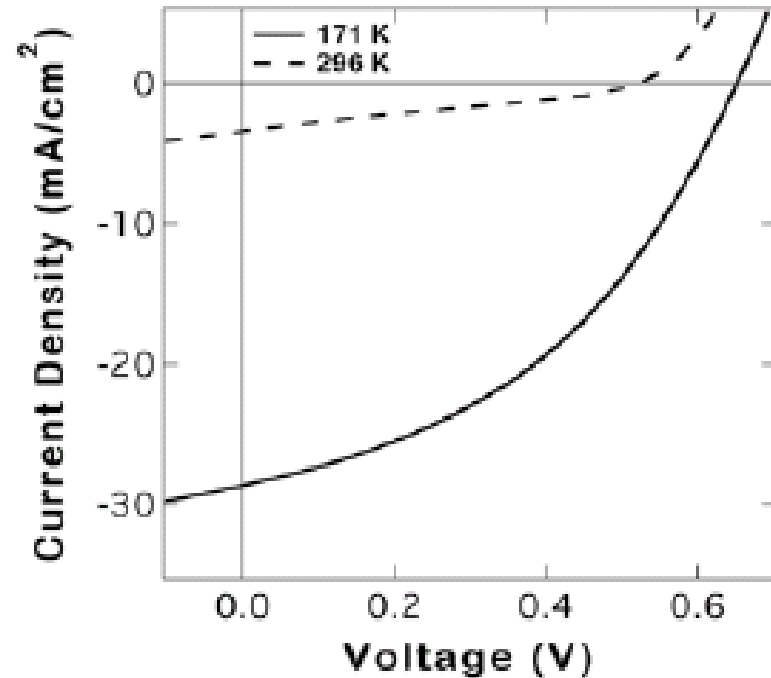
- separate different decay channels reliably
- 100 GB datasets, use advanced factor analysis



Fabricating Nanoparticle Solar Cells

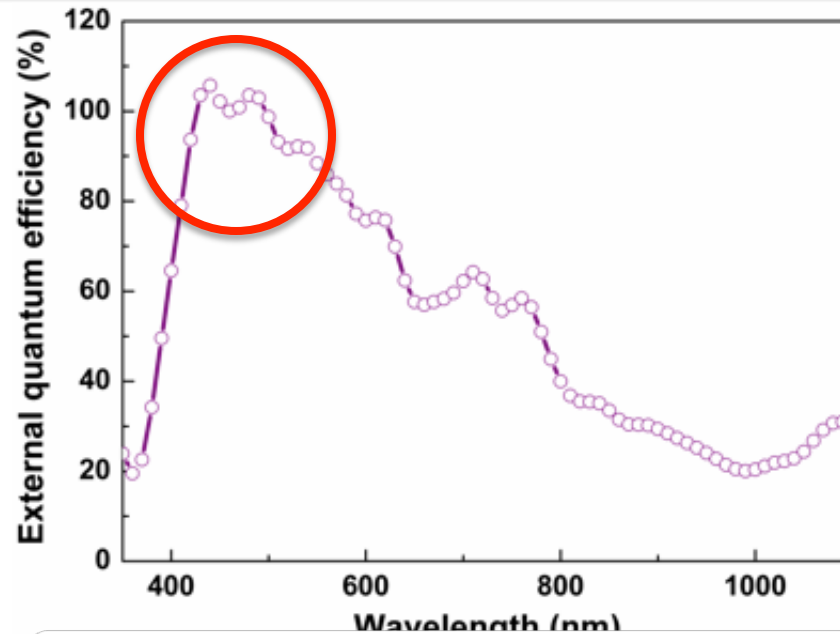
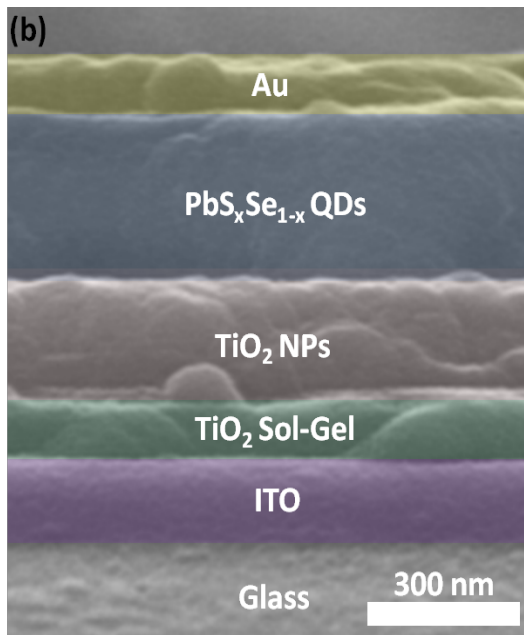
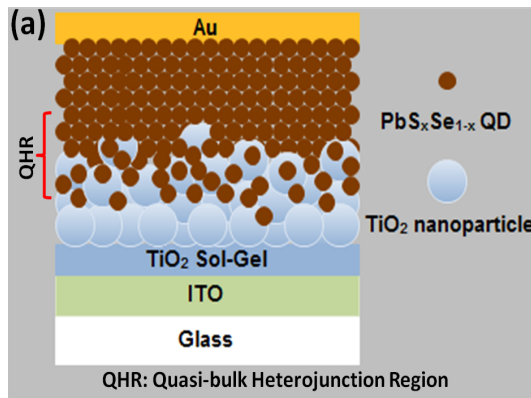


TEM image of ALD of Cu_2S onto TiO_x nanoparticle film with pore size of $<1\text{nm}$



I-V of PbS NP solar cell

Observation of Multiple Exciton Generation in a Functioning Solar Cell



Beard & Nozik
(Dec. 2011):
MEG in working
solar cell.
Used hydrazine:
combustible

Carter lab: EQE > 100% in a functioning solar cell. Optimized cell performance not by the use of hydrazine, but by varying the composition PbS_xSe_{1-x} .

The paper has been accepted in Nanotechnology

Theory: Turbo-charged Time-Dependent Density Functional Analysis

1. Managing Quantum Confinement

- 1.1. Surface reconstruction reduces the gap
- 1.2. Asymmetry reduces the gap
- 1.3. Charge extraction

2. Multi-Exciton Generation

- 2.1. Reconstruction can compensate confinement
- 2.2. Particle and hole localization

3. Si NPs with different phases

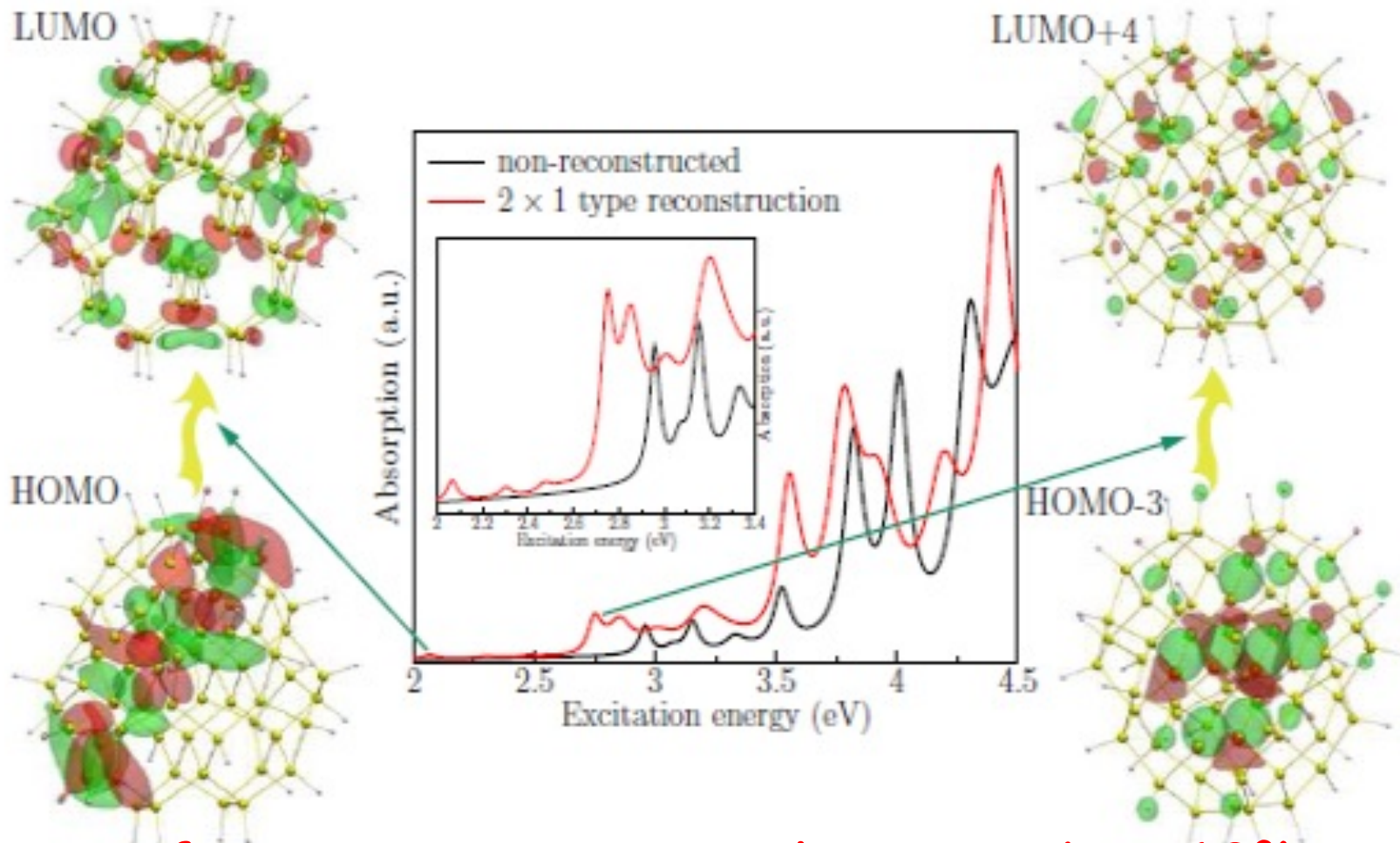
- 3.1. Another pathway to reduce the gap
- 3.2. The Harvard-MIT experiment

4. Si NPs with different embeddings

- 4.1. Precipitation- Delocalization - gap reduction

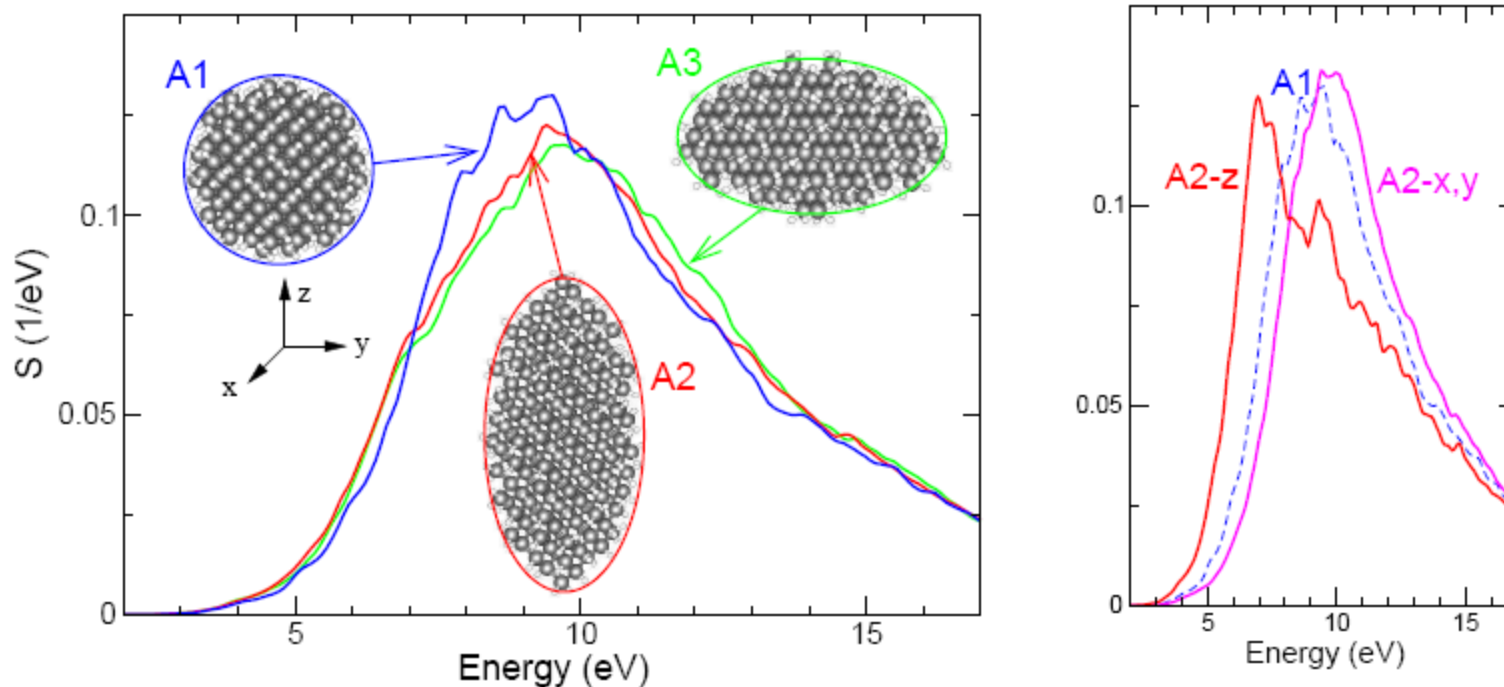
1. Managing Quantum Confinement:

1.1. Surface Reconstruction Reduces the Gap



Surface reconstruction reduces gap by ~10% or more

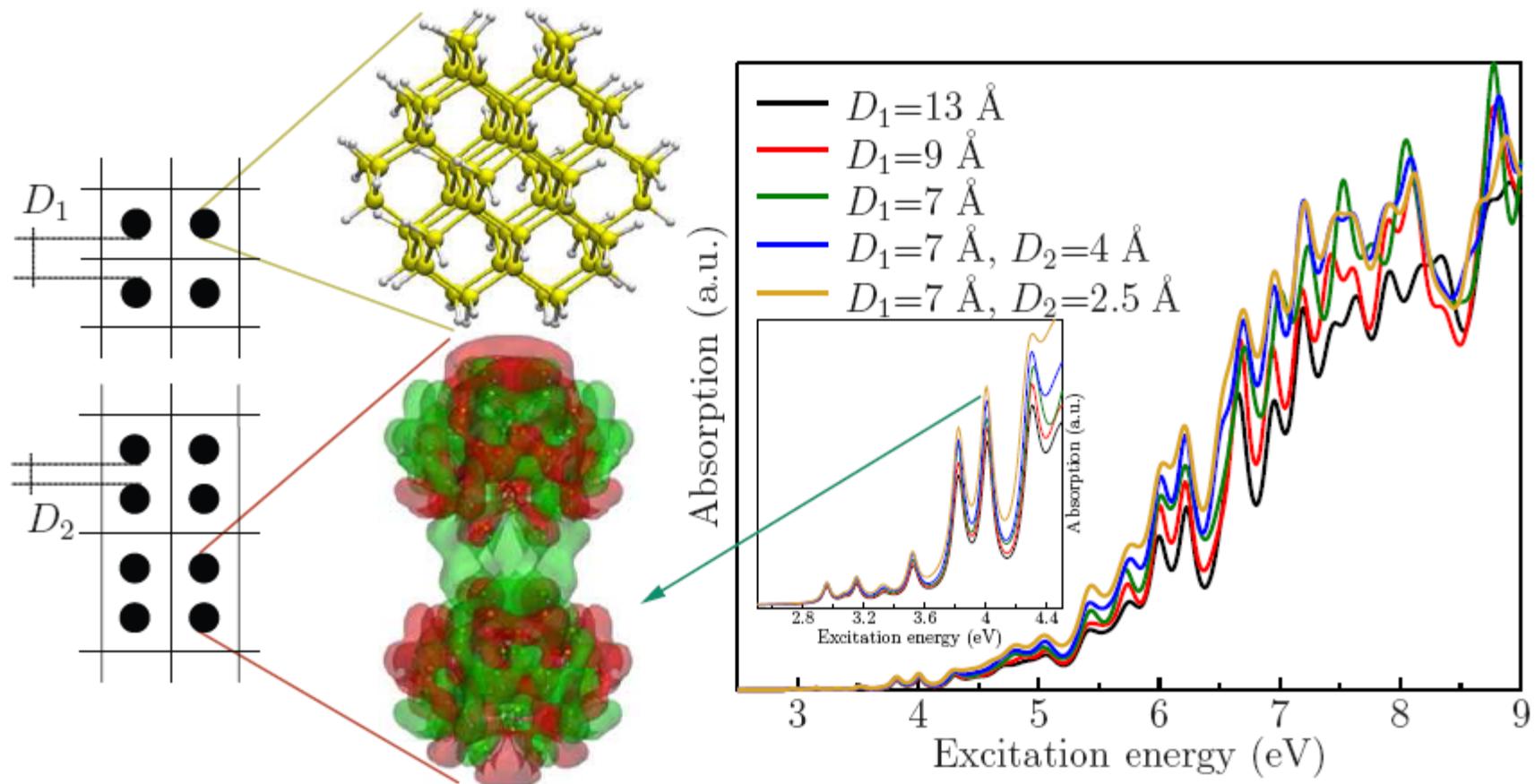
1. Managing Quantum Confinement: 1.2. Asymmetry Reduces the Gap



Reducing symmetry of shape reduces gap because a lot of transitions which were forbidden by selection rules become allowed: nanorods show strong MEG

1. Managing Quantum Confinement:

1.3. Charge Extraction less of a Problem



Wavefunction overlap at surprisingly large NP-NP separations -> can explain good charge extraction

2. Multi-Exciton Generation

2.1. Computational details

Fermi's golden rule for exciton- \rightarrow biexciton process with static RPA screened Coulomb interaction:

$$\Gamma_i = 2\pi \sum_f |\langle X_i | W | X X_f \rangle|^2 \delta(E_i - E_f)$$

$$\left\{ \begin{array}{l} \Gamma_j^+ = 2\pi \sum_{klc} (2|V_{lckj} - V_{kclj}|^2 + |V_{lckj}|^2 + |V_{kclj}|^2) \delta[\epsilon_j - (\epsilon_l - \epsilon_c + \epsilon_k)] \\ \Gamma_a^- = 2\pi \sum_{lbc} (2|V_{aclb} - V_{abl c}|^2 + |V_{aclb}|^2 + |V_{abl c}|^2) \delta[\epsilon_a - (\epsilon_b - \epsilon_l + \epsilon_c)] \end{array} \right.$$

Huge triple summation!

$$\Gamma_{ja} = \Gamma_a^- + \Gamma_j^+$$

$$V_{rsut} = \int \int d^3r d^3r' \psi_r^*(\mathbf{r}) \psi_s(\mathbf{r}) W(\mathbf{r}, \mathbf{r}') \psi_u^*(\mathbf{r}') \psi_t(\mathbf{r}')$$

$$W(\mathbf{r}, \mathbf{r}') = \int d^3r'' \epsilon_{\text{RPA}}^{-1}(\mathbf{r}, \mathbf{r}'') \frac{2}{|\mathbf{r}' - \mathbf{r}''|}$$

2. Multi-Exciton Generation

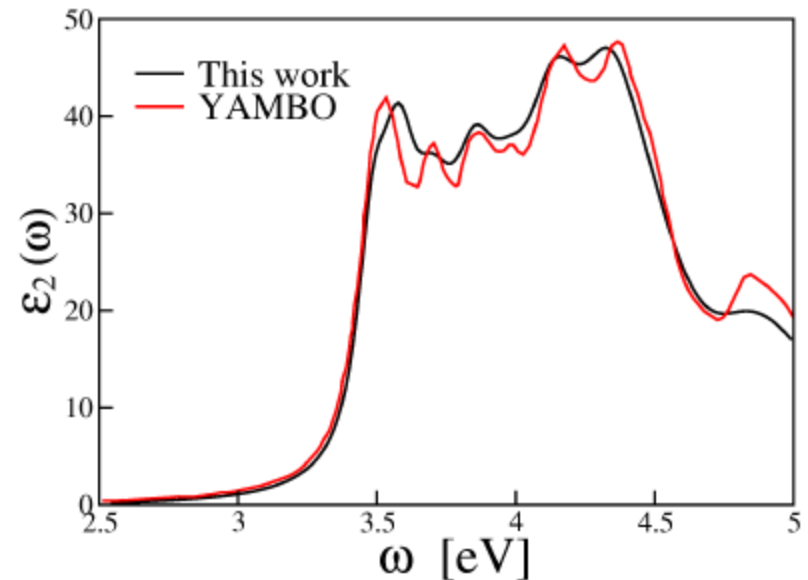
2.1. Computational details

a. Liouvillian super-operator matrix formalism

b. Projecting out unoccupied states - summation only over occupied states

c. Lanczos continued fraction solution of Bethe-Salpeter eq.

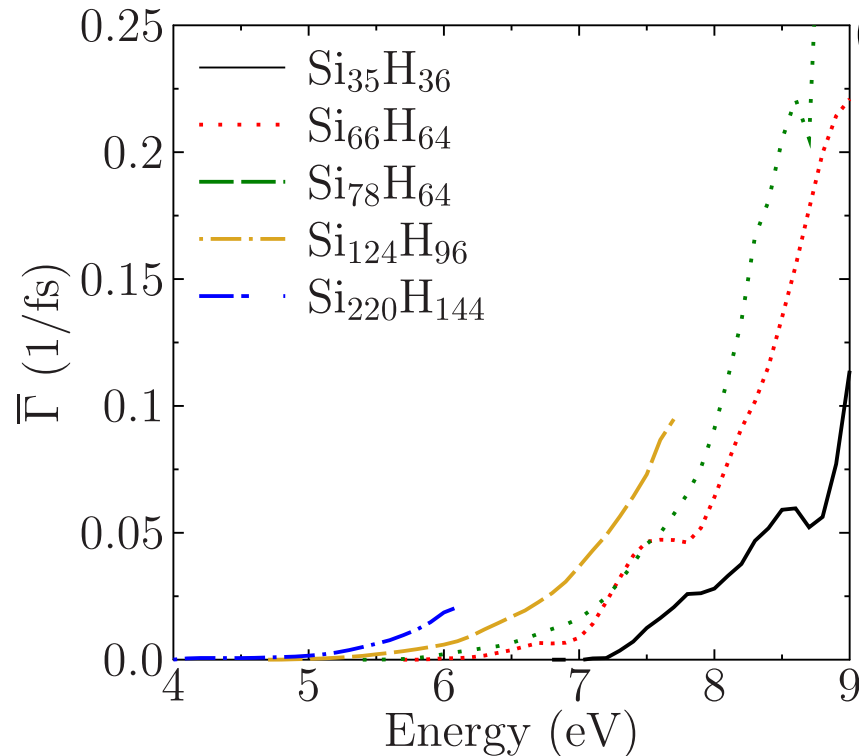
d. Comparison with YAMBO code - benzene: same results, considerably faster



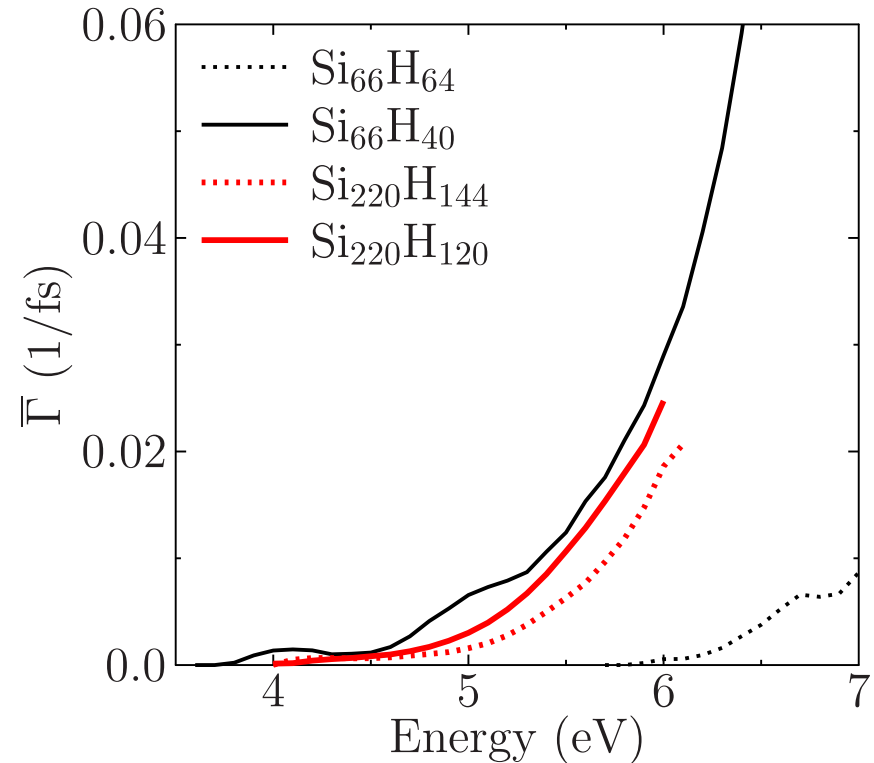
Yambo results from CPC 180, 1392 (2009)

2. Multi-Exciton Generation

2.2. Reconstruction Can Compensate Confinement



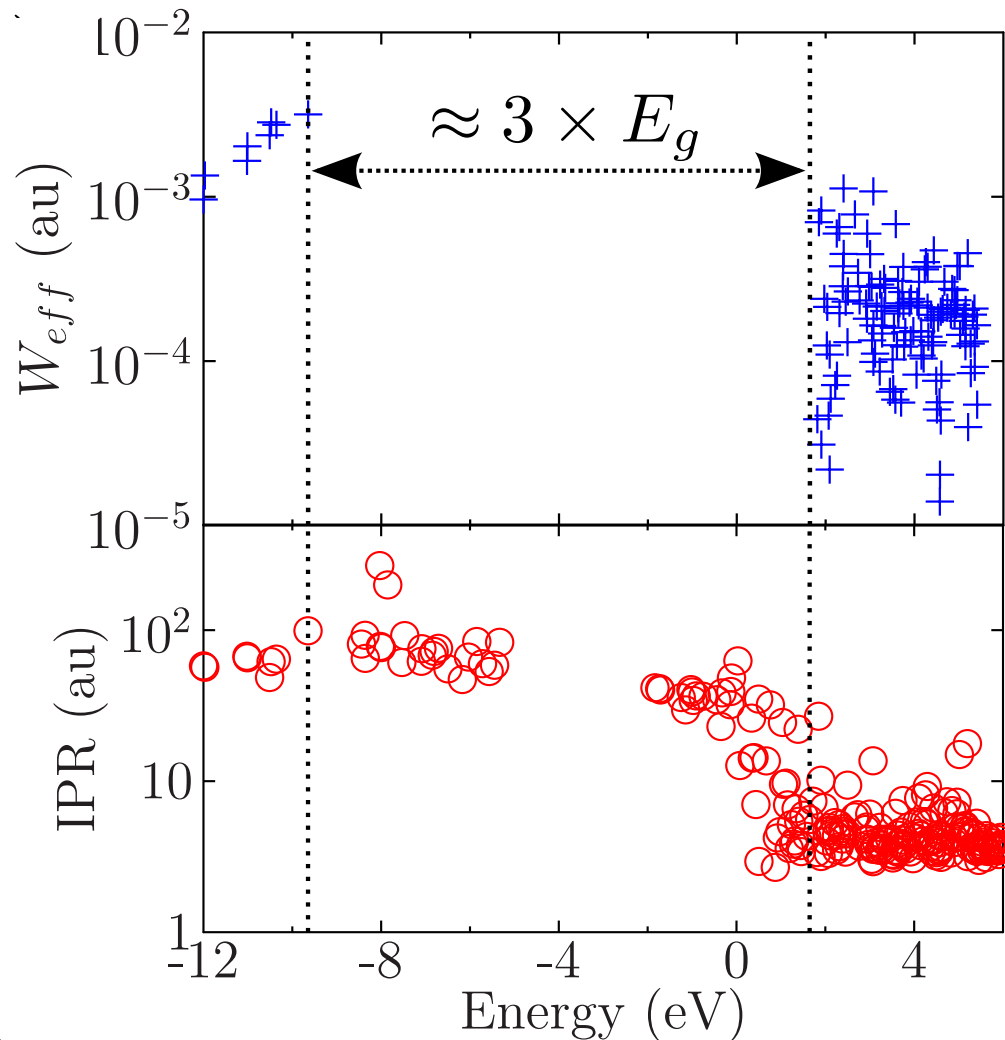
Quantum confinement enhances the gap in unreconstructed NPs



Reconstruction can completely compensate the gap enhancement

2. Multi-Exciton Generation

2.3. Of Particles and Holes



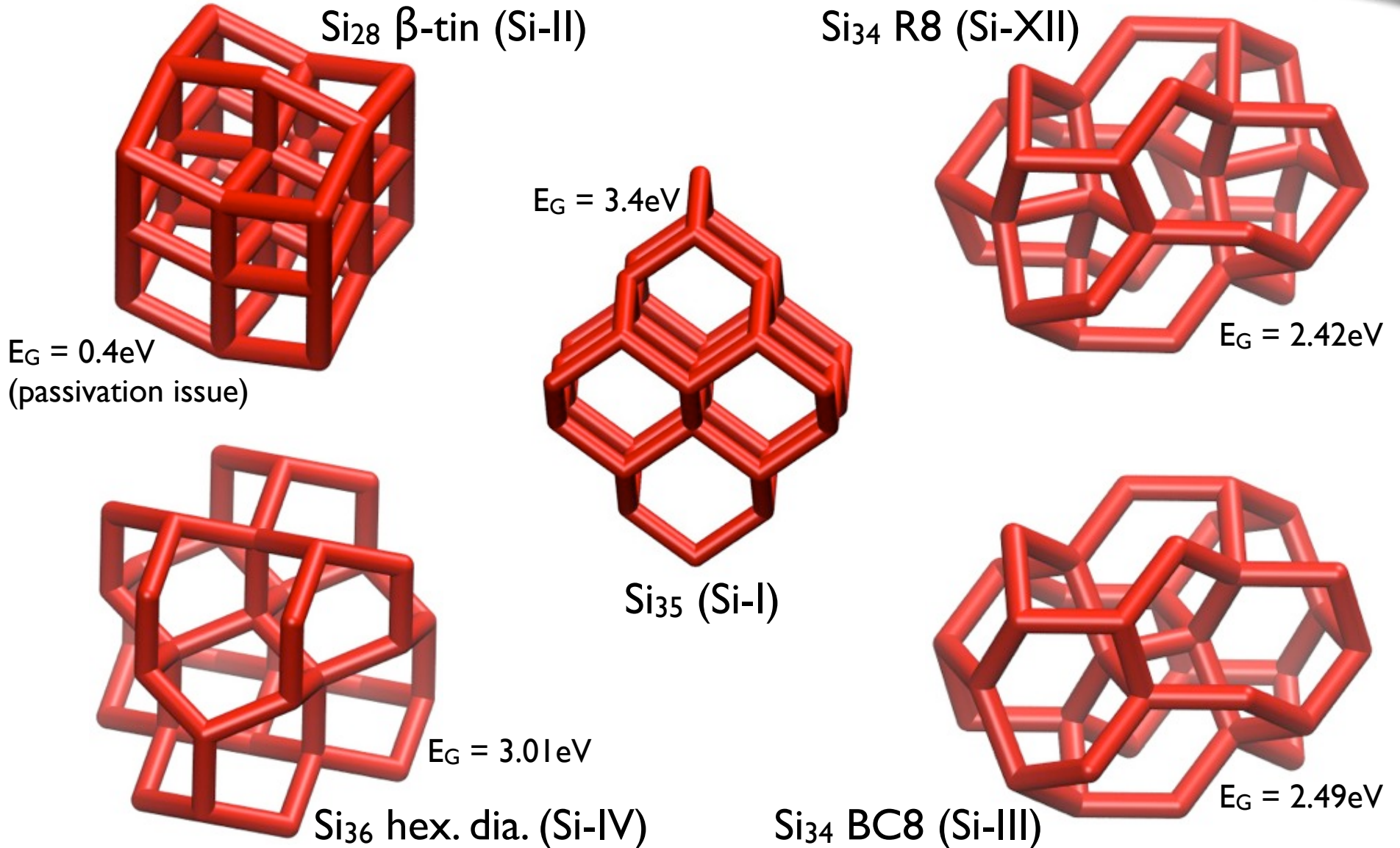
Effective Coulomb interaction is very different for electrons and holes

Inverse Participation Ratio (IPR) explains:

Holes are much more localized than electrons

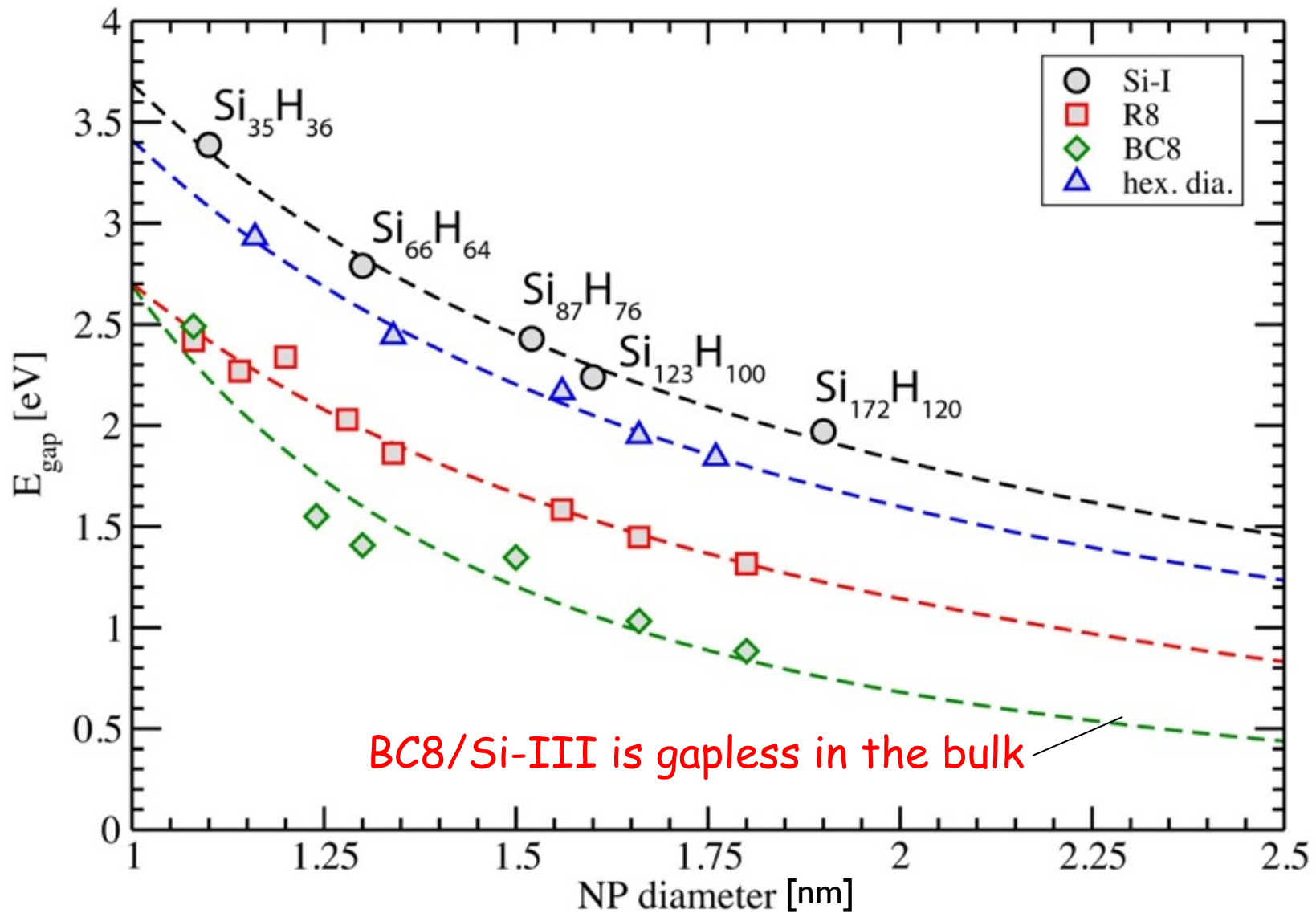
3. High Pressure Phases of Si NPs:

3.1. Reduce Gap by using Bulk-Gapless Si Phases



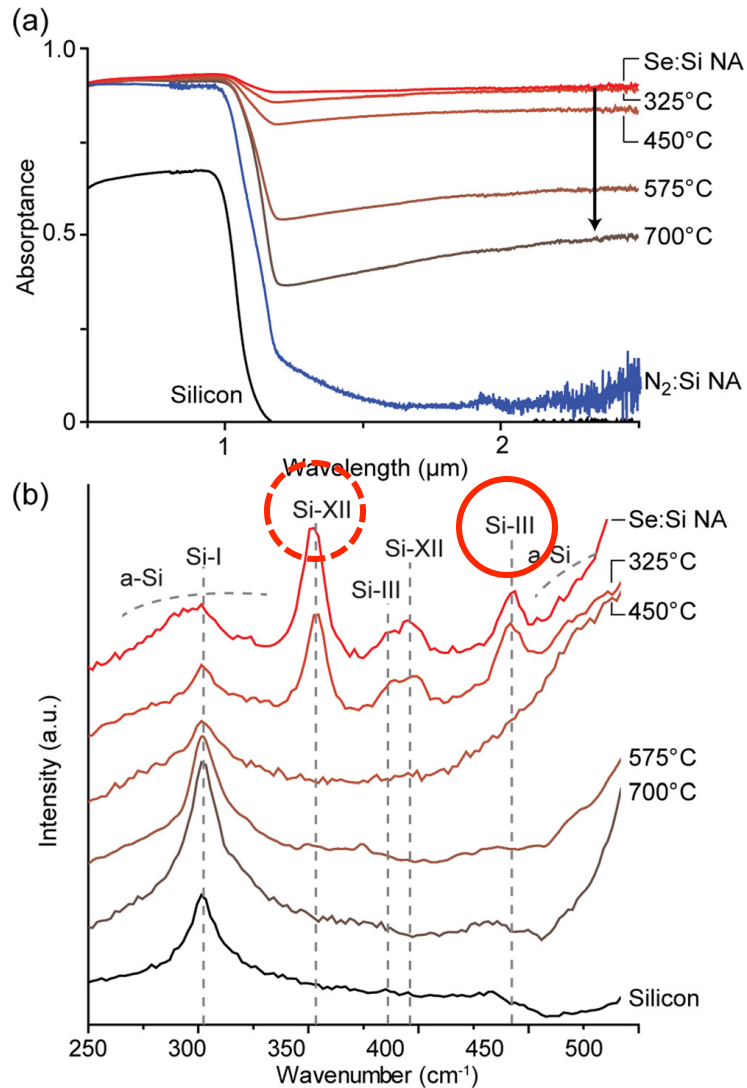
3. High Pressure Phases of Si NPs:

3.1. Gap reduction in BC8/Si-III



3. High Pressure Phases of Si NPs:

3.2. Mazur/Gradecak group results



JOURNAL OF APPLIED PHYSICS **110**, 053524 (2011)

Pressure-induced phase transformations during femtosecond-laser doping of silicon

Matthew J. Smith,¹ Yu-Ting Lin,² Meng-Ju Sher,³ Mark T. Winkler,³ Eric Mazur,^{2,3} and Silvija Gradečak^{1,a)}

1. The presence of BC8/Si-III phase confirmed by Raman scattering

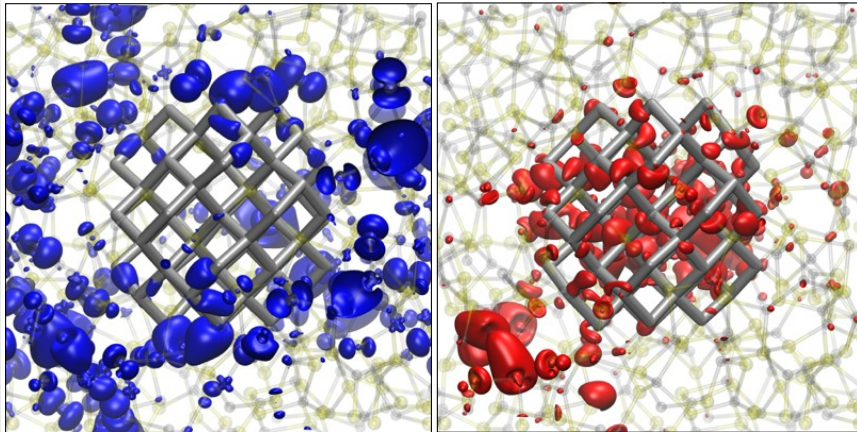
2. When BC8/Si-III phase is annealed away, subgap absorptance is greatly reduced

4. Charge Separation and Extraction

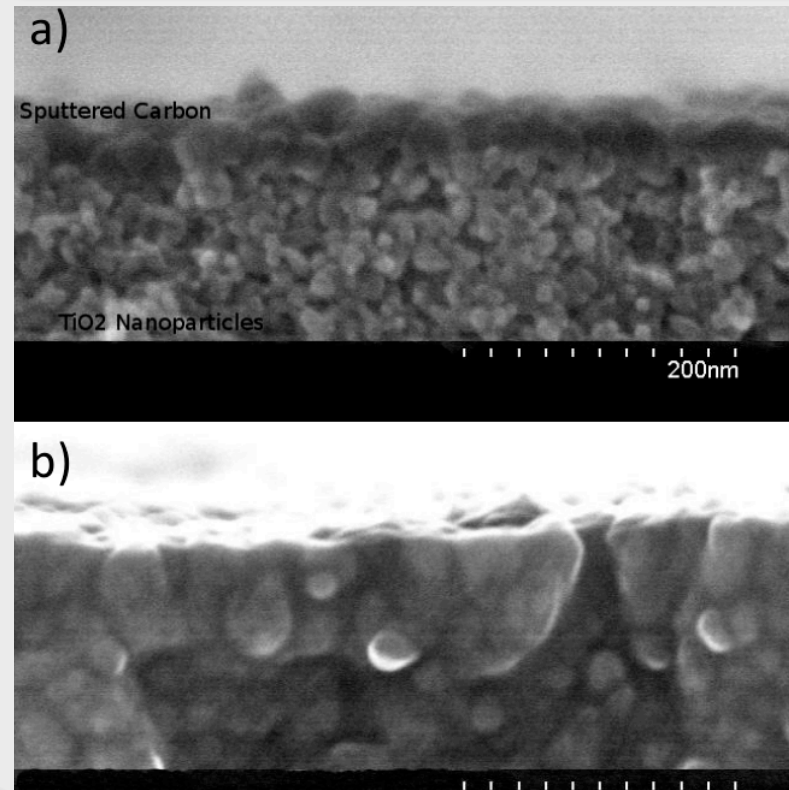
4.1. Complementary Charge Transport Networks: Si in ZnS

Valence band edge states:
Localized in host matrix

Conduction band edge states:
Localized in nanoparticle



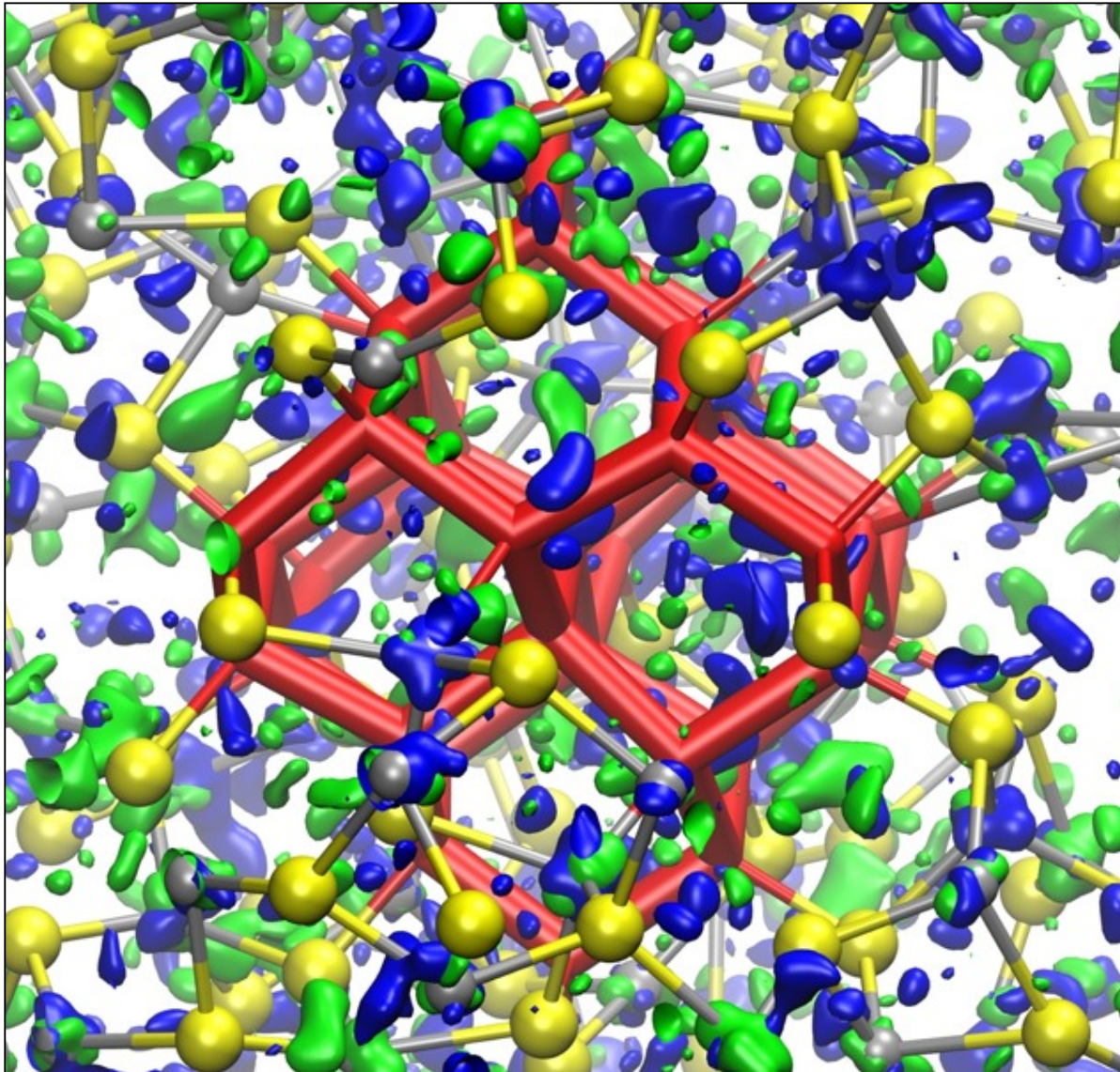
4.2. Towards Atomic Layer Deposition of ZnS on Ge films



SUMMARY

1. Solar energy problem is intellectually complex & morally honorable
2. There are many entry points for physicists
3. Multiple Exciton Generation is a most promising paradigm
4. Quantum Confinement enhances the Coulomb interaction and MEG
5. Its two negative effects, the gap enhancement and the charge localization can be reduced or eliminated by:
 - (a) surface reconstruction
 - (b) symmetry reduction: nanorods
 - (c) NPs with bulk-low-gap/gapless phases
 - (d) judicious NP embedding to separate electrons and holes
6. Theory uses advanced many-body methods: Liouville operators, Bethe-Salpeter eq., Self-consistent self-energy $\text{Im}\Sigma$, Projection methods for summations, Lanczos continued fractions

4.1. Embedding: Si NPs in ZnS



HOMO: blue
LUMO: green
Courtesy of Jelly Beans Co.

1. HOMO and LUMO orbits delocalized: good for charge extraction
2. S precipitates on NP boundary, Zn forms a metallic outer host
3. Host gap reduced allowing NP wave fc. to delocalize

Where are the Frontiers of Energy Research in a Stormy World?

